

# Nuclear data, uncertainties and their applications

## Part 3: nuclear data uncertainties for reactors and fuels

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- Discussions



#### All slides can be found at:

ftp://ftp.nrg.eu/pub/www/talys/bib\_rochman/presentation.html).

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General comments:

- l uncertainties are not errors (and vice versa),
- I uncertainties should now be given with every data (seems obvious ?),
- III they are related to risks, quality of work, perception, fear, safety...

Uncertainty  $\Leftrightarrow$  safety  $\Leftrightarrow$  professionalism

- ₩ True uncertainties do not exist ! They are the reflection of our knowledge and methods.
- III All the above for covariances
- Image: The importance of nuclear data uncertainties should be checked. If believed negligible, please prove it !



#### Nuclear data uncertainties



Nuclear data Uncertainty propagation

- reactors ( $k_{eff}$ ,  $\beta_{eff}$ , void, Doppler, reaction rates, you name it),
- fuel storage (criticality),
- burn-up (inventory, radiotoxicity),
- transient behaviour...

#### TMC for nuclear data uncertainty propagation, what else ?

- $\bigcirc$ ( $\bigcirc$  $(\cdot)$  $\bigcirc$  $\bigcirc$  $\bigcirc$  $(\cdot, \cdot)$  $(\cdot)$  $(\cdot)$ 
  - + No MF 32-35 (no 2 Gb files) but every possible cross correlation included
  - + No approximation but true probability distribution
  - + Only essential info for an evaluation is stored
  - + No perturbation code necessary, only "essential" codes
  - + Feedback to model parameters
  - + Fission yields and decay data included
  - + QA
  - Needs discipline to reproduce
  - Memory and computer time
  - Complexity for full reactor core calculation not fully investigated
  - Role of data centers would change

#### TMC for nuclear data uncertainty propagation

"In general, this paper will or will not be a breakthrough in methodology if the [practicality and robustness] can or can not be demonstrated.",

ANE Referee, May 2008

"What about actinides, what about real systems ?", JEFF &WPEC meetings, May-June 2008

#### TMC for nuclear data uncertainty propagation

"In general, this paper will or will not be a breakthrough in methodology if the [practicality and robustness] can or can not be demonstrated.", ANE Referee, May 2008

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Okay, let's go from academic solutions ( $\clubsuit$ ) to mass/applied production ( $\checkmark$ ) !

- TALYS calculation + Resonance parameters (RP) + uncertainties
- 5 100 to 2000 ENDF files per isotope from <sup>6</sup>Li to <sup>252</sup>Cf
- 3 190 criticality-safety benchmarks (> 60 000 calculations) from the ICSBP
- Mo All Oktavian shielding benchmarks (neutrons and gammas)
- No Reactivity swing for a LWR using an "Inert Matrix Fuel" (Pu and Mo)
- $\delta \approx k_{eff}$  for a HTR (PBMR), ESKOM specifications
- No Inventory





#### **Example with <sup>238</sup>U: Monte Carlo calculations**



### Examples with <sup>63</sup>Cu(n,2n) and <sup>65</sup>Cu(n,el)











#### **Examples of criticality benchmarks for** <sup>19</sup>**F**







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## **Examples of criticality benchmarks for** $^{180-186}$ **W and** $^{240}$ **Pu**



#### **Examples of reactivity swing**



#### **Examples on shielding benchmarks**



- Oktavian: Leakage current spectrum from the outer surface of a spherical pile of material, 14 MeV D-T neutron source at the center of the pile. (Al, Cu, Si, Ti, Cr, Mn, Co...)
- □ FNS: Slabs of material of varying thickness, at five different angles, 20 cm from a 14 MeV D-T neutron source. (Fe, W).
- □ LLNL Pulsed Spheres: Time-of-Flight measurements through spherical shells of varying thickness, 14 MeV D-T neutron source. (Al, Mg, Fe).

#### **Application for Cr Oktavian benchmark**



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#### **Application for Mn Oktavian benchmark**



#### **Application for Si Oktavian benchmark**



#### **Application for W FNS benchmarks**



#### **Application for Fe FNS benchmarks**



#### **Application for Mg LLNL benchmarks**



#### **Results for the ESFR parameters**

The sodium void reactivity (SVR) in units of dollars (\$) can be obtained with the following equation :

$$SVR = \frac{k_2 - k_1}{k_1 k_2} \frac{1}{\beta_{\text{eff}}} \times 10^5,$$
 (1)

where the number of delayed neutron  $\beta_{eff}$  (in units of pcm) and the  $k_{eff}$  values are obtained from the MCNP calculations.

 $k_1$  corresponds to the core flooded with Na coolant, and  $k_2$  to the same core voided of Na coolant.

In both cases the Na coolant present in the axial and radial reflectors is supposed to remain unchanged.

Main components: <sup>23</sup>Na, <sup>56</sup>Fe, Zr, <sup>238</sup>U, <sup>239,240</sup>Pu Most sensitive reactions: <sup>239</sup>Pu(n,f) and <sup>238</sup>U(n, $\gamma$ )



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#### **TMC versus Perturbation method**

- ① Obtain uncertainties on a large-scale models due to nuclear data uncertainties
- ② Systematic approach, reliable and reproducable

#### Solution (1): Total Monte Carlo



#### Solution (2): Perturbation method

 $\implies$  MCNP+ Perturbation cards+covariance files



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#### **TMC and Perturbation method**



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#### **Necessary software**



#### **Convergence and consistency of v-bar and resonance parameters**



#### **Convergence TMC/Perturbation**



#### **TMC versus Perturbation: Results**

Comparison TMC-Perturbation methods for a few  $k_{eff}$  benchmarks. The ratio in the last column is "TMC over Perturbation".

		Total Monte Carlo	Perturbation	Ratio
Benchmark	Isotopes	Uncertainty	Uncertainty	
		due to nuclear	due to nuclear	
		data (pcm)	data (pcm)	
hst39-6	<sup>19</sup> F	330	290	1.16
hmf7-34	<sup>19</sup> F	350	290	1.21
ict3-132	<sup>90</sup> Zr	190	150	1.29
hmf57-1	<sup>208</sup> Pb	500	410	1.22
pmf2	<sup>239</sup> Pu	840	720	1.16
pmf2	<sup>240</sup> Pu	790	650	1.21

#### **Results: Details of the TMC-Perturbation methods for** $^{19}$ **F** $k_{eff}$ **benchmarks**

<u>chmarks</u>			uious io	<b>L L N</b> eff	NRC
	hs	t39-6 <sup>19</sup> F	hm	<b>f7-34</b> <sup>19</sup> <b>F</b>	
	$\Delta \mathbf{k}$	K <sub>eff</sub> (pcm)	$\Delta \mathbf{k}$	K <sub>eff</sub> (pcm)	—
	TMC	Perturbation	TMC	Perturbation	
Total	330	290	350	290	_
MF2	280	240	310	280	
MF3	170	160	75	105	
MF4	100	-	80	-	
MF6	30	-	35	-	

# Results: Details of the TMC-Perturbation methods for <sup>239,240</sup>Pu k<sub>eff</sub> benchmarks

	pn	nf2 <sup>239</sup> Pu	<b>p</b> n	nf2 <sup>240</sup> Pu
	$\Delta \mathbf{k}$	K <sub>eff</sub> (pcm)	$\Delta \mathbf{k}$	K <sub>eff</sub> (pcm)
	TMC	Perturbation	TMC	Perturbation
Total	840	720	790	650
MF1	400	-	370	-
(n,inl)	170	140	70	50
(n,el)	250	240	30	40
(n,γ)	100	100	30	30
(n,f)	720	660	730	640
MF4	20	_	20	_
MF5	50	_	30	_
MF6	50	_	30	_

#### TMC vs. perturbation: pro and cons

- Given First attempt to compare two uncertainty propagation method
- Control TMC: more general and exact answer, does not require special codes, more exhaustive
- 👶 but slower
- Perturbation: approximate, require special processing and codes, limited
   but faster
  - TMC uncertainties 15 to 30 % larger than from perturbation

Perturbation approach still dominates the *market*, but for how long ?

#### **Application to a Pebble Bed Modular Reactor (PBMR)**

- ✤ Model of a fuel pebble
- \* Fuel particles, surrounded by coating layers, explicitly modeled
- \* Regular rectangular lattice of fuel particles



#### **Application to a Pebble Bed Modular Reactor (PBMR)**

- ✤ Hexagonal close packed lattice
- Moderator region consists of homogeneous moderator pebbles as the fuel, reflectors and shields as defined by ESKOM



#### **PBMR:** Neutron Flux spectrum



Neutron flux spectrum at the radial core boundary (Almost no neutron abov@ochman - 41/66 Budapest 2012 Part 3

## **PBMR:** <sup>12</sup>C nuclear data

- ✤ For neutron energy lower than few MeV: only elastic and capture cross sections
- \* JEFF-3.1:  $\sigma_{th}$  (n,el)= 4.746 ± 0.002b and  $\sigma_{th}$  (n, $\gamma$ )= 3.53 ± 0.07mb
- \* All (n,el), (n, $\gamma$ ), angular distribution and emission spectra randomly varied



#### **PBMR: Results**



- \* Convergence achieved after  $\simeq 350$  runs (10 days of 15 CPU)
- More runs would be suitable
- \* Effect of other isotopes ( $^{13}$ C, Si, fission products and of course actinides)

TMC is the only method to propagate uncertainties due to thermal scattering data (no covariances exist)

In the case of H in H<sub>2</sub>O, the incoherent inelastic scattering is the major component and the coherent and incoherent elastic scattering can be neglected. The inelastic scattering is described by the scattering law  $S(\alpha,\beta)$  at different temperatures.

$$\frac{\partial^2 \sigma(E \to E', \mu)}{\partial E' \partial \mu} = \frac{\sigma_b}{2kT} \sqrt{\frac{E'}{E}} S(\alpha, \beta)$$
(2)

with *E* and *E'* the incident and outgoing neutron energies in the laboratory system,  $\mu$  is the cosine of the scattering angle in the laboratory system,  $\sigma_b$  is the characteristic bound scattering cross section for the material (water in this case) and *kT* is the thermal energy in eV. S( $\alpha$ , $\beta$ ) is the asymmetric form of the scattering law, which depends on two variables: the momentum transfer  $\alpha$  and the energy transfer  $\beta$ :

$$\alpha = \frac{E + E' - 2\sqrt{EE'\mu}}{AkT}$$
(3)  
$$\beta = \frac{E' - E}{kT}$$
(3)  
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- 1. create input parameters for the LEAPR module of NJOY,
- 2. run LEAPR to generate thermal scattering data in ENDF format "MF 7, MT 4" (incoherent inelastic data in terms of  $S(\alpha,\beta)$  tables for different temperatures),
- 3. use the ENDF file with the THERMR module of NJOY to generate pointwise thermal scattering cross sections,
- 4. use the ENDF file and the output of THERMR with the ACER module of NJOY to generate thermal scattering data for the MCNP code in the ACE format,
- 5. and finally repeat *n* times the previous steps with random input parameters for LEAPR.

The central (or nominal) values for all model parameters to be used in LEAPR are the values used for the JEFF-3.1.1 evaluation.





Figure 1: Top: incoherent random inelastic scattering cross section of H in H<sub>2</sub>O compared to experimental data and the inelastic cross section from the JEFF-3.1.1 library. BuBotto 2012 Determination on the inelastic cross section calculated from 1330 random in-



Figure 2: Energy-energy correlation matrix for the incoherent inelastic scattering of H in  $H_2O$ . Note that the correlation values are always larger than 0.7.



Figure 3: Standard deviations for some benchmarks as a function of the number of D. Rochman – 48 / 66



#### **Burn-up calculation: Overview**

- ➡ Method: Total Monte Carlo (TMC)
- Description of the SERPENT model (Fuel pin-cell)
- Considered data in TMC

Results



The complete report (NRG-113696) can be found at

ftp://ftp.nrg.eu/pub/www/talys/bib\_rochman/tmc.nrg.pdf

#### **Description of the SERPENT model (Fuel pin-cell)**



The fuel test is a typical fuel rod from TMI-1 PWR, 15x15 assembly design.

Hot Full Power conditions		Configuration	
Fuel temperature (K)	900	Unit cell pitch (mm)	14.427
Cladding temperature (K)	600	Fuel pellet diameter (mm)	9.391
Moderator (coolant) temperature (K)	562	Fuel pellet material	$UO_2$
Moderator (coolant) density $(g/cm^3)$	0.7484	Fuel density (g/cm <sup>3</sup> )	10.283
Reactor power (MWt)	2772	Fuel enrichment (w/o)	4.85
Number of assembly in reactor core	177	Cladding outside diameter (mm)	10.928
Number of fuel rods/fuel assembly	208	Cladding thickness (mm)	0.673
Active core length (mm)	3571.20	Cladding material	Zircaloy-4
		Cladding density (g/cm <sup>3</sup> )	6.55
		Gap material	He
		Moderator material	$H_2O$

The fuel sample is burned for a unique complete cycle and the lengths of the burn time and cooling time:

Operating cycle	1
Burn time (days)	1825
Final burnup (GWd/MTU)	61.28
Downtime (days)	1870
Specific power (kW/kgU)	33.58

#### **Considered data in TMC**

pellet dia	meter			2 %			
fuel enric	hment			3 %			
fuel der	nsity			4 %			
moderator	density			5 %			
Nuclear data	ENDF-6 name	<sup>235</sup> U	<sup>238</sup> U	<sup>237</sup> Np	<sup>239</sup> Pu	<sup>241</sup> Pu	Lumped fiss. prod.
complete ENDF file	MF1-6,10,12,14	Х	Х		Х		Х
fission yields	MF8	X	Х	Х	Х	Х	
v-bar	MF1	X	Х		Х		
Resonance range	MF2	X	Х		Х		
Fast range	MF3	X	Х		Х		
Angular distr.	MF4	X	Х		Х		
Fission neut. spec.	MF5	Х	Х		Х		
(n,γ)		X	Х		Х		
(n,f)		Х	Х		Х		
(n,el)		X	Х		Х		

Lumped (138) fission products:  $^{72-74,76}$ Ge,  $^{75}$ As,  $^{76-80,82}$ Se,  $^{79,81}$ Br,  $^{80-84,86}$ Kr,  $^{85,87}$ Rb,  $^{86-88,92}$ Sr,  $^{89}$ Y,  $^{93,95}$ Zr,  $^{94,95}$ Nb,  $^{95-97}$ Mo,  $^{99}$ Tc,  $^{99-104,106}$ Ru,  $^{103,105,106}$ Rh,  $^{104-108,110}$ Pd,  $^{109}$ Ag,  $^{111-114,116}$ Cd,  $^{113,115}$ In,  $^{115,117-119,126}$ Sn,  $^{121,123,125}$ Sb,  $^{122-128,130}$ Te,  $^{127,129,135}$ I,  $^{128,130-132,134-136}$ Xe,  $^{133-137}$ Cs,  $^{134-138}$ Ba,  $^{140}$ La,  $^{140,142}$ Ce,  $^{141,144}$ Pr,  $^{142-146,148,150}$ Nd,  $^{147-149}$ Pm,  $^{147,149-152,154}$ Sm,  $^{151-156}$ Eu,  $^{152,154-158,160}$ Gd,  $^{159,160}$ Tb,  $^{160-164}$ Dy,  $^{165}$ Ho,  $^{166,167}$ Er.



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#### Results on $k_\infty$





#### **Results on** $k_{\infty}$

<b>Results</b> on	$\mathbf{k}_{\infty}$						<b>\</b>
							-NRG
			В	urn-up (GWd/M	ITU)		
	0	10	20	30	40	50	60
k∞	1.41e+00	1.25e+00	1.16e+00	1.08e+00	1.02e+00	9.55e-01	9.01e-01
Order							
1.	<sup>235</sup> U	<sup>238</sup> U	<sup>238</sup> U	<sup>238</sup> U	<sup>238</sup> U	<sup>239</sup> Pu	<sup>239</sup> Pu
2.	<sup>238</sup> U	<sup>235</sup> U	<sup>235</sup> U	<sup>235</sup> U	<sup>235</sup> U	Fiss. Yields	Fiss. Yields
3.		Fiss. Prod.	Fiss. Prod.	<sup>239</sup> Pu	<sup>239</sup> Pu	<sup>238</sup> U	<sup>238</sup> U
4.		<sup>239</sup> Pu	<sup>239</sup> Pu	Fiss. Prod.	Fiss. Yields	Fiss. Prod.	Fiss. Prod.
5.		Fiss. Yields	Fiss. Yields	Fiss. Yields	Fiss. Prod.	<sup>235</sup> U	<sup>235</sup> U
			Uncertainties (in	n %) coming fro	om		
<sup>235</sup> U	0.50	0.43	0.39	0.35	0.32	0.28	0.24
<sup>238</sup> U	0.46	0.47	0.44	0.40	0.35	0.33	0.36
<sup>239</sup> Pu	0.05	0.15	0.26	0.33	0.39	0.44	0.47
Fiss. Yiel.	0.00	0.21	0.25	0.29	0.32	0.35	0.36
Lumped F.P.	0.00	0.37	0.36	0.31	0.31	0.29	0.28
Total	0.68	0.79	0.78	0.76	0.76	0.76	0.79

#### **Results on reaction rates**

			Burn	u-up (GWd/M7	ΓU)		
	0	10	20	30	40	50	60
rr $^{235}$ U(n, $\gamma$ )	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	$^{235}$ U(n, $\gamma$ )	$^{235}$ U(n, $\gamma$ )
rr $^{238}$ U(n, $\gamma$ )	<sup>238</sup> U(n,el)	$^{238}$ U(n, $\gamma$ )	$^{238}$ U(n, $\gamma$ )	<sup>238</sup> U(n, γ)	<sup>238</sup> U(n, γ)	$^{238}$ U(n, $\gamma$ )	$^{238}$ U(n, $\gamma$ )
rr <sup>239</sup> Pu(n, $\gamma$ )	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	$^{238}$ U(n, $\gamma$ )	$^{235}$ U(n, $\gamma$ )	$^{238}$ U(n, $\gamma$ )
rr <sup>240</sup> Pu(n, $\gamma$ )	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>238</sup> U(n, γ)	$^{238}$ U(n, $\gamma$ )	$^{238}$ U(n, $\gamma$ )	$^{238}$ U(n, $\gamma$ )
rr <sup>241</sup> Pu(n, $\gamma$ )	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>238</sup> U(n,γ)	$^{238}$ U(n, $\gamma$ )	$^{238}$ U(n, $\gamma$ )
rr <sup>235</sup> U(n,f)	<sup>235</sup> U MF5	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U MF5	<sup>238</sup> U(n,γ)	<sup>238</sup> U(n,γ)	<sup>238</sup> U(n,γ)
rr <sup>238</sup> U(n,f)	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>239</sup> Pu MF5
rr <sup>239</sup> Pu(n,f)	<sup>239</sup> Pu(n,el)	<sup>239</sup> Pu(n,el)	<sup>239</sup> Pu(n,el)	<sup>239</sup> Pu(n,f)	<sup>239</sup> Pu(n,f)	<sup>239</sup> Pu(n,f)	<sup>239</sup> Pu(n,f)
rr <sup>240</sup> Pu(n,f)	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>239</sup> Pu MF5
rr <sup>241</sup> Pu(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>238</sup> U(n,γ)	<sup>238</sup> U(n,γ)	<sup>238</sup> U(n,γ)
	Total	uncertainties (d	ue to transport	data and fissio	on yields, in %	) for	
rr $^{235}$ U(n, $\gamma$ )	2.05	2.04	2.07	2.14	2.31	2.54	2.79
rr <sup>238</sup> U(n,γ)	1.75	1.74	1.69	1.65	1.55	1.37	1.25
rr <sup>239</sup> Pu(n,γ)	1.22	1.12	1.09	1.13	1.36	1.68	2.05
rr <sup>240</sup> Pu(n, $\gamma$ )	0.64	0.98	0.64	0.72	0.96	1.27	1.61
rr <sup>241</sup> Pu(n, $\gamma$ )	1.35	1.20	1.16	1.17	1.38	1.69	2.09
rr <sup>235</sup> U(n,f)	0.52	0.56	0.69	0.87	1.21	1.61	2.07
rr <sup>238</sup> U(n,f)	6.61	5.91	5.29	4.84	4.31	3.91	3.70
rr <sup>239</sup> Pu(n,f)	1.99	1.84	1.77	1.77	1.92	2.17	2.53
rr <sup>240</sup> Pu(n,f)	2.68	2.45	2.27	2.18	2.14	2.22	2.49
rr $^{241}$ Pu(n,f)	1.34	1.21	1.15	1.17	1.36	1.67	2.06



#### **Results on macroscopic cross sections**

esults	on macro	oscopic cr	oss sectio	ons			— N	RC
			Βι	urn-up (GWd/N	ITU)			
	0	10	20	30	40	50	60	
$\Sigma_{abs1}$	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>239</sup> Pu MF1	<sup>239</sup> Pu MF1	$^{238}$ U(n, $\gamma$ )	$^{238}$ U(n, $\gamma$ )	
$\Sigma_{abs2}$	<sup>235</sup> U(n,el)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	$^{235}$ U(n, $\gamma$ )	<sup>238</sup> U(n,γ)	$^{238}$ U(n, $\gamma$ )	$^{238}$ U(n, $\gamma$ )	
$\Sigma_{\rm fiss1}$	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>239</sup> Pu MF5	<sup>239</sup> Pu MF5	
$\Sigma_{\rm fiss2}$	<sup>235</sup> U(n,el)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>238</sup> U(n, γ)	<sup>238</sup> U(n,γ)	$^{238}$ U(n, $\gamma$ )	
$\nu \Sigma_{\rm fiss1}$	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	$^{238}$ U v-bar	<sup>238</sup> U MF1	<sup>238</sup> U MF1	
$\nu \Sigma_{\rm fiss2}$	<sup>235</sup> U(n,el)	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	<sup>238</sup> U MF1	<sup>238</sup> U(n,γ)	<sup>238</sup> U(n,γ)	<sup>238</sup> U(n,γ)	
D <sub>iff1</sub>	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>239</sup> Pu MF5	<sup>239</sup> Pu MF5	
D <sub>iff2</sub>	<sup>238</sup> U MF4	F. P.	F. P.	F. P.	F. P.	<sup>235</sup> U MF5	<sup>239</sup> Pu MF5	
	To	otal uncertainti	es (due to tran	sport data and	fission yields, in	n %) for		-
$\Sigma_{abs1}$	1.08	1.11	1.09	1.04	1.07	1.06	1.08	-
$\Sigma_{abs2}$	1.12	1.06	1.13	1.28	1.50	1.74	2.00	
$\Sigma_{\rm fiss1}$	1.71	1.75	1.74	1.73	1.76	1.83	2.00	
$\Sigma_{\rm fiss2}$	1.63	1.44	1.40	1.52	1.73	2.03	2.36	
$\nu \Sigma_{\rm fiss1}$	1.98	2.01	2.02	2.07	2.15	2.28	2.46	
$\nu \Sigma_{\rm fiss2}$	1.63	1.40	1.39	1.51	1.74	2.03	2.37	
D <sub>iff1</sub>	1.88	1.49	1.32	1.19	1.10	1.06	1.01	
D <sub>iff2</sub>	1.22	1.63	1.62	1.62	1.56	1.56	1.56	

#### **Results on number densities for actinides**

			Burn-ı	ıp (GWd/MTU	J)		Cooling ti	me (years)
	0	20	30	40	50	60	0	300
<sup>4</sup> U	-	<sup>235</sup> U(n,f)	$^{235}$ U(n, $\gamma$ )					
<sup>5</sup> U	-	<sup>235</sup> U(n,f)	<sup>235</sup> U(n,f)	$^{238}$ U(n, $\gamma$ )	$^{238}$ U(n, $\gamma$ )	$^{238}$ U(n, $\gamma$ )	<sup>238</sup> U(n,γ)	$^{238}$ U(n, $\gamma$ )
<sup>6</sup> U	-	$^{235}$ U(n, $\gamma$ )	$^{235}U(n,\gamma)$	$^{235}U(n,\gamma)$	$^{235}$ U(n, $\gamma$ )			
<sup>8</sup> U	-	$^{238}U(n,\gamma)$	$^{238}$ U(n, $\gamma$ )					
<sup>7</sup> Np	-	<sup>235</sup> U MF5	$^{235}U(n,\gamma)$	$^{235}$ U(n, $\gamma$ )				
<sup>8</sup> Pu	-	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>235</sup> U MF5	<sup>235</sup> U MF5	$^{235}$ U(n, $\gamma$ )	$^{235}$ U(n, $\gamma$ )	$^{235}$ U(n, $\gamma$ )
<sup>9</sup> Pu	-	<sup>238</sup> U(n,γ)	$^{238}$ U(n, $\gamma$ )	<sup>238</sup> U(n,γ)	<sup>238</sup> U(n,γ)	$^{238}$ U(n, $\gamma$ )	$^{238}$ U(n, $\gamma$ )	$^{238}$ U(n, $\gamma$ )
<sup>0</sup> Pu	-	<sup>235</sup> U(n,f)	$^{239}$ Pu(n,f)	$^{239}$ Pu(n,f)	$^{239}$ Pu(n,f)	$^{239}$ Pu(n,f)	<sup>239</sup> Pu(n,f)	<sup>239</sup> Pu(n,f)
<sup>1</sup> Pu	-	$^{235}$ U(n,f)	<sup>235</sup> U(n,f)	$^{239}$ Pu(n,f)	$^{239}$ Pu(n,f)	<sup>238</sup> U(n,γ)	$^{238}$ U(n, $\gamma$ )	<sup>239</sup> Pu(n,f)
<sup>1</sup> Am	-	<sup>235</sup> U(n,f)	<sup>238</sup> U(n,γ)					
		Total u	incertainties (d	lue to transpor	t data and fissi	on yields, in %	b) for	
<sup>4</sup> U	-	0.12	0.41	0.55	0.69	0.93	0.97	1.90
<sup>5</sup> U	-	0.17	0.72	1.21	1.88	2.79	2.93	2.92
<sup>6</sup> U	-	1.98	1.96	1.95	1.93	1.91	1.90	1.88
<sup>8</sup> U	-	0.01	0.02	0.03	0.04	0.04	0.04	0.04
<sup>7</sup> Np	-	9.50	4.13	3.39	2.98	2.74	2.72	1.83
<sup>8</sup> Pu	-	12.1	4.98	3.83	3.16	2.74	2.71	2.53
<sup>9</sup> Pu	-	1.78	2.30	2.60	2.91	3.22	3.26	3.22
<sup>0</sup> Pu	-	1.93	1.95	2.05	2.22	2.41	2.43	2.34
<sup>1</sup> Pu	-	2.04	1.52	1.62	1.88	2.19	2.23	2.47
1 1 m		2 1 1	1.63	1 90	2 44	3 14	3 24	2.26

#### **Results on number densities for fission products**

							~ ~ ~	
			Burn-ı	up (GWd/MTU	J)		Cooling ti	me (years)
	0	10	30	40	50	60	0	300
Tc	-	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.
<sup>33</sup> Cs	-	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.
<sup>40</sup> Ce	-	<sup>235</sup> U F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.
<sup>13</sup> Nd	-	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.
<sup>47</sup> Sm	-	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	F.P.	F.P.	F.P.	F.P.	F.P.
<sup>49</sup> Sm	-	<sup>235</sup> U F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.
<sup>51</sup> Sm	-	<sup>235</sup> U F.Y.	F.P.	F.P.	F.P.	F.P.	F.P.	F.P.
<sup>54</sup> Sm	-	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.	<sup>239</sup> Pu F.Y.
<sup>53</sup> Eu	-	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	F.P.	F.P.	F.P.
<sup>55</sup> Gd	-	F.P.	F.P.	F.P.	F.P.	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.	<sup>235</sup> U F.Y.
		Total ı	uncertainties (	due to transpor	rt data and fiss	ion yields, in <sup>o</sup>	%) for	
Tc	-	10.4	9.41	9.19	9.10	9.11	9.12	9.12
<sup>3</sup> Cs	-	3.50	3.74	4.16	4.72	5.39	5.47	5.45
<sup>40</sup> Ce	-	2.55	2.78	2.95	3.14	3.34	3.37	3.38
<sup>43</sup> Nd	-	4.35	4.93	5.42	5.98	6.59	6.67	6.65
<sup>47</sup> Sm	-	11.4	20.6	25.0	28.7	31.7	32.0	23.8
<sup>49</sup> Sm	-	11.4	10.8	10.7	11.0	11.3	11.4	10.9
<sup>51</sup> Sm	-	26.6	22.5	21.5	20.9	20.5	20.5	20.1
<sup>54</sup> Sm	-	26.2	20.6	19.4	18.6	18.1	18.1	18.1
<sup>3</sup> Eu	-	13.8	12.1	12.5	12.9	13.3	13.4	13.3
<sup>5</sup> Gd	-	27.0	22.4	22.4	22.5	22.8	23.0	11.0

#### Example for $k_{\infty}$



#### **Example for reaction rates**



#### **Example for macroscopic cross sections**



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#### **Example for number densities**



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#### **Example for number densities**



#### **Discussion/conclusion**



#### **Discussion/conclusion**



#### **Discussion/conclusion**

