

# Nuclear data uncertainty propagation with Monte Carlo methods

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A. Koning, S.C. van der Marck and D.F. daCruz

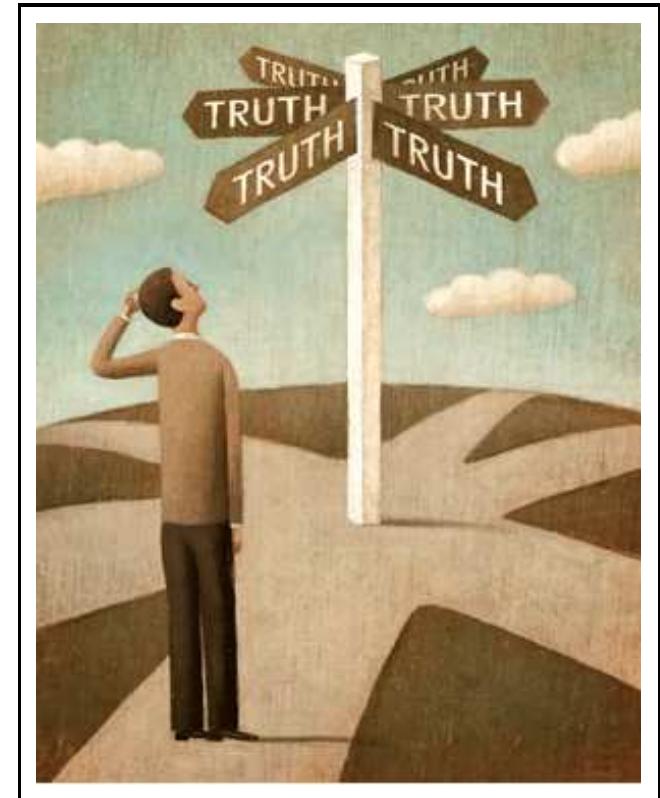
*Nuclear Research and Consultancy Group,*

*NRG, Petten, The Netherlands*

GRS Garching, July 2013

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- ① General information
- ② Uncertainty propagation: the TMC method
- ③ Examples
- ④ fast TMC and fast GRS methods
- ⑤ Full core example
- ⑥ Conclusions



All slides can be found at:

[ftp://ftp.nrg.eu/pub/www/talys/bib\\_rochman/presentation.html](ftp://ftp.nrg.eu/pub/www/talys/bib_rochman/presentation.html).

# Who are we ?



- ☞ NRG: a leading nuclear sector service provider
- ☞ Over 50 years experience in nuclear technology
- ☞ Over 400 employees (10 in R&D reactor physics and simulations)
- ☞ Turnover approximately Meuros 60 / per year
- ☞ High Flux Reactor, Hot Cell Laboratories and Radiological labs

## Health - Medical Isotopes world-wide



# What are nuclear data ?



The term "nuclear data" can have different meaning,

- ▶ dusty books, constants, mature field, code inputs,
- ▶ list, Schrodinger equation, unexciting...
- ▶ but this is not ! (I'm going to prove that)

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## U.S. News

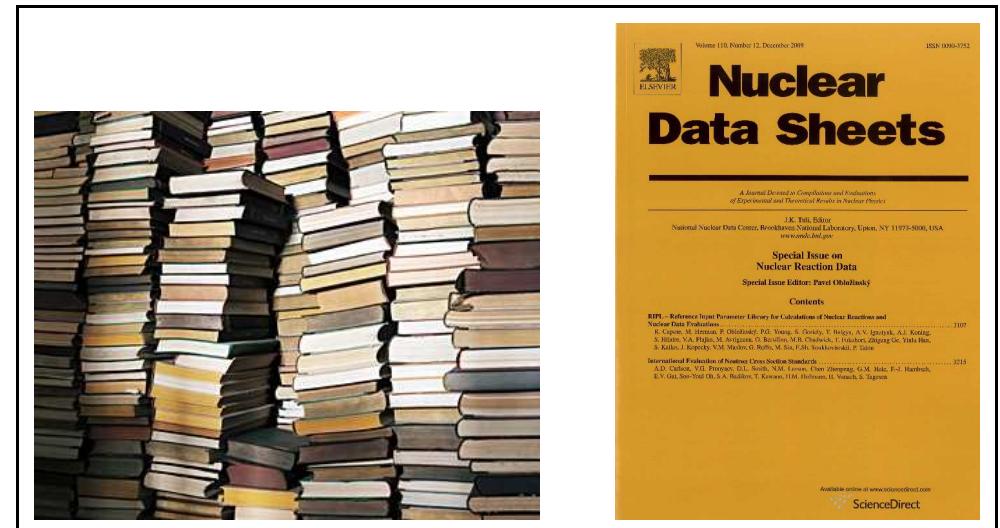
### U.S., Russia exchange nuclear data

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President Dimitri Medvedev (L) of Russia and U.S. President Barack Obama hold a bilateral meeting at the United Nations in New York on September 23, 2009. UPI/Olivier Douliery/Pool

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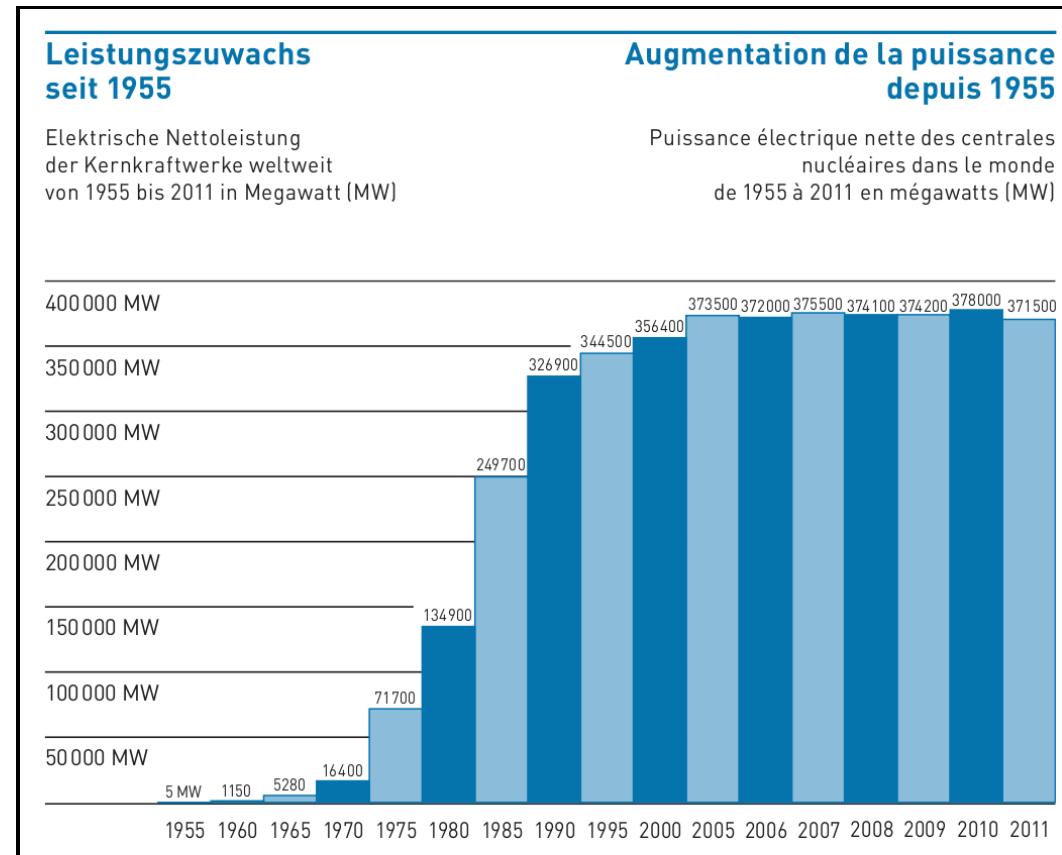
# Why are nuclear data important ? (Part 1)

Better nuclear data can help for:

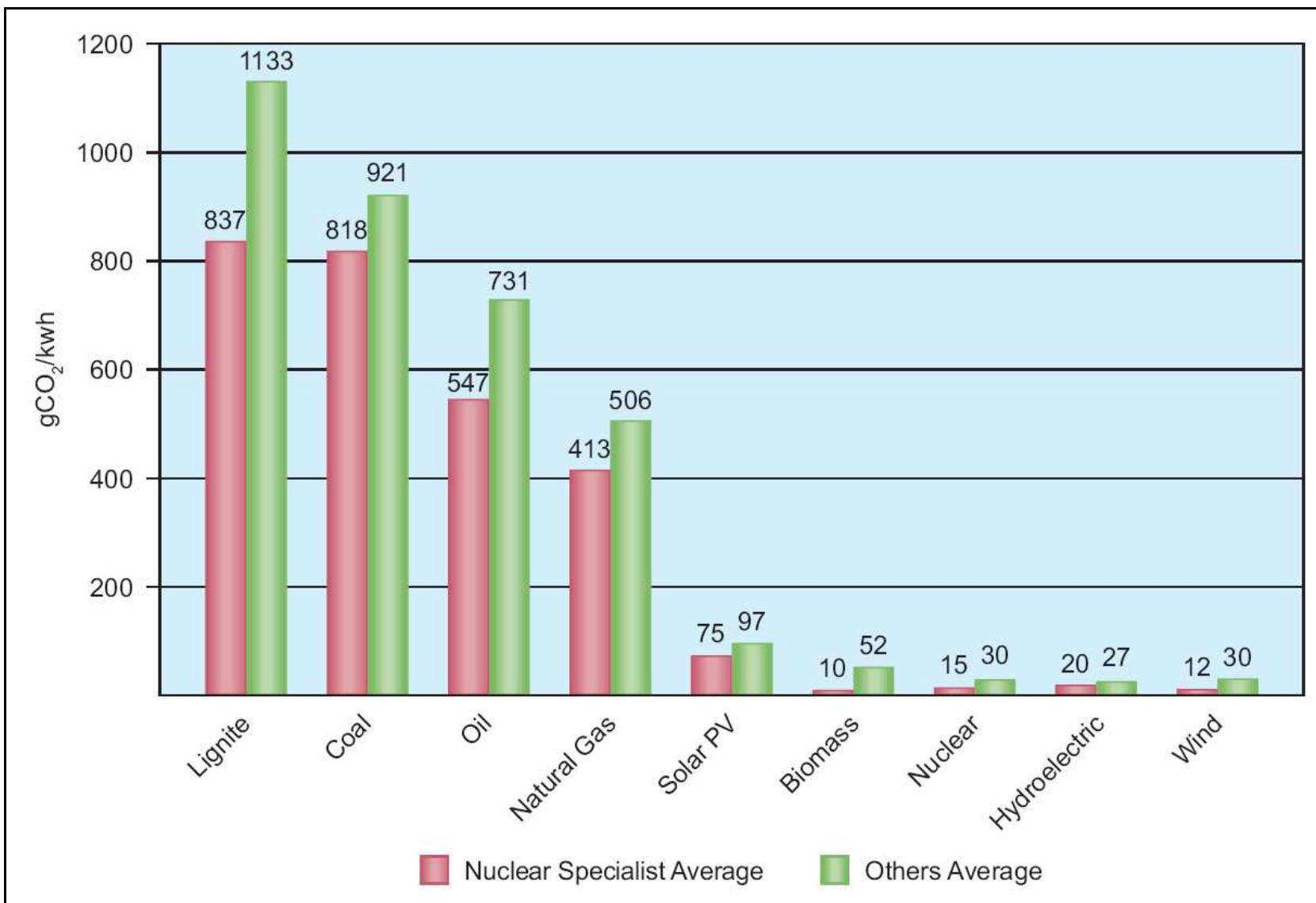
- ▶ safety margins, fuel storage,
- ▶ life-time extension,
- ▶ cost reduction in design of new systems,
- ▶ isotope production,
- ▶ safety of people (shielding),
- ▶ waste transmutation,
- ▶ development of future systems.

Better nuclear data have a limited effect on:

- ◀ current reactor operation,
- ◀ current reactor safety,...
- ◀ accident simulation,
- ◀ proliferation,
- ◀ Chernobyl, TMI, Fukushima.



# Why are nuclear data important ? (Part 2)



Source: [World Nuclear Association Report](#)

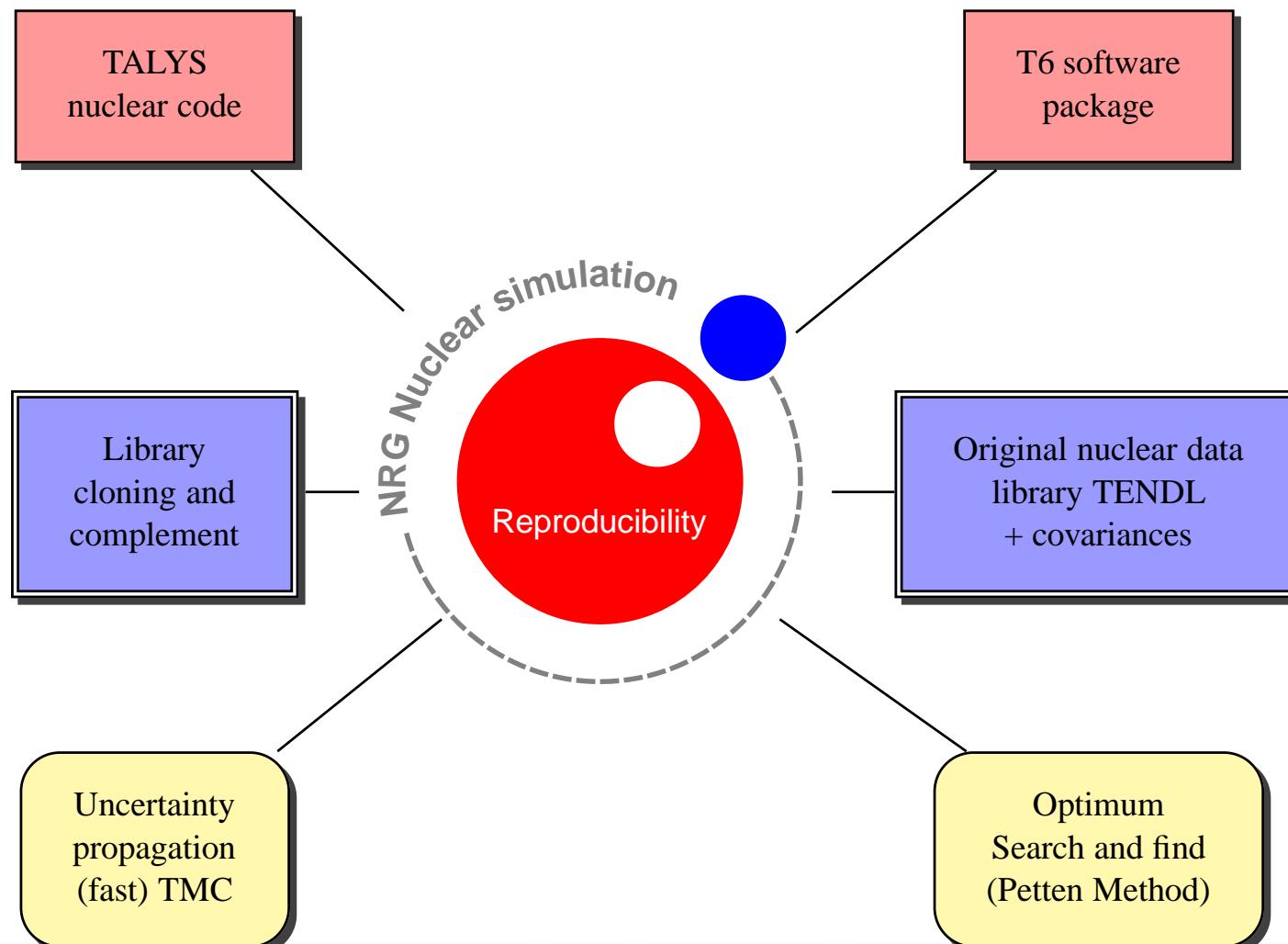
# Nuclear data uncertainties: general comments



- I    uncertainties are not errors (and vice versa),
- II    they are related to risks, quality of work, money, perception, fear, safety...
- III                 **Uncertainty  $\Leftarrow$  safety  $\Leftarrow$  professionalism**
- IV    True uncertainties do not exist ! They are the reflection of our knowledge and methods.
- V    All the above for covariances
- VI    The importance of nuclear data uncertainties should be checked. If believed

Our motivation:  
Any justification for not providing uncertainties  
should become obsolete

## Our mission: improve nuclear simulations



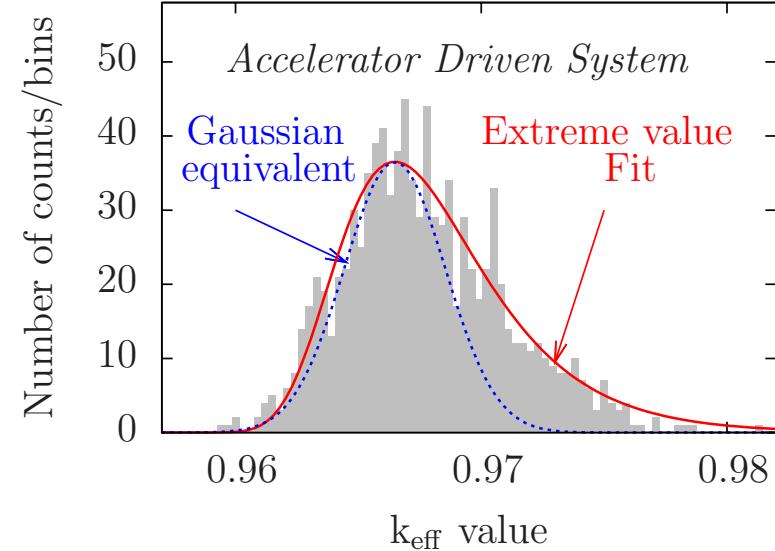
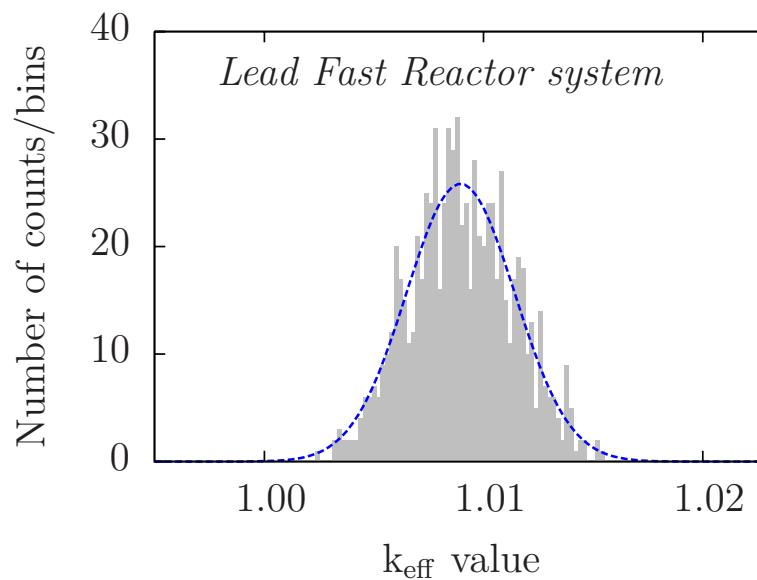
# 2008: Total Monte Carlo (TMC)

Control of nuclear data (TALYS system)  
+ processing (NJOY)  
+ system simulation (MCNP/ERANOS/CASMO...)

1000  
times

$$\sigma_{\text{total}}^2 = \sigma_{\text{statistics}}^2 + \sigma_{\text{nuclear data}}^2$$

For each random ENDF file, the benchmark calculation is performed with MCNP. At the end of the  $n$  calculations,  $n$  different  $k_{\text{eff}}$  values are obtained.



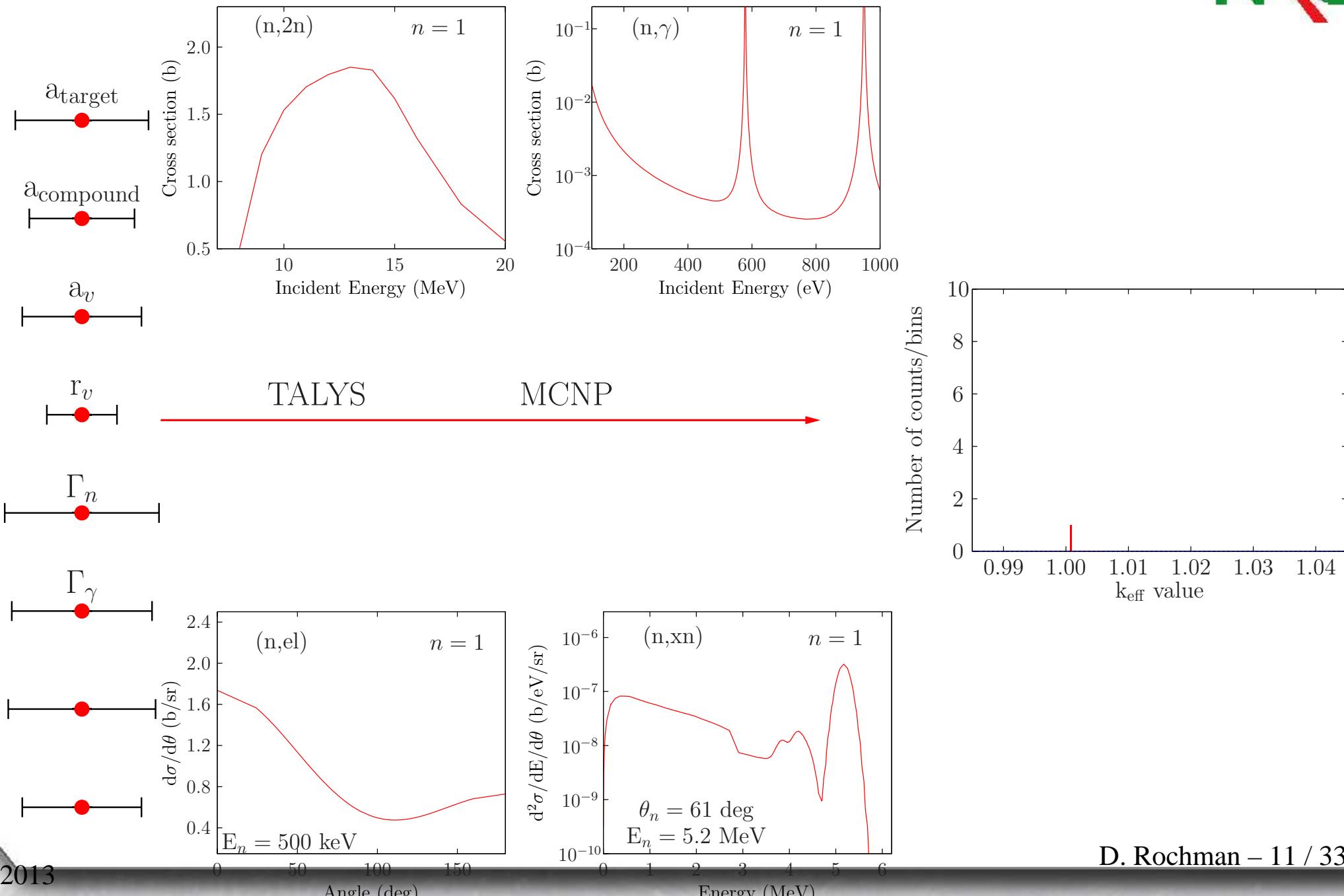
"Towards sustainable nuclear energy: Putting nuclear physics to work",

# TMC for nuclear data uncertainty propagation, what else ?

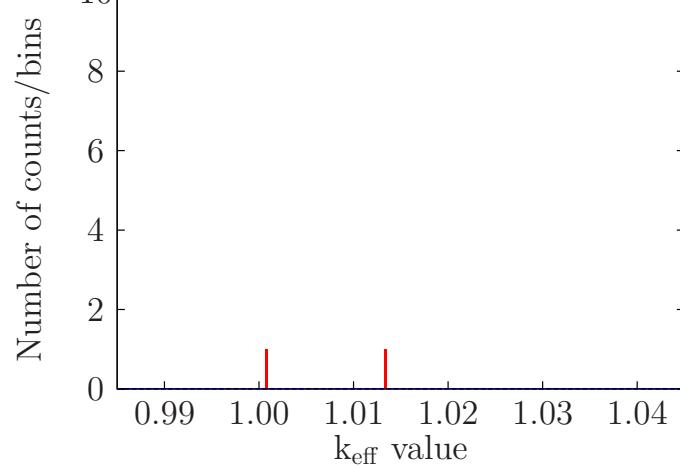
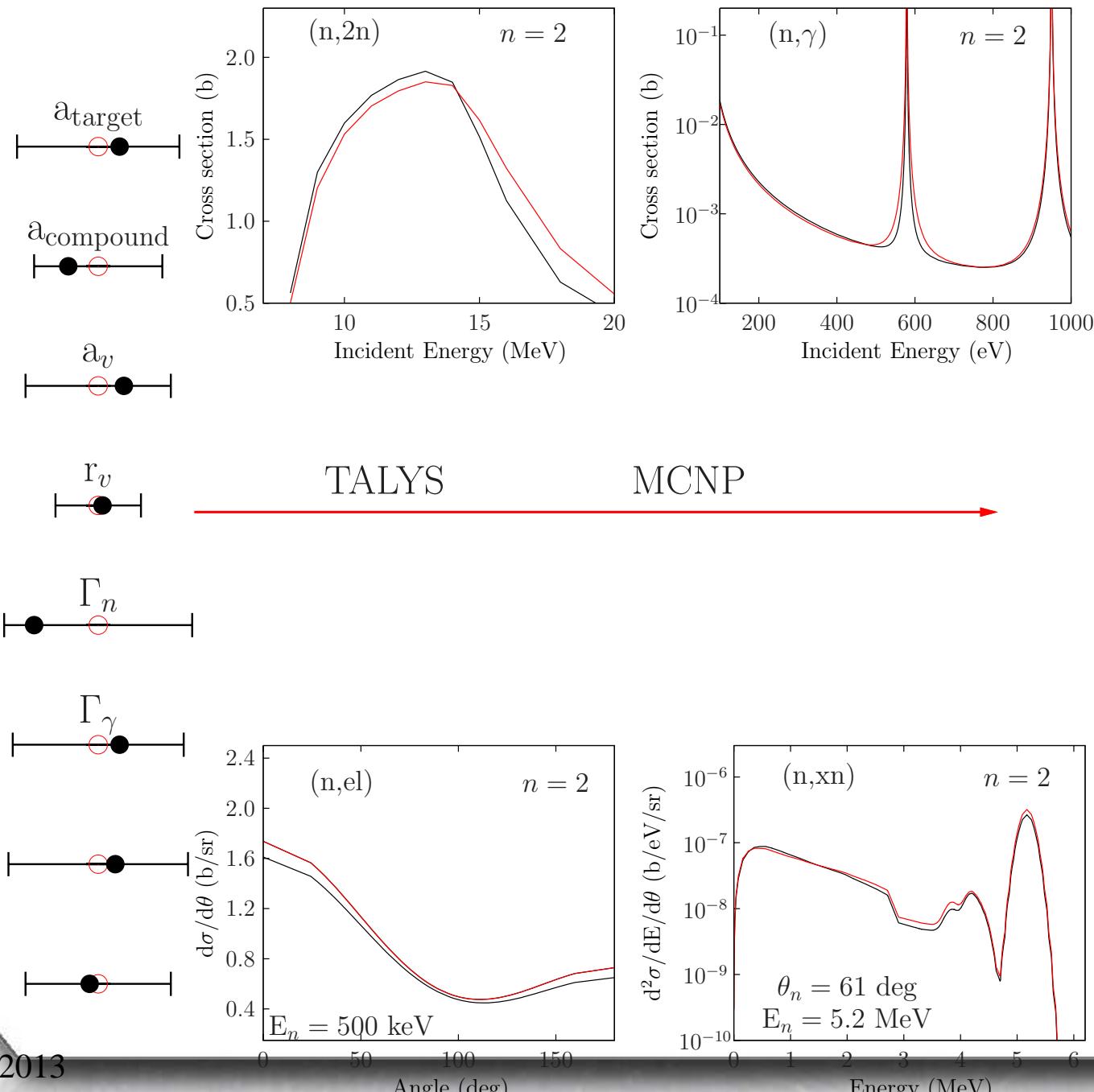


- 😊 + No covariance matrices (no 2 Gb files) **but** every possible cross correlation included,
- 😊 + No approximation **but** true probability distribution,
- 😊 + Only essential info for an evaluation is stored,
- 😊 + No perturbation code necessary, **only** “essential” codes,
- 😊 + Feedback to model parameters,
- 😊 + Full reactor core calculation and transient,
- 😊 + Also applicable to fission yields, thermal scattering, pseudo-fission products, all isotopes (...**just everything**),
- 😊 + Other variants: AREVA (NUDUNA), GRS (XSUSA), CIEMAT (ACAB), PSI (NUSS), CNRS Grenoble..., based on covariance files,
- 😊 + Many spin-offs (TENDL covariances, sensitivity, adjustment...)
- 😊 + Computer time (not human time)
- 😊 + QA.
- 😢 - Needs discipline to reproduce,
- 😢 - Memory and computer time (not human time),
- 😢 - Need mentality change.

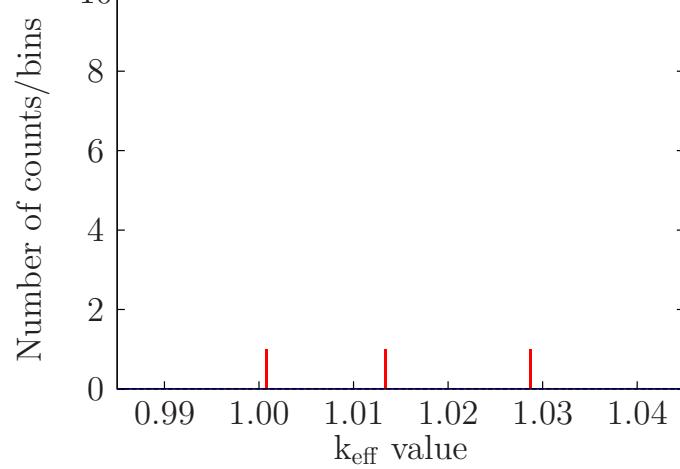
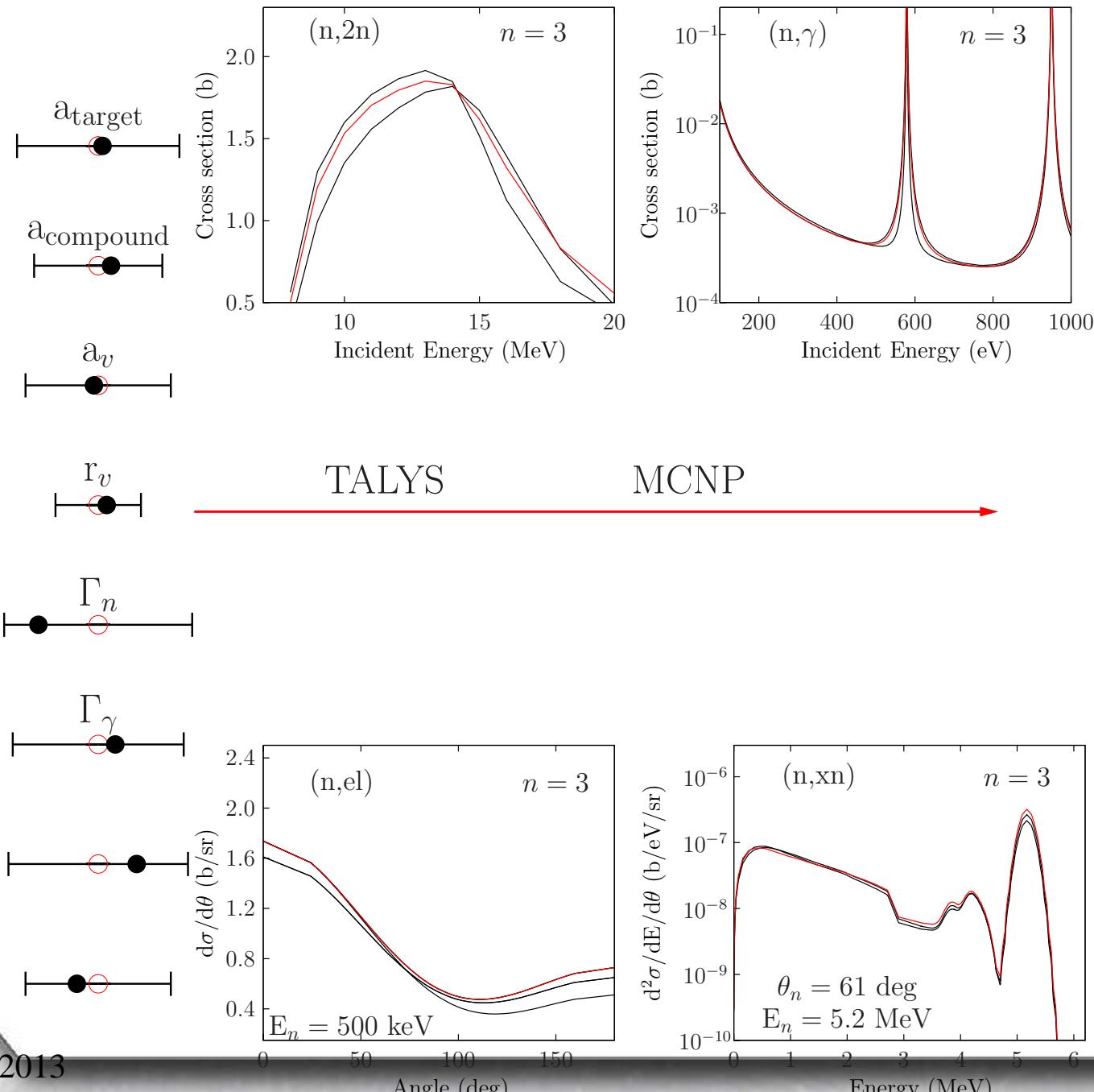
# Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



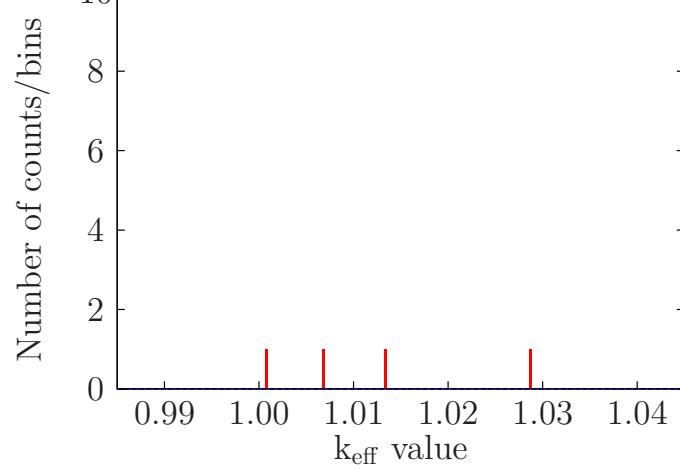
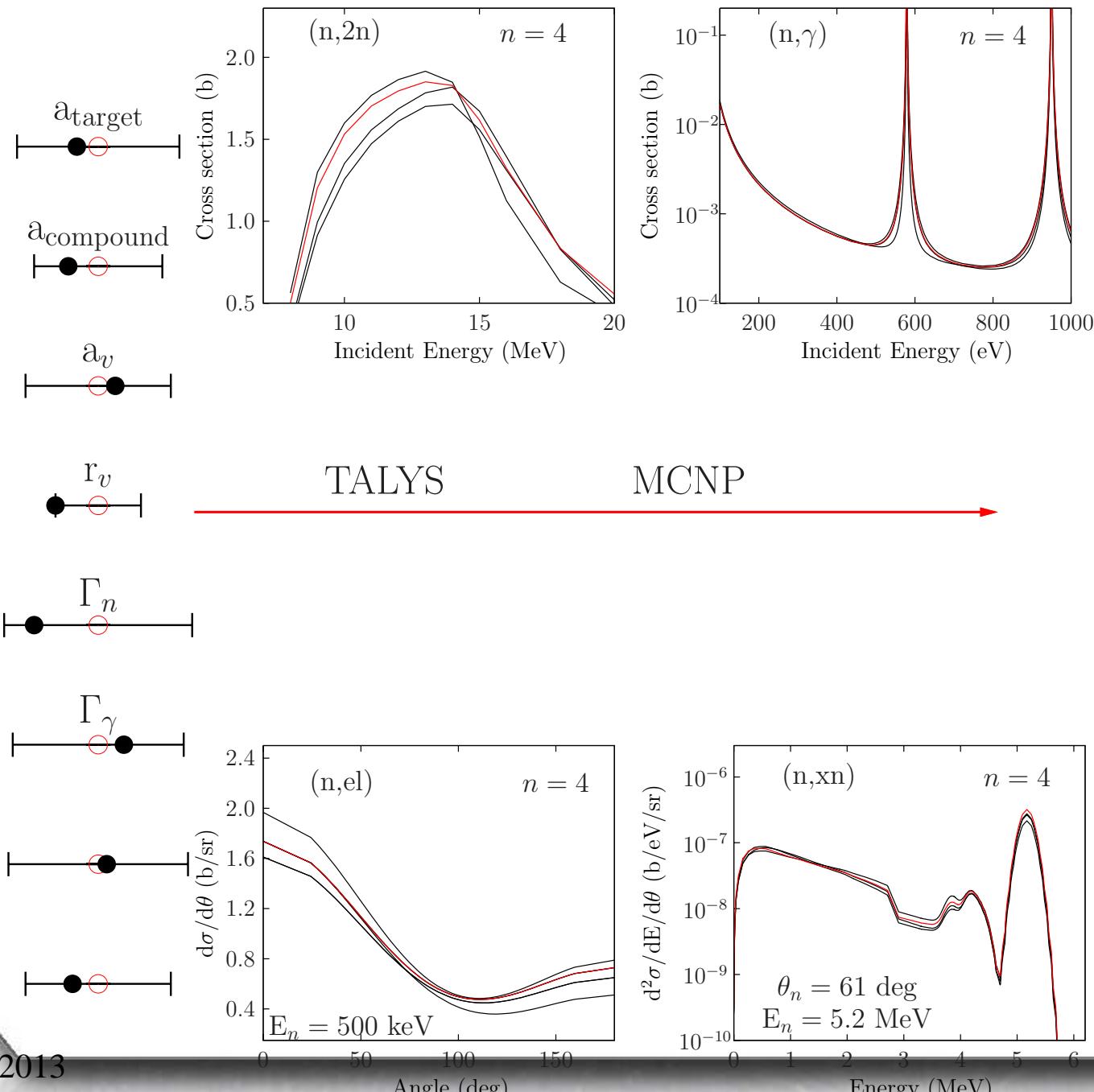
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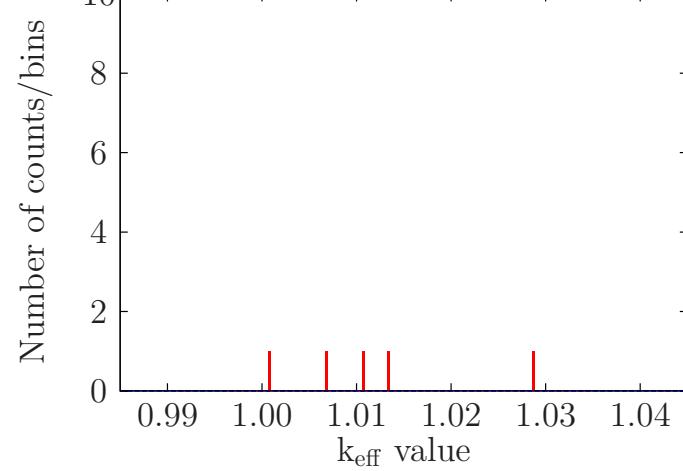
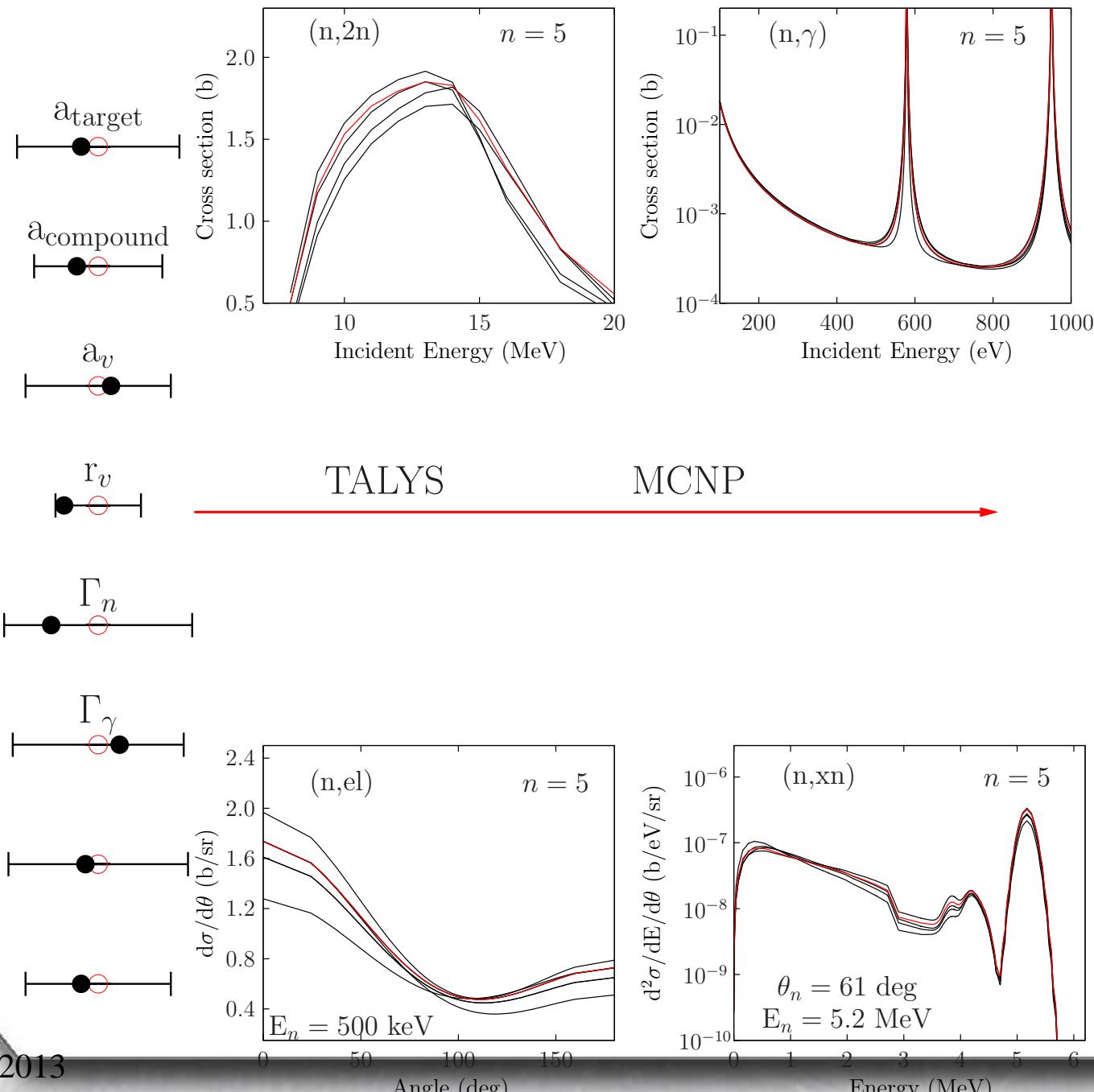
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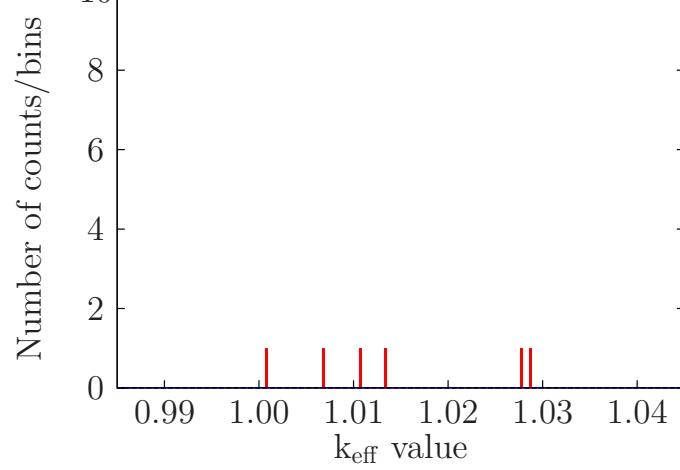
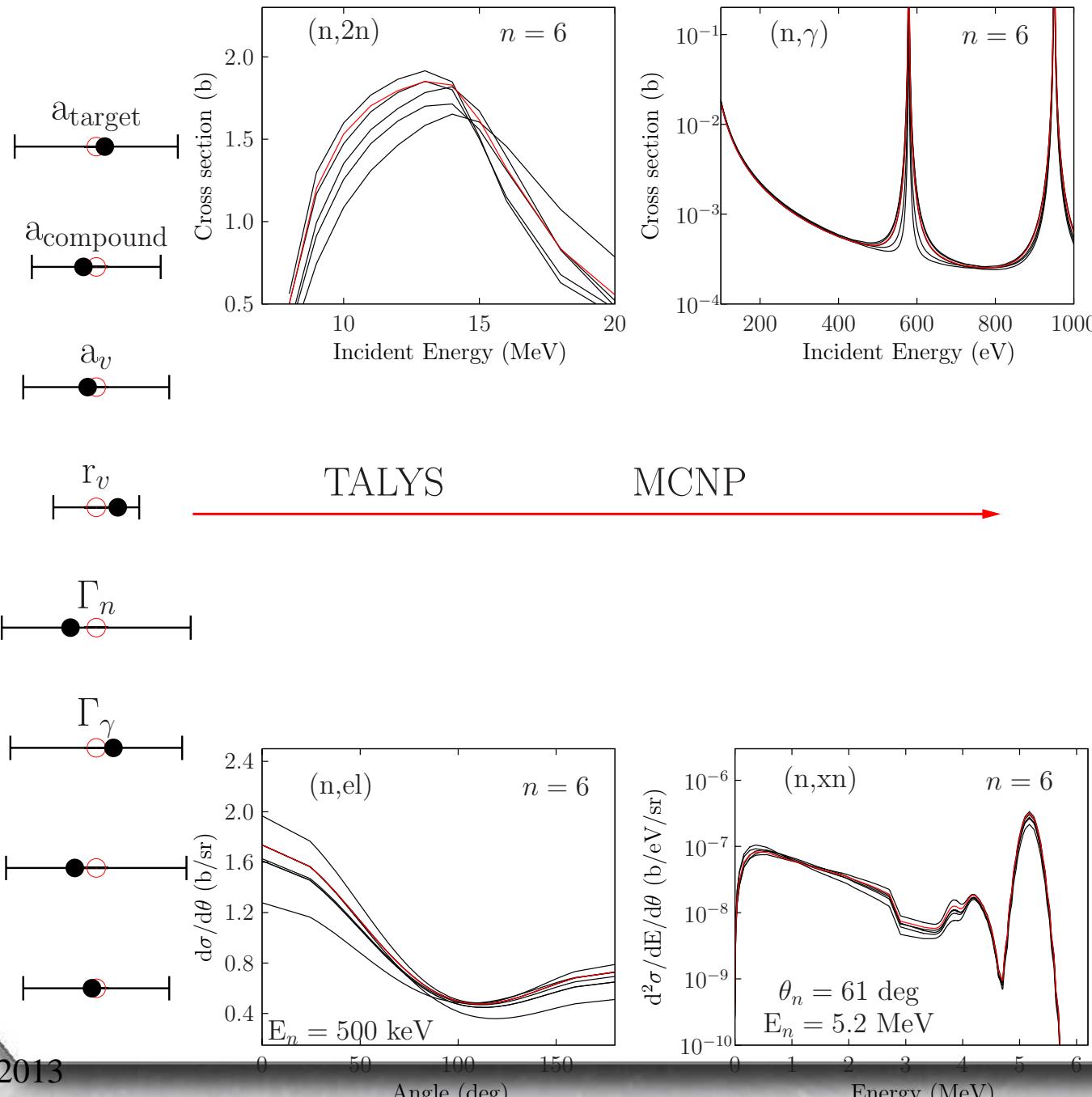
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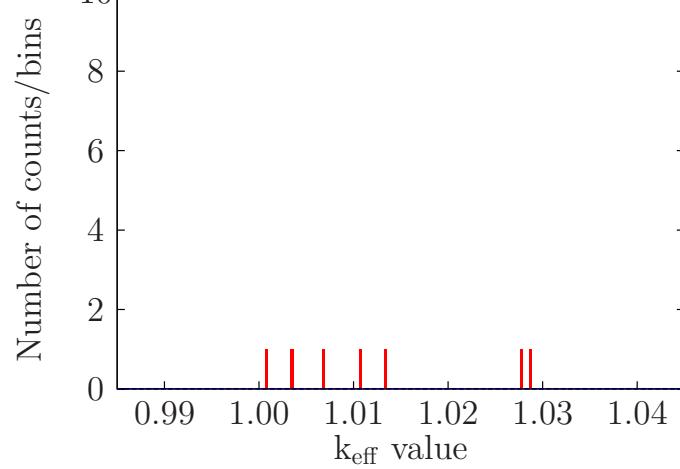
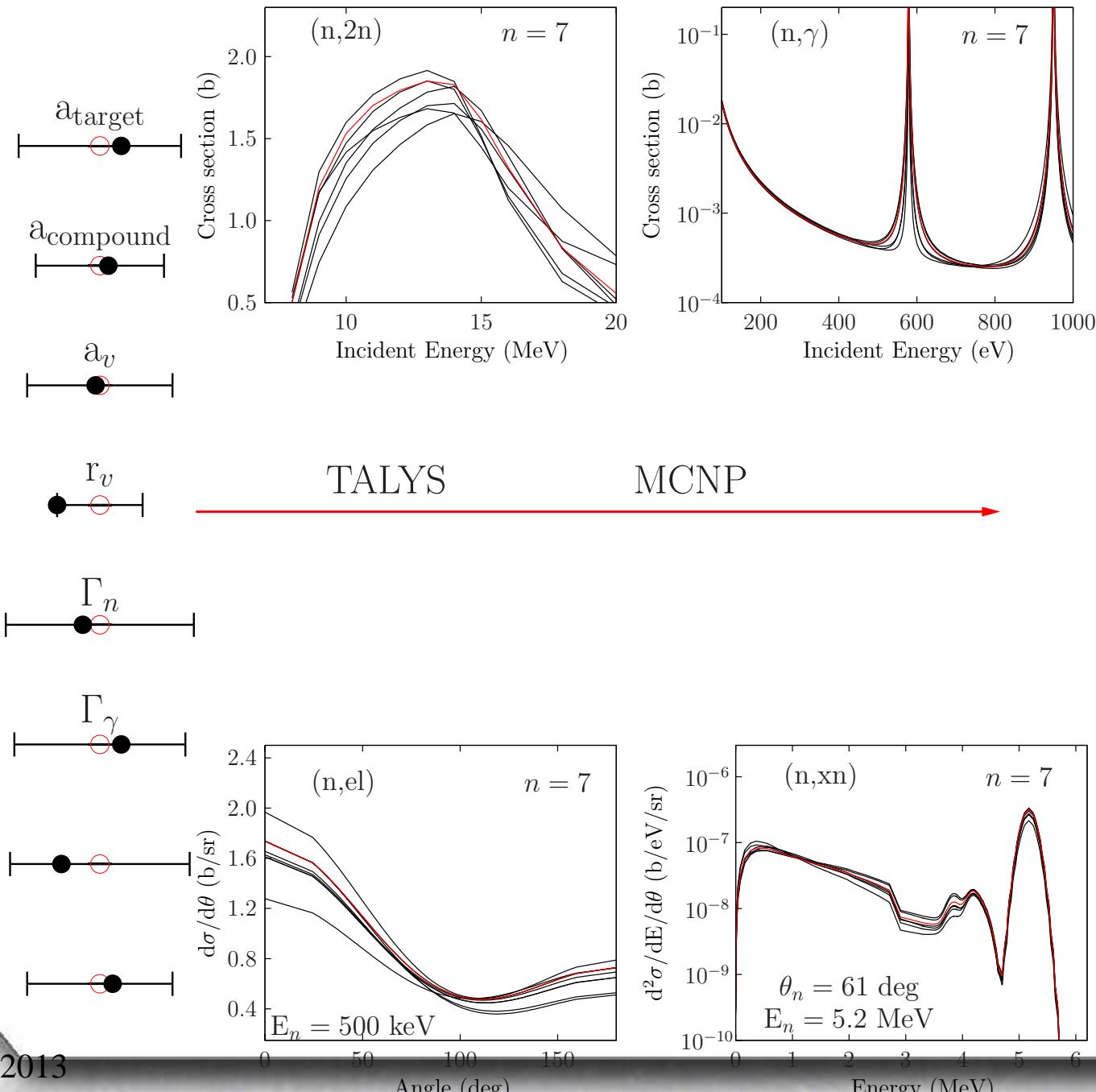
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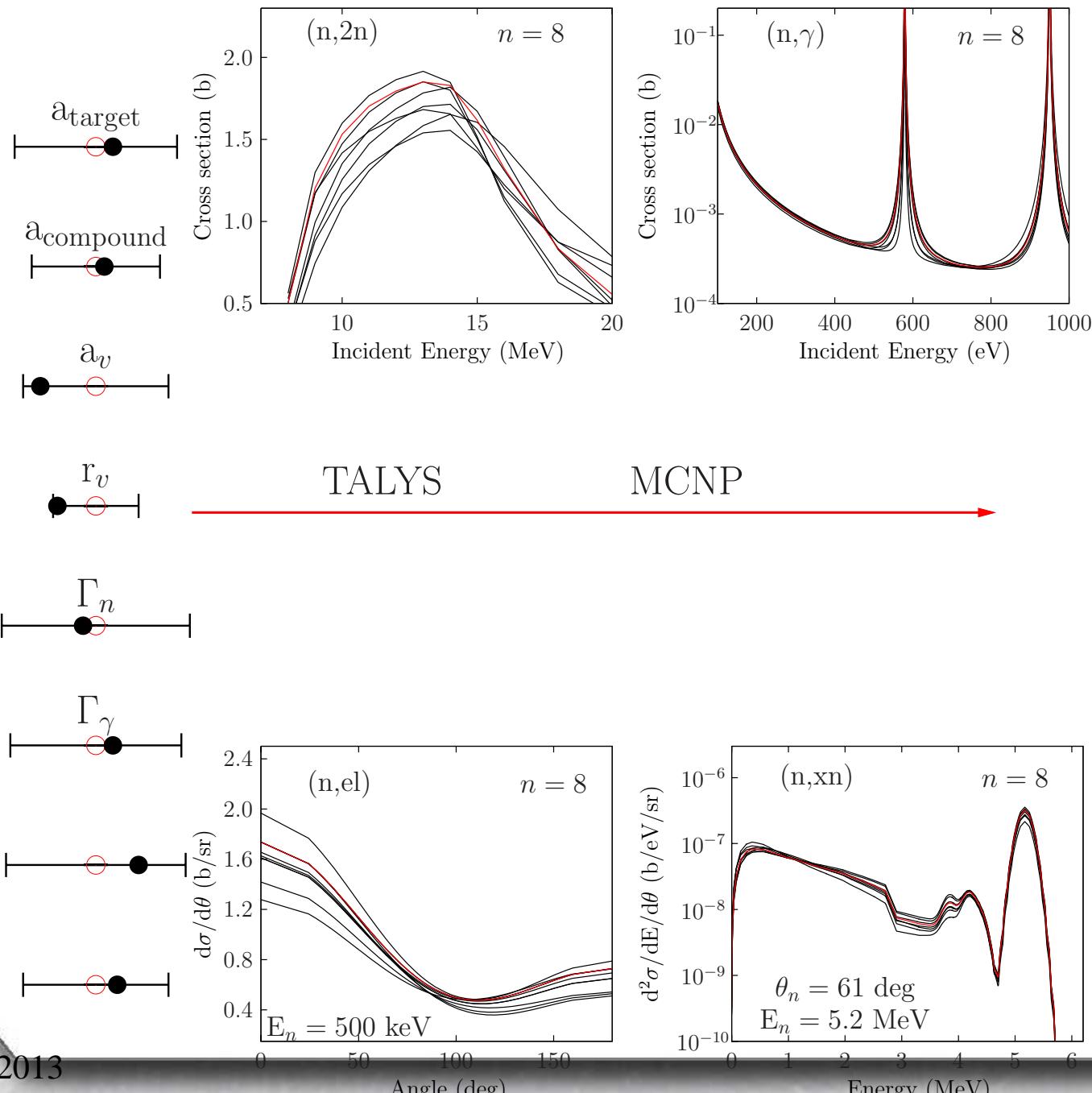
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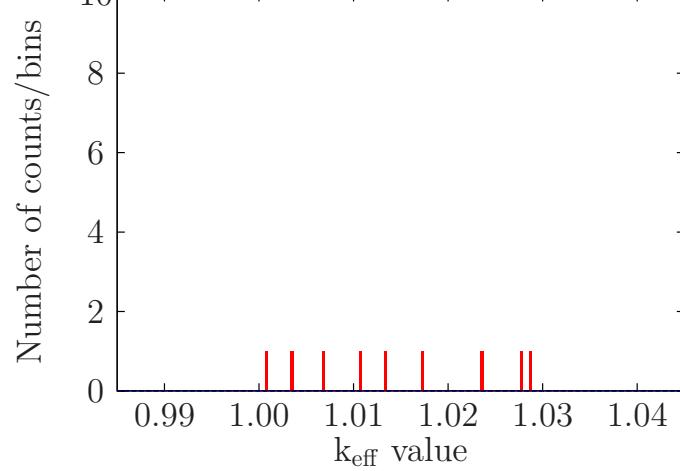
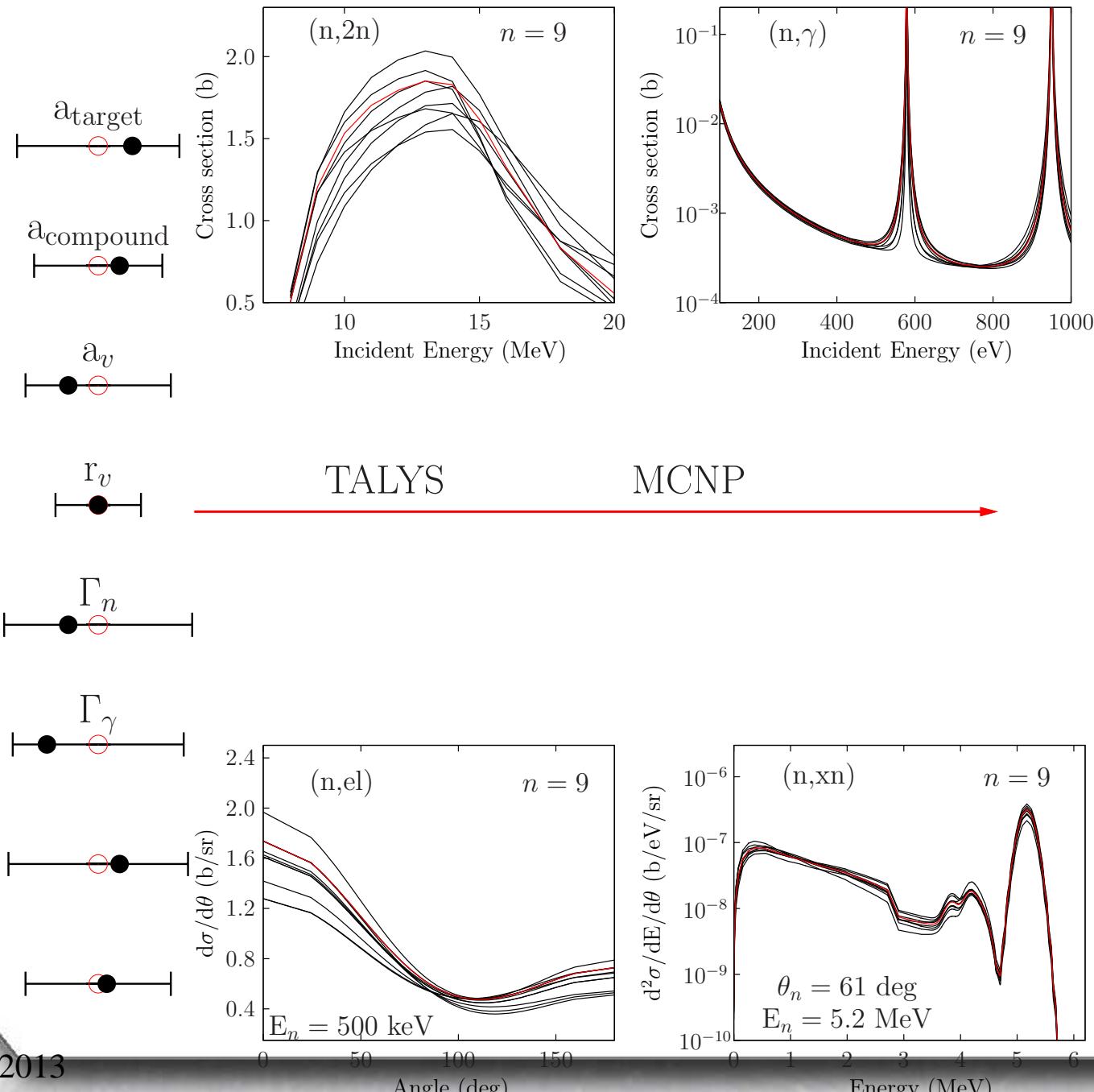
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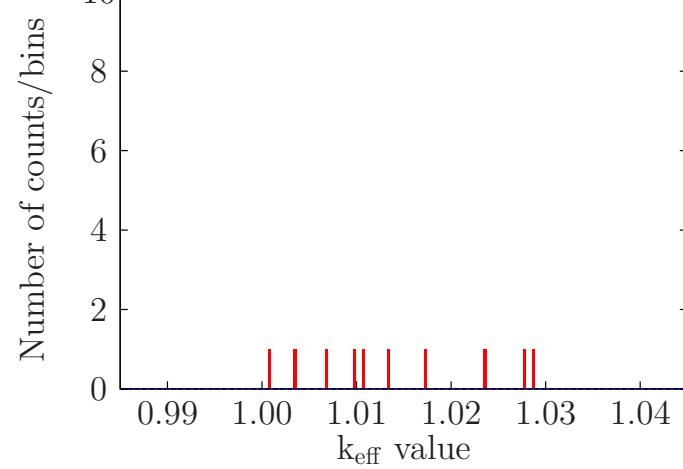
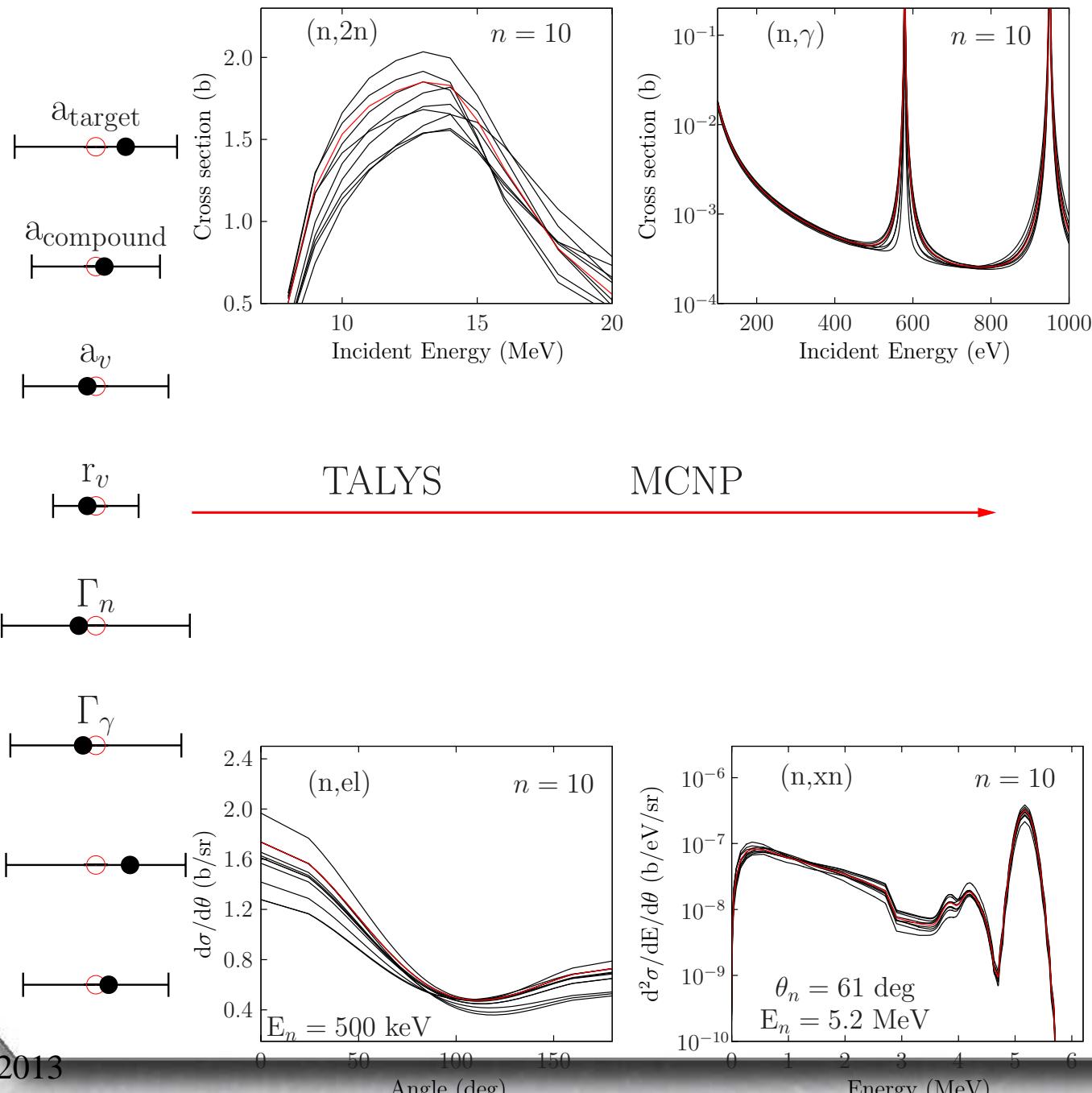
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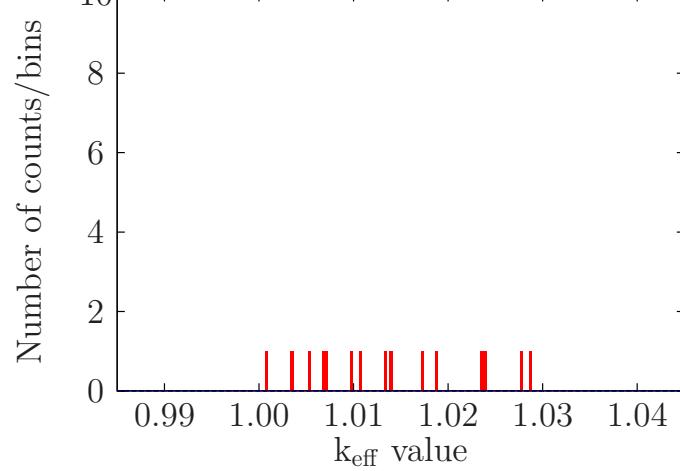
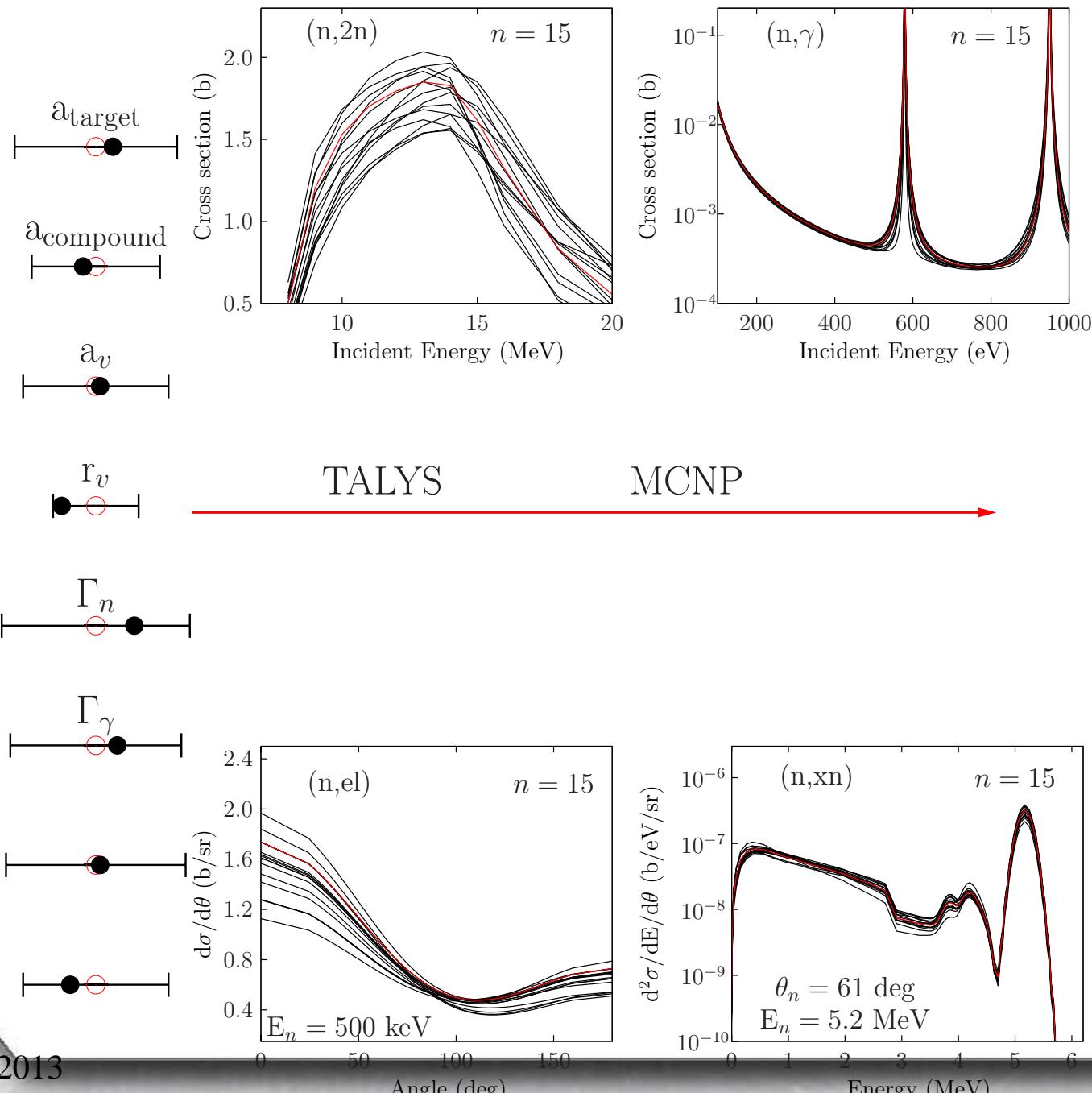
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# Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



$a_{\text{target}}$

$a_{\text{compound}}$

$a_v$

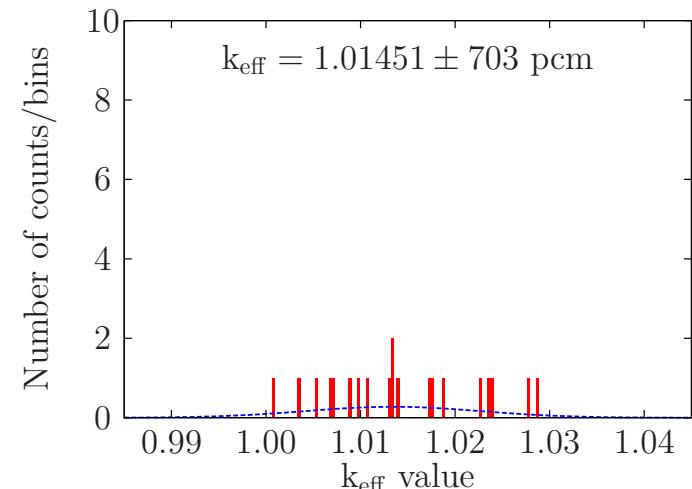
$r_v$

$\Gamma_n$

$\Gamma_\gamma$

$n = 20$

TALYS                    MCNP



# Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



$a_{\text{target}}$

$a_{\text{compound}}$

$a_v$

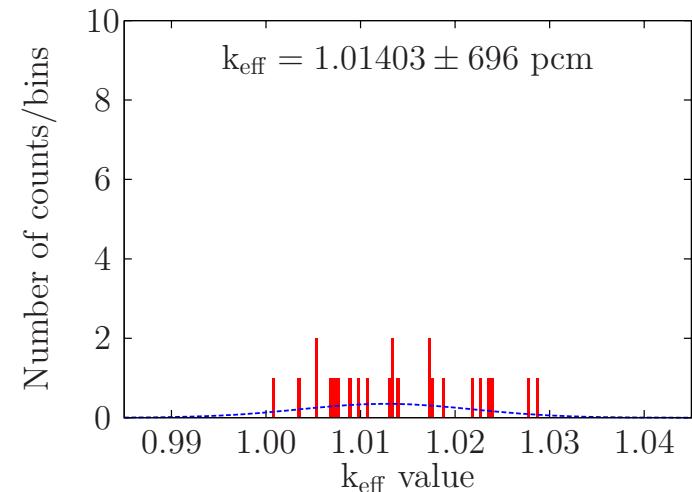
$r_v$

$\Gamma_n$

$\Gamma_\gamma$

$n = 25$

TALYS                    MCNP



# Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



$a_{\text{target}}$

$a_{\text{compound}}$

$a_v$

$r_v$

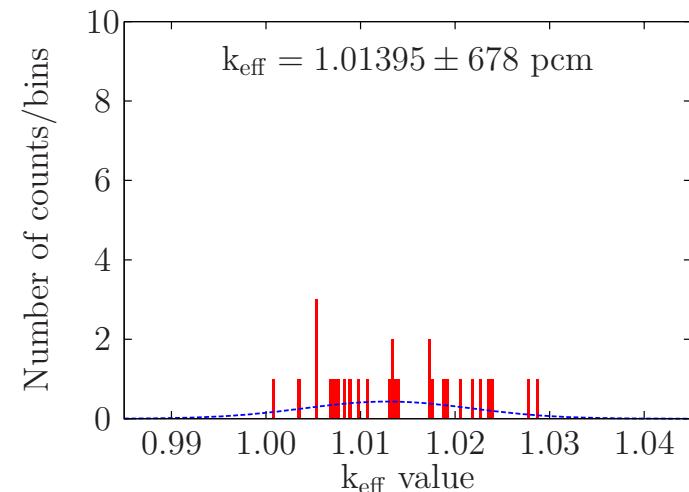
$\Gamma_n$

$\Gamma_\gamma$

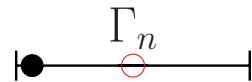
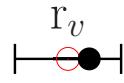
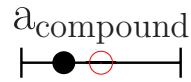
TALYS

MCNP

$n = 30$



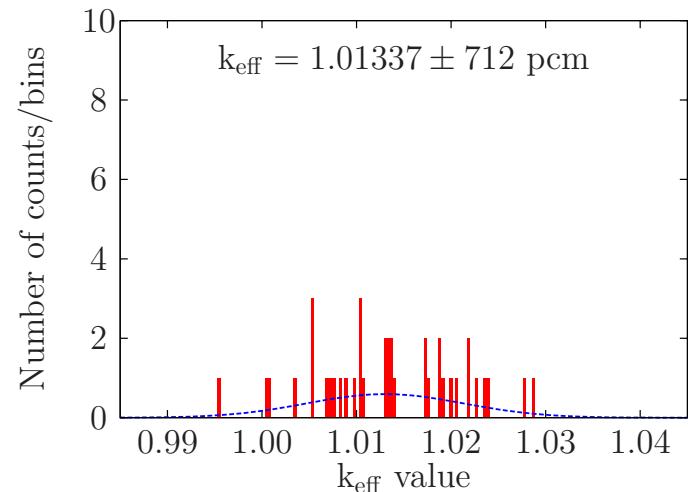
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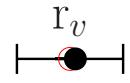
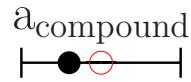
TALYS

MCNP

$n = 40$



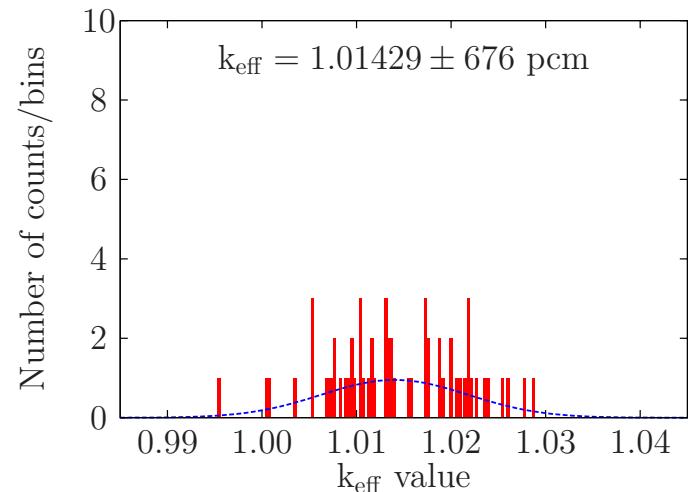
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TALYS

MCNP

$n = 60$



# Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



$a_{\text{target}}$

$a_{\text{compound}}$

$a_v$

$r_v$

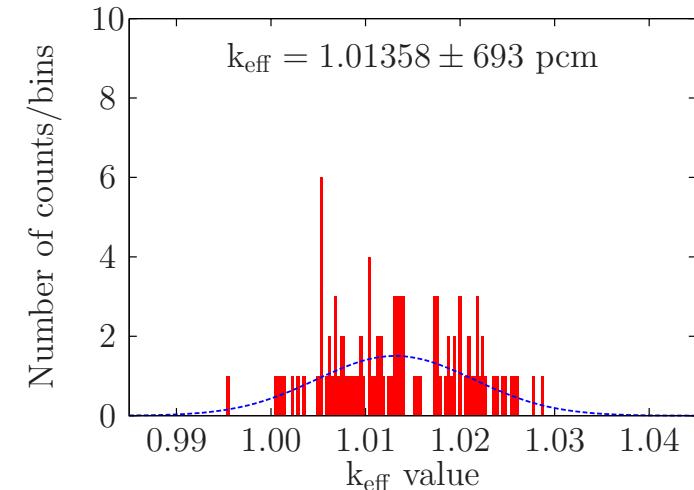
$\Gamma_n$

$\Gamma_\gamma$

$n = 100$

MCNP

TALYS



# Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



$a_{\text{target}}$

$a_{\text{compound}}$

$a_v$

$r_v$

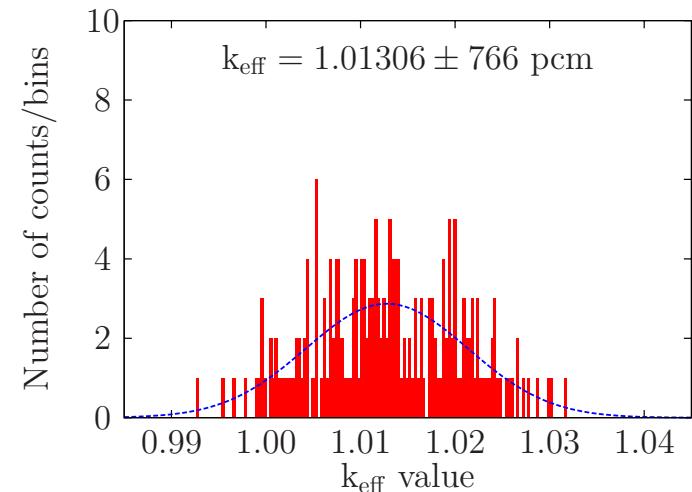
$\Gamma_n$

$\Gamma_\gamma$

TALYS

MCNP

$n = 200$



# Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



$a_{\text{target}}$

$a_{\text{compound}}$

$a_v$

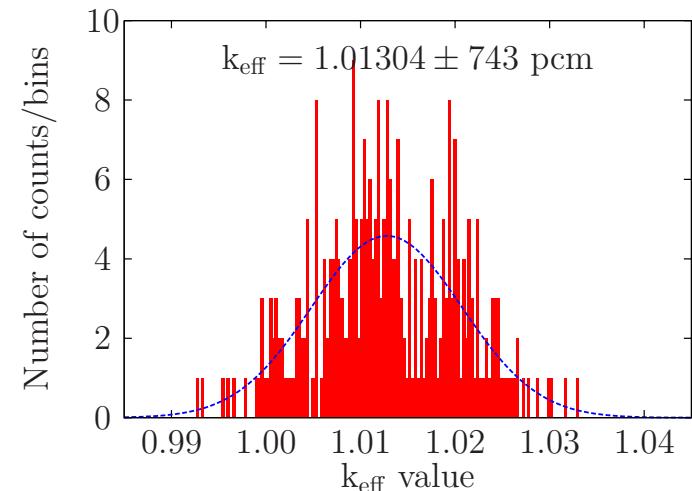
$r_v$

$\Gamma_n$

$\Gamma_\gamma$

TALYS                    MCNP

$n = 300$



# Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



$a_{\text{target}}$

$a_{\text{compound}}$

$a_v$

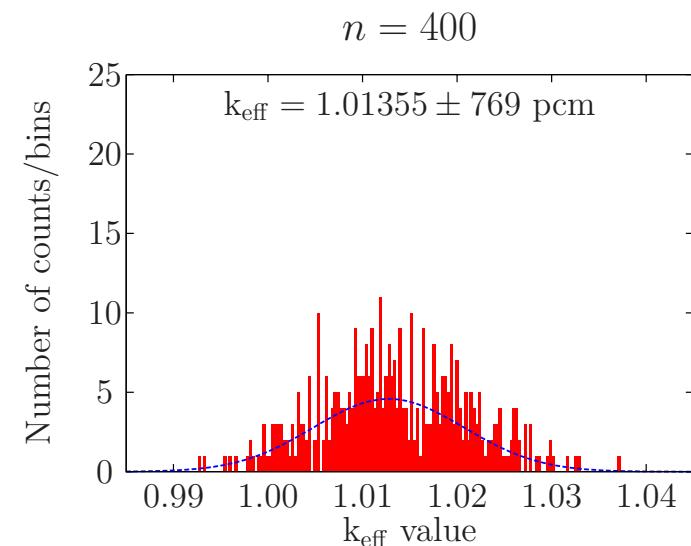
$r_v$

$\Gamma_n$

$\Gamma_\gamma$

TALYS

MCNP



# Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



$a_{\text{target}}$

$a_{\text{compound}}$

$a_v$

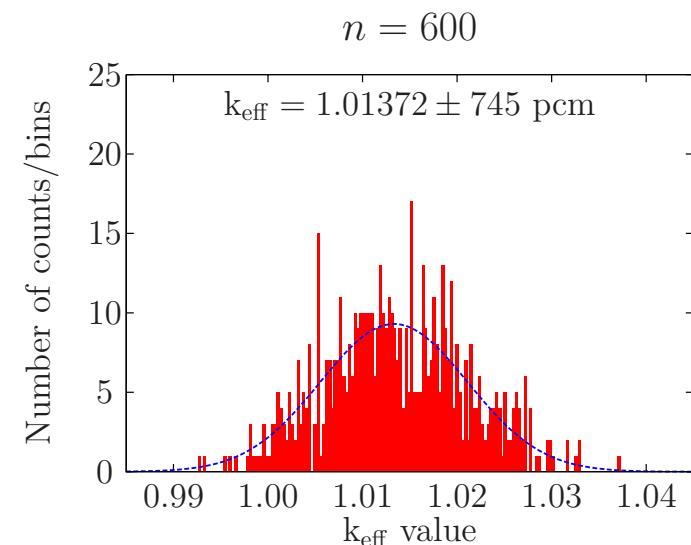
$r_v$

$\Gamma_n$

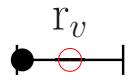
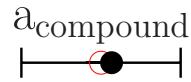
$\Gamma_\gamma$

TALYS

MCNP

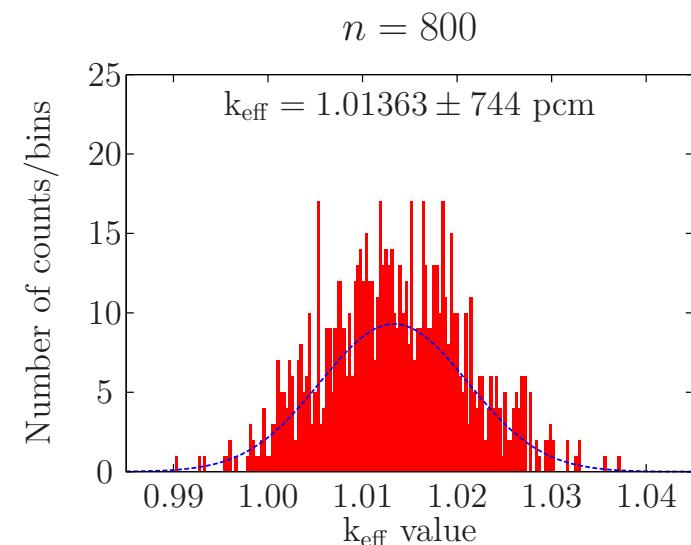


# Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



TALYS

MCNP



# Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



$a_{\text{target}}$

$a_{\text{compound}}$

$a_v$

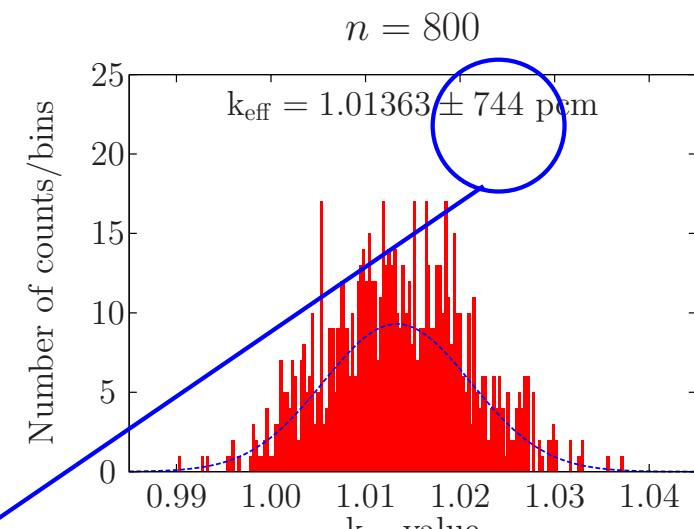
$r_v$

$\Gamma_n$

$\Gamma_\gamma$

TALYS

MCNP



Statistical uncertainty  $\simeq 68 \text{ pcm}$

$\Rightarrow$  uncertainty due to nuclear data  $\simeq 740 \text{ pcm}$

# Considered data in TMC (or fast TMC)



Several hundreds of random ENDF files for transport + depletion

- 3 Major actinides:  $^{235}\text{U}$ ,  $^{238}\text{U}$ ,  $^{239}\text{Pu}$ ,
- Light elements: lighter than oxygen,
- Thermal scattering data: H in  $\text{H}_2\text{O}$ , D in  $\text{D}_2\text{O}$ , C in Carbon,
- All Fission yields (e.g.  $^{234,235,236,238}\text{U}$ ,  $^{239,240,241}\text{Pu}$ ,  $^{237}\text{Np}$ ,  $^{241,243}\text{Am}$ ,  $^{243,244}\text{Cm}$ ),
- All Minor actinides (e.g.  $^{234,236,237}\text{U}$ ,  $^{237}\text{Np}$ ,  $^{238,240,241,242}\text{Pu}$ , Am, Cm),
- All fission products (e.g. from Ge to Er), and decay data,

(fast) TMC can be applied to **any** input data, propagating uncertainties to **any** outputs

# Considered data in TMC (or fast TMC)



Several hundreds of random ENDF files for transport + depletion

- 3 Major actinides:  $^{235}\text{U}$ ,  $^{238}\text{U}$ ,  $^{239}\text{Pu}$ ,
- Light elements: lighter than oxygen,
- Thermal scattering data: H in  $\text{H}_2\text{O}$ , D in  $\text{D}_2\text{O}$ , C in Carbon,
- All Fission yields (e.g.  $^{234,235,236,238}\text{U}$ ,  $^{239,240,241}\text{Pu}$ ,  $^{237}\text{Np}$ ,  $^{241,243}\text{Am}$ ,  $^{243,244}\text{Cm}$ ),
- All Minor actinides (e.g.  $^{234,236,237}\text{U}$ ,  $^{237}\text{Np}$ ,  $^{238,240,241,242}\text{Pu}$ , Am, Cm),
- All fission products (e.g. from Ge to Er), and decay data,

(fast) TMC can be applied to **any** input data, propagating uncertainties to **any** outputs

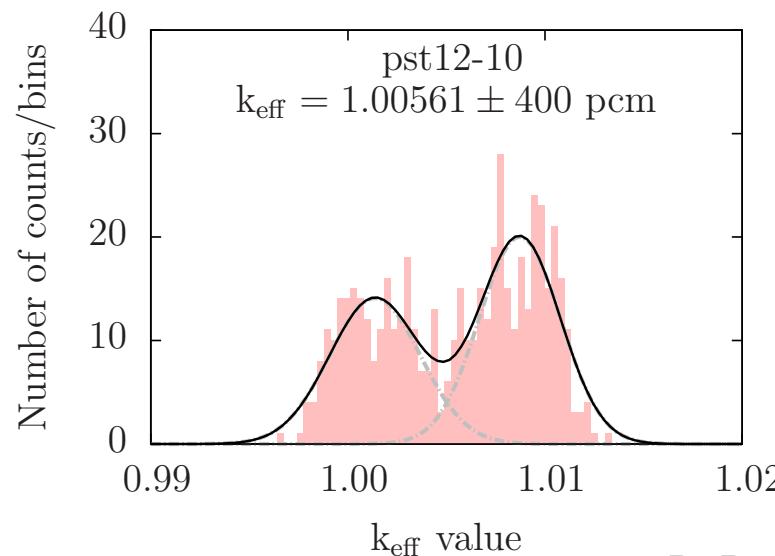
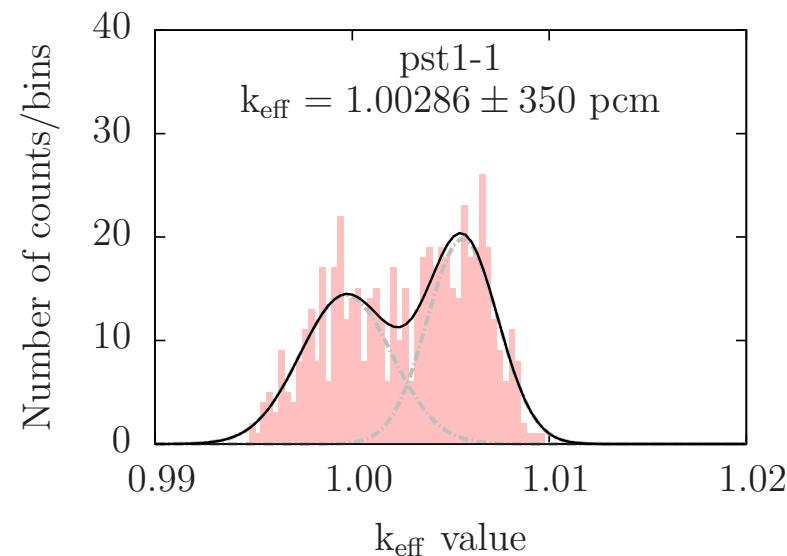
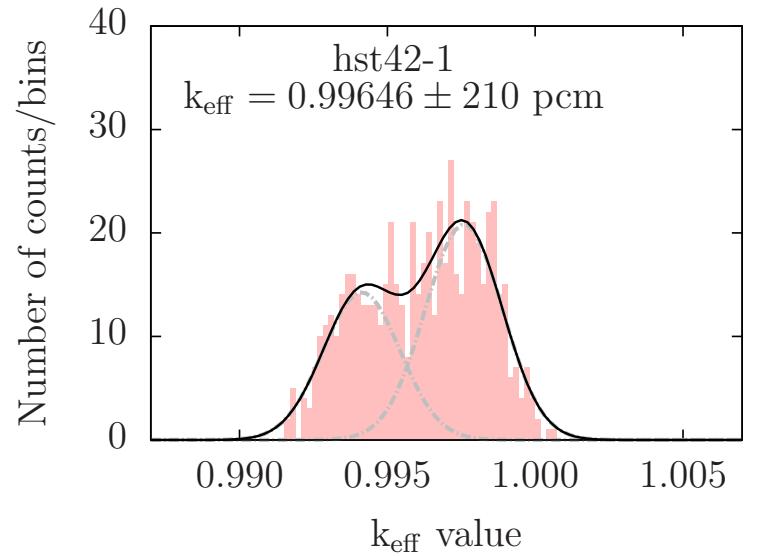
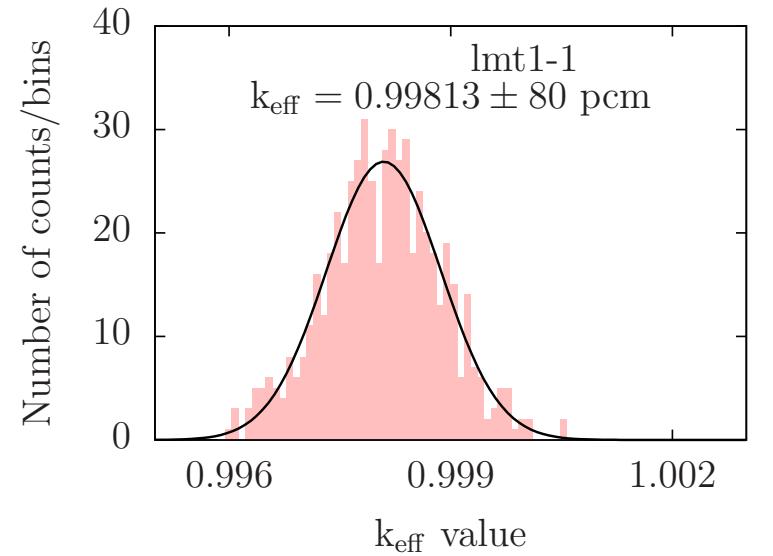
TMC was already applied to

- criticality-safety, shielding, pin-cell/assembly burn-up, full core, activation,
- PWR, BWR, Gen-IV systems,
- $\text{UO}_2$ , MOX fuels,
- MCNP, SERPENT, FISPACT, DRAGON, PANTHER, RELAP-5

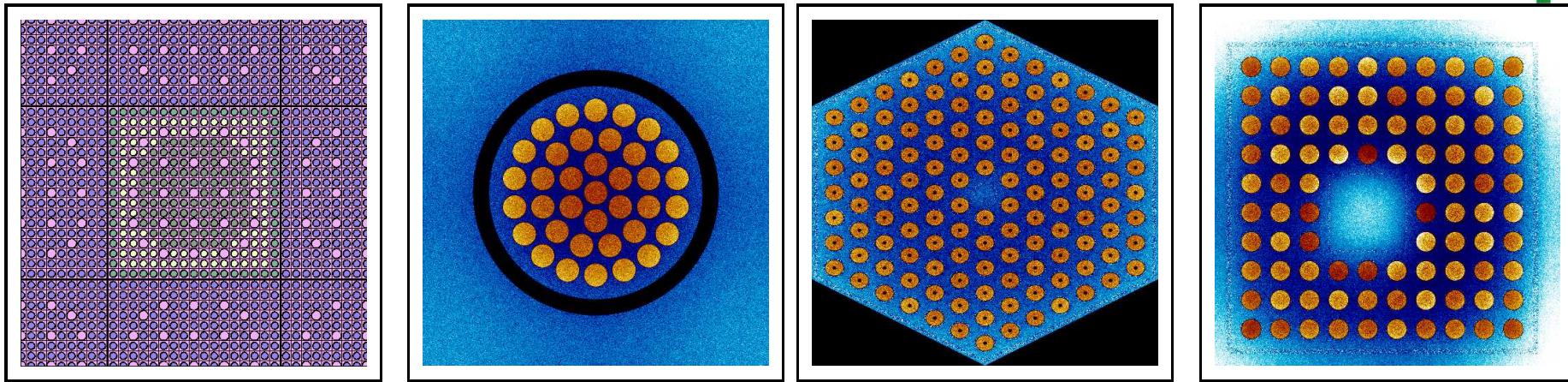
# Application: thermal scattering for H in H<sub>2</sub>O or S(α,β) tables (with MCNP)



Random parameters of the S(α,β) for inelastic scattering

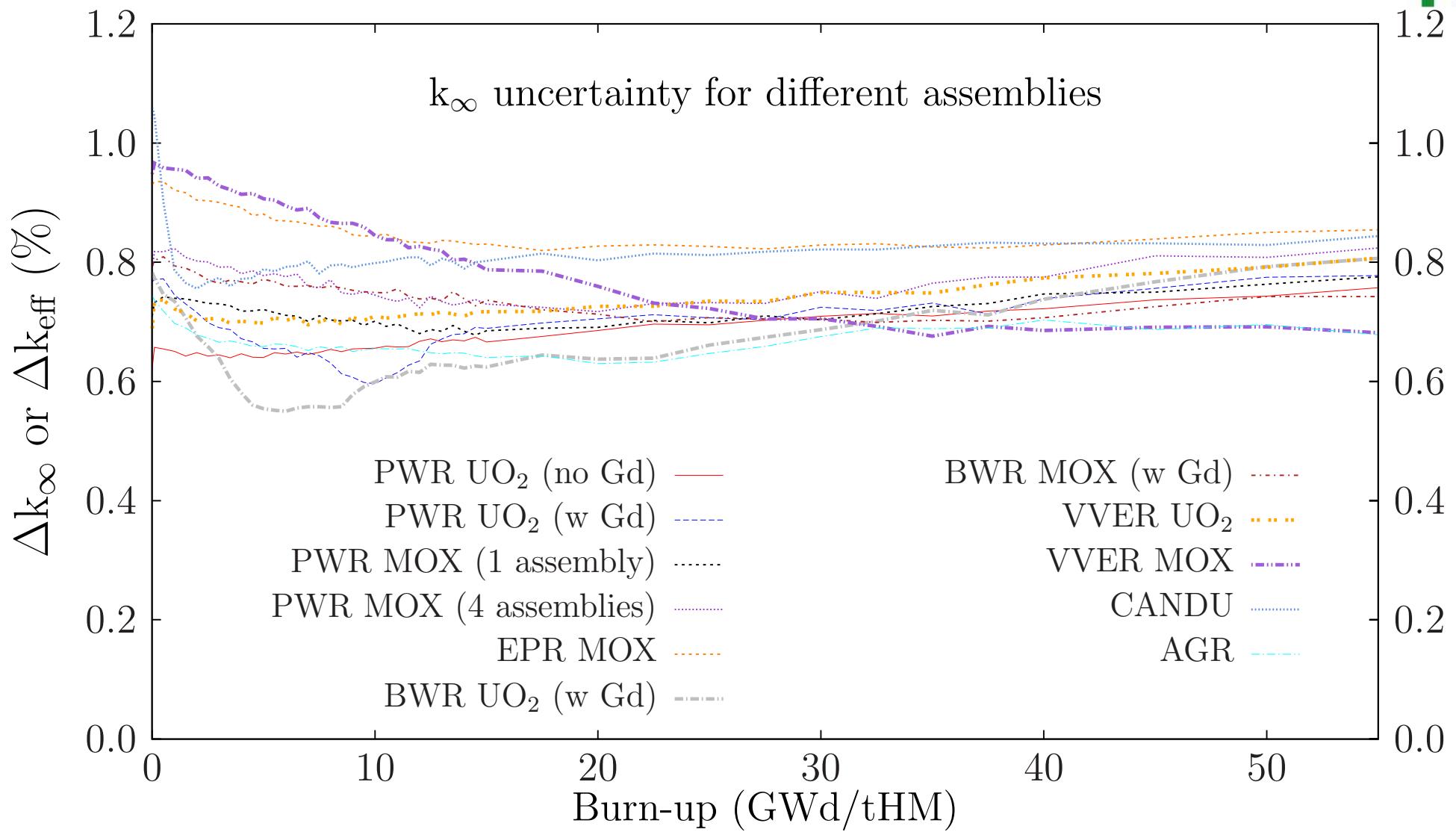


# Systematical study on UO<sub>2</sub>/MOX assembly uncertainties

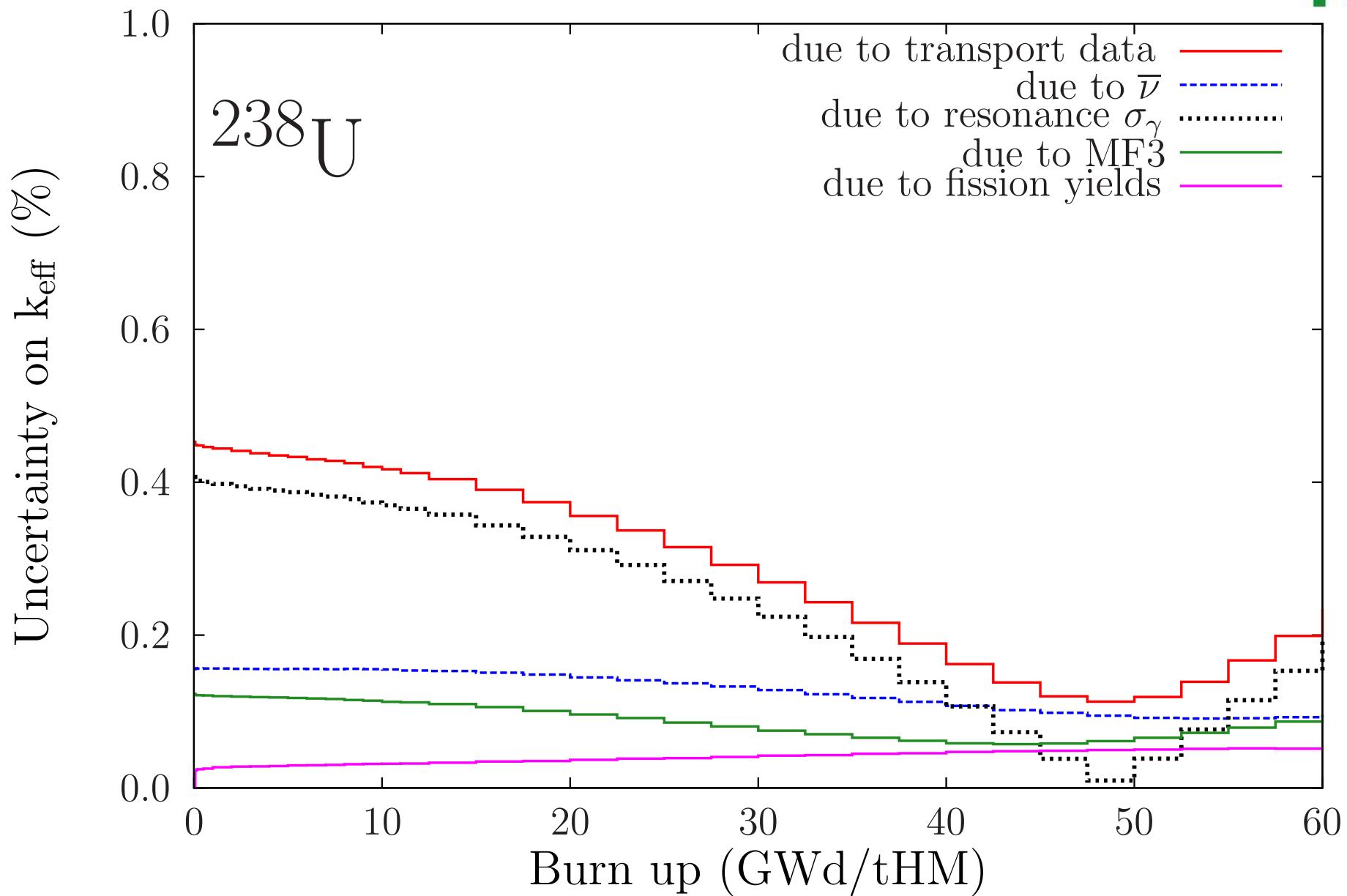


- Different UO<sub>2</sub>/MOX assemblies (PWR, BWR, VVER, AGR, CANDU, fast systems),
- Burn-up calculated with SERPENT,
- All major nuclear data taken into account.
- $\Rightarrow$  systematical study on  $k_{\text{eff}}$ , inventory, heat...

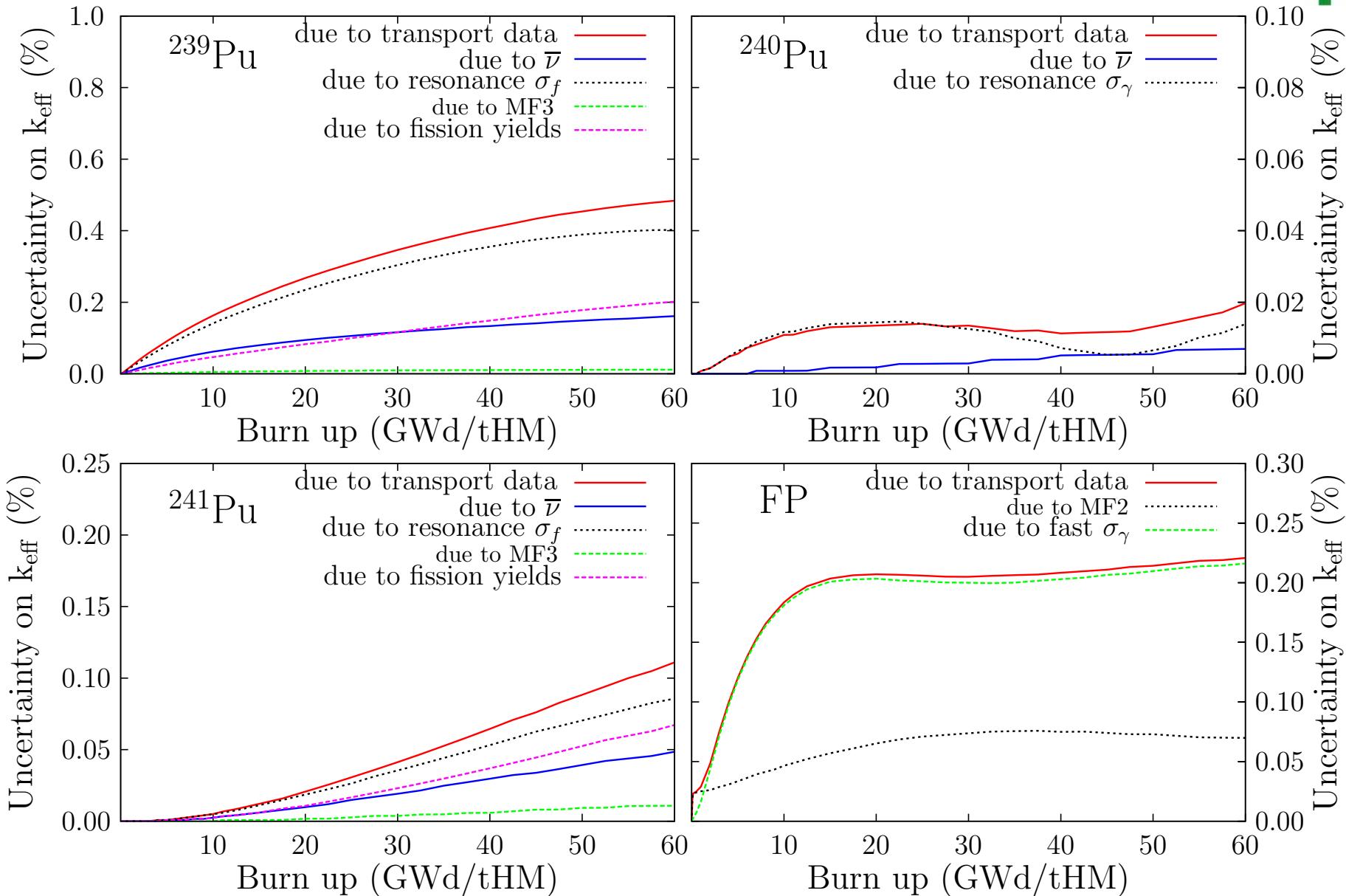
# Comparison of $\Delta k_{\infty}$ for assemblies and full core (SERPENT)



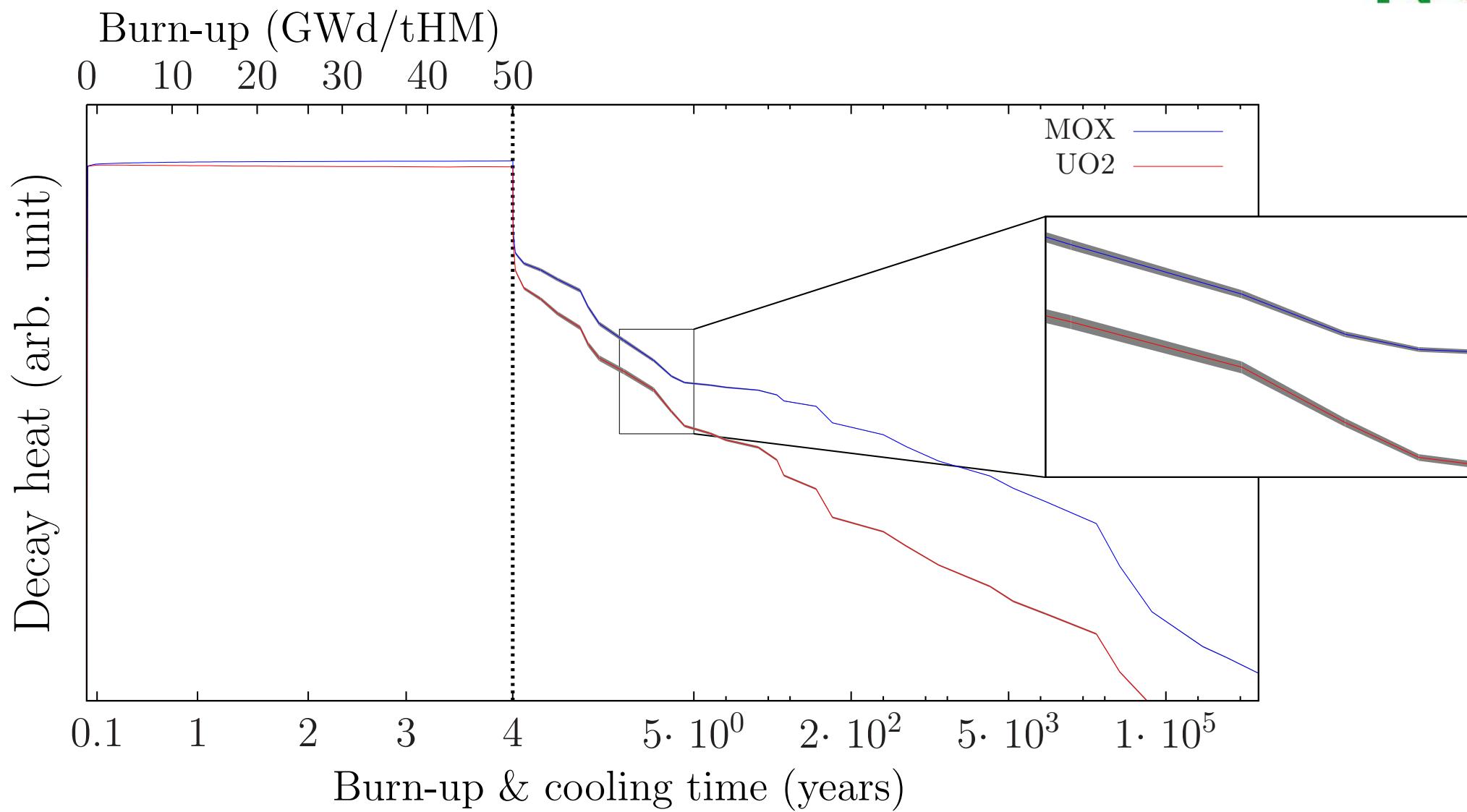
# TMC applied to PWR assembly burn-up calculations with DRAGON



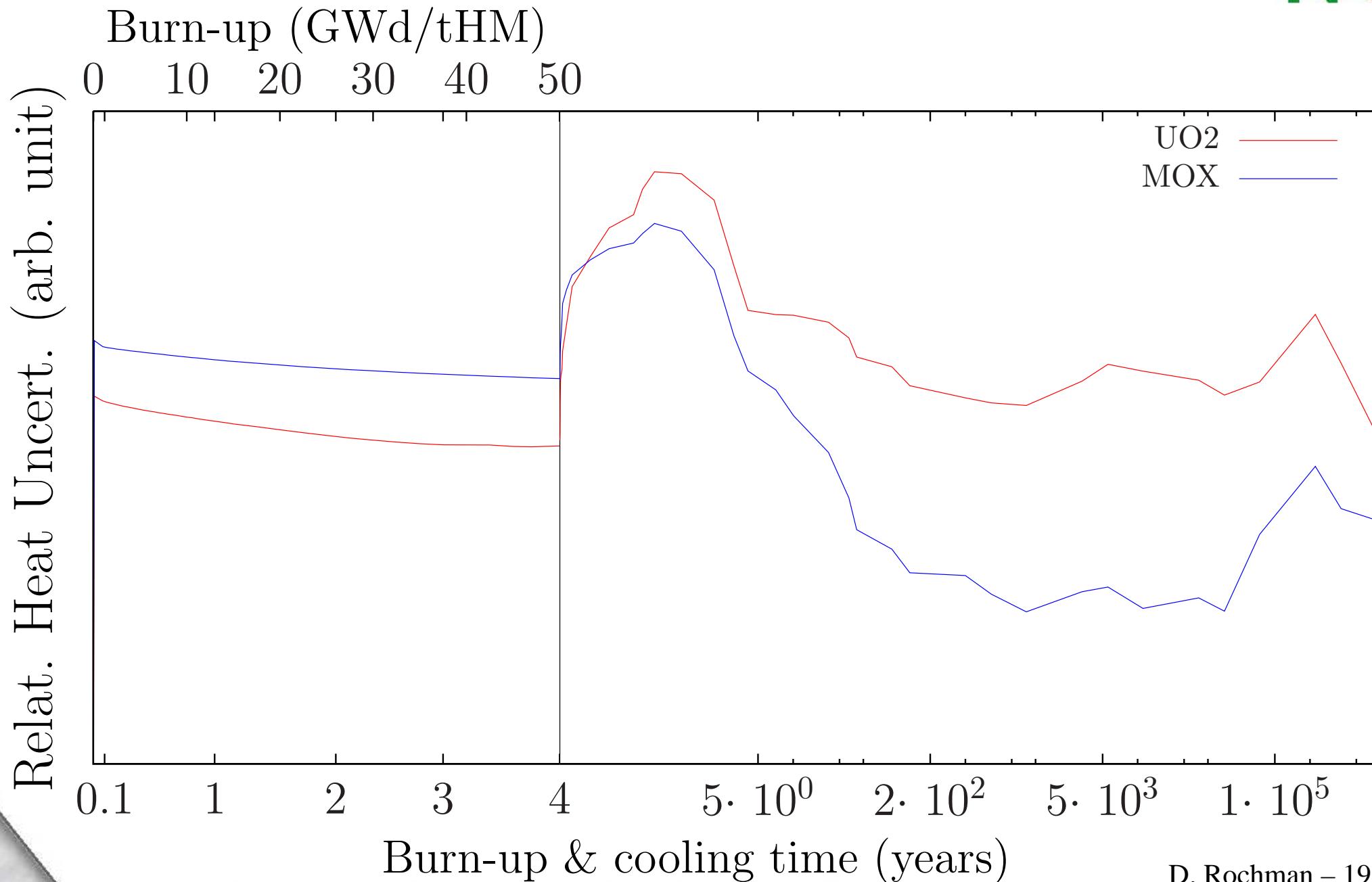
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# TMC applied for burn-up calculations: decay heat



# TMC applied for burn-up calculations: decay heat uncertainties



# Effect of H in H<sub>2</sub>O for a full core PWR (courtesy of O. Cabellos, UPM, Spain)



Method: TMC applied to COBAYA (3D multigroup core calculations) + SIMULA (coupled neutronic-thermohydraulics 3D core calculations)

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## III.2 PWR problem description

PWR (WESTINGHOUSE), 3 loops , 157 FA, power 2775. MWth

**1/4 CORE**

	1	2	3	4	5	6	7	8	→
1	1	13	4	21	6	21	16	14	
2	13	11	15	2	16	6	20	7	
3	4	15	3	21	8	22	19		
4	21	2	21	9	18	20	5		
5	6	16	8	18	12	17			
6	21	6	22	20	17				
7	16	20	19	10					
8	14	7							

↓

**AVE. BURNUP PER FUEL ASSEMBLY**

	1	2	3	4	5	6	7	8
1	18.137	11.662	27.397	0.000	30.867	0.000	14.984	11.662
2	11.662	16.188	13.130	28.902	12.155	28.866	0.000	30.191
3	27.397	13.130	27.572	0.000	22.778	0.000	0.000	
4	0.000	28.902	0.000	30.755	15.236	0.000	30.124	
5	30.867	12.155	22.778	15.236	13.123	14.882		
6	0.000	28.866	0.000	0.000	14.882			
7	14.984	0.000	0.000	30.503				
8	11.662	30.191						

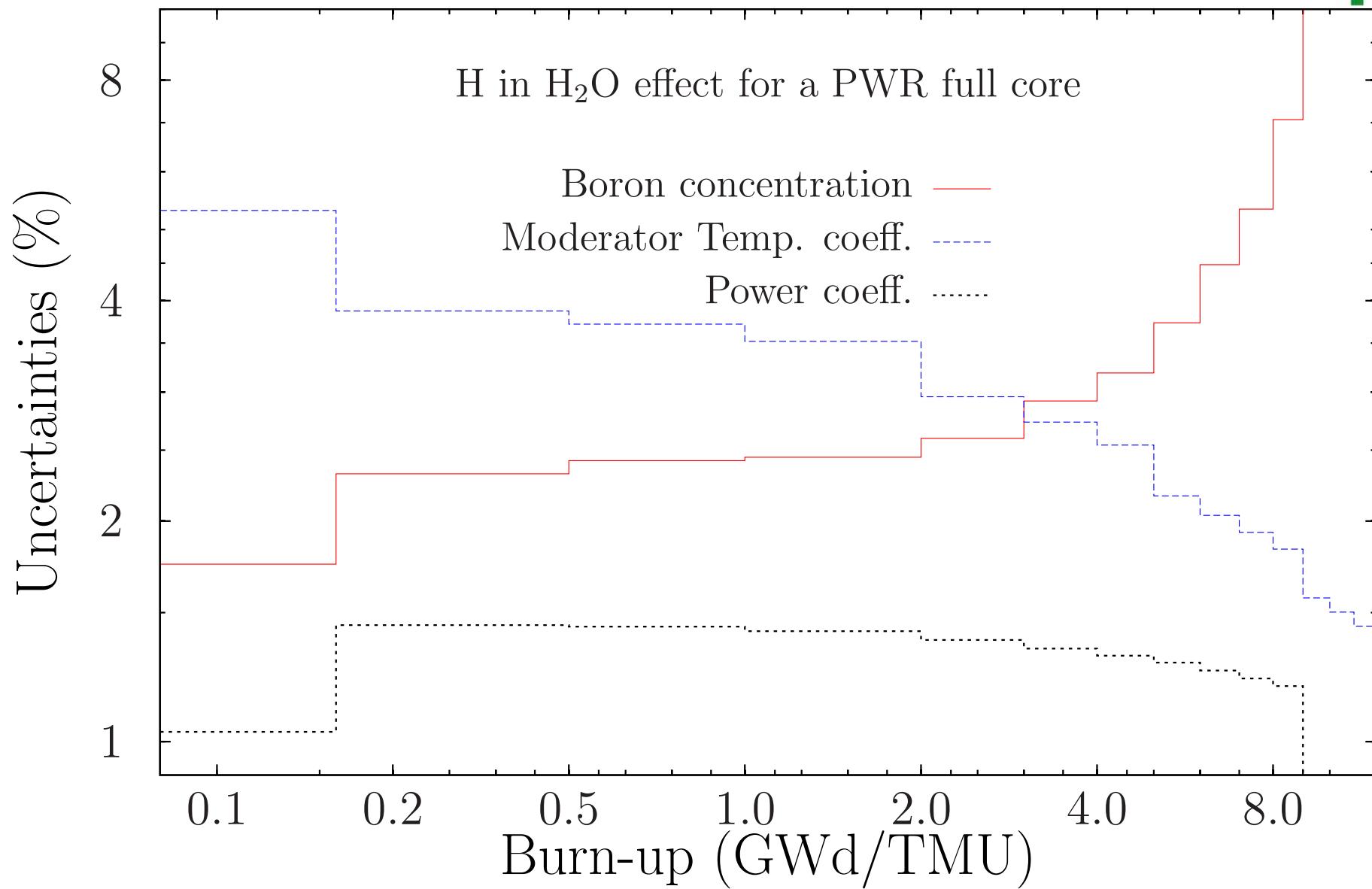
**FUEL TYPE w/o(%) WABAS**

1	OFA	2.10	0
2	OFA	3.10	0
3	OFA	3.24	0
4	OFA	3.24	0
5	OFA	3.24	0
6	OFA	3.24	0
7	OFA	3.24	0
8	OFA	3.24	0
9	OFA	3.24	0
10	OFA	3.24	0
11	OFA	3.24	0
12	AEF	3.60	0
13	AEF	3.60	0
14	AEF	3.60	0
15	AEF	3.60	0
16	AEF	3.60	0
17	AEF	3.60	0
18	AEF	3.60	0
19	AEF	3.60	0
20	AEF	3.60	4
21	AEF	3.60	8
22	AEF	3.60	12

**UAM7 – Paris (France), April 10-12, 2013**

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# Effect of H in $H_2O$ for a full core PWR (courtesy of O. Cabellos, UPM, Spain)



## Drawbacks of the TMC method



In TMC:

*If we can do a calculation **once**, we can also do it a **1000** times, each time with a varying data library.*

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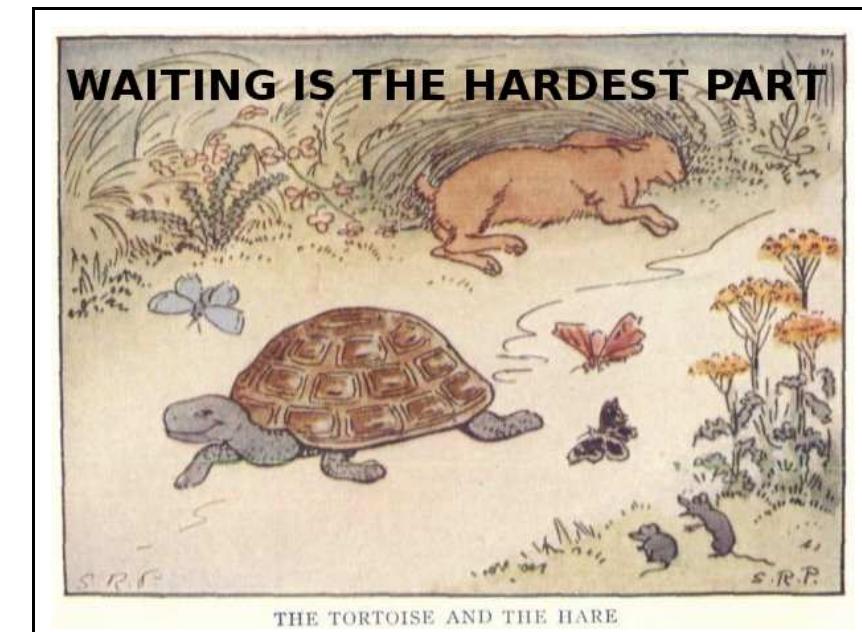


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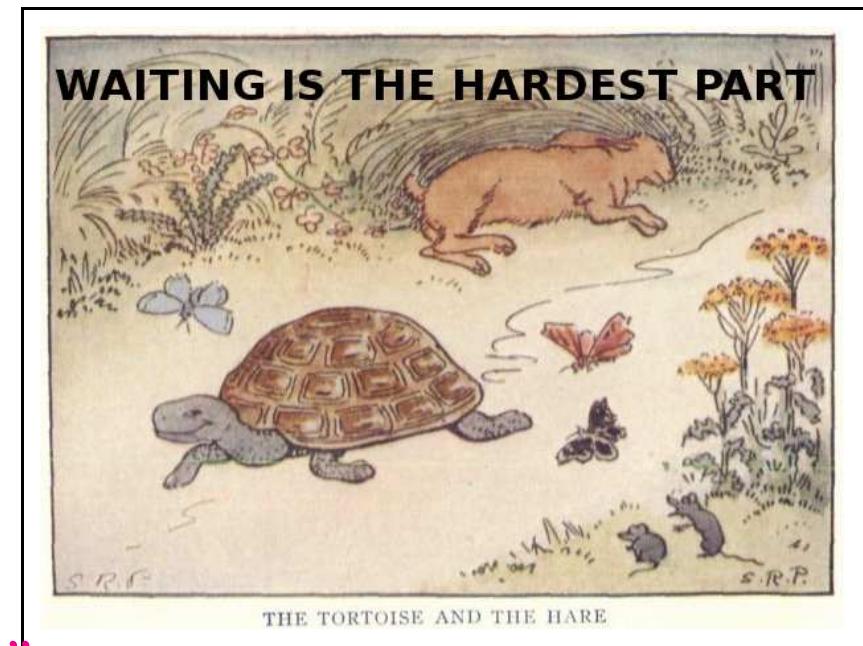
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There is a solution with Monte Carlo codes:  
(in fact 2 solutions)

- \* fast GRS method,
- \* and fast TMC.



**"Efficient use of Monte Carlo: uncertainty propagation"**,

D. Rochman, W. Zwermann et al., submitted to NSE, May 2013.

## 2012: fast GRS method



First presented in PHYSOR-2012 by W. Zwermann *et al.*. It takes advantage of conditional expectations:

If two output variables  $k^{(1)}$  and  $k^{(2)}$  are identically distributed and conditionally independent given the vector of nuclear data input then

$$\sigma_{\text{nuclear data}} = \sqrt{\text{cov}(k^{(1)}, k^{(2)})}$$

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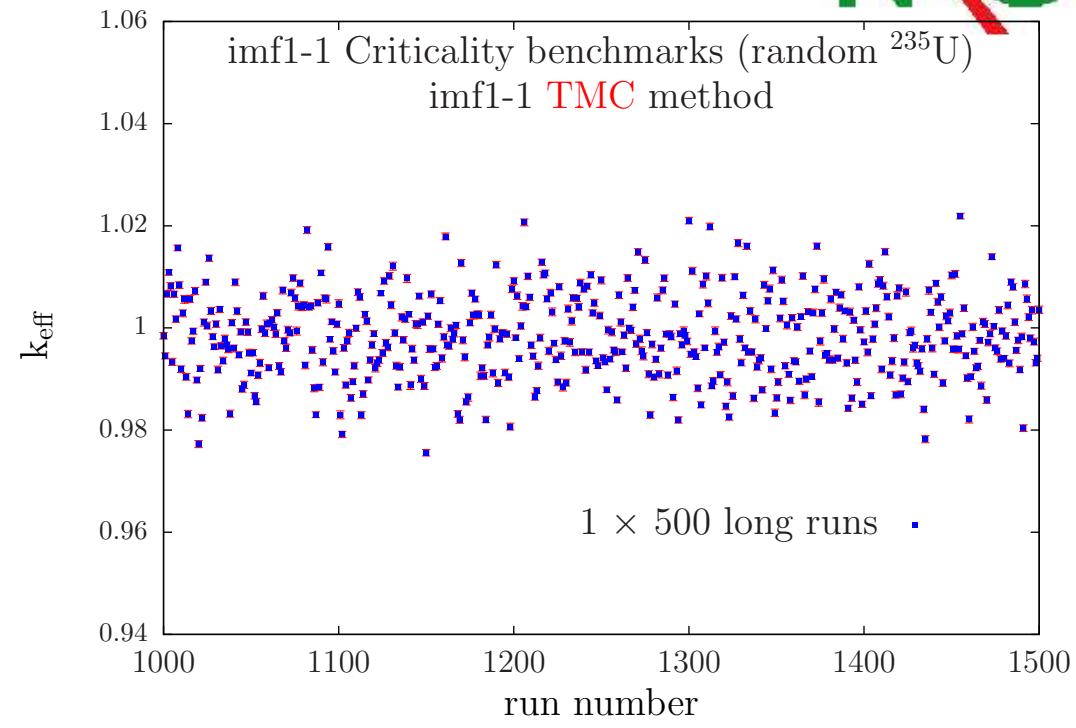
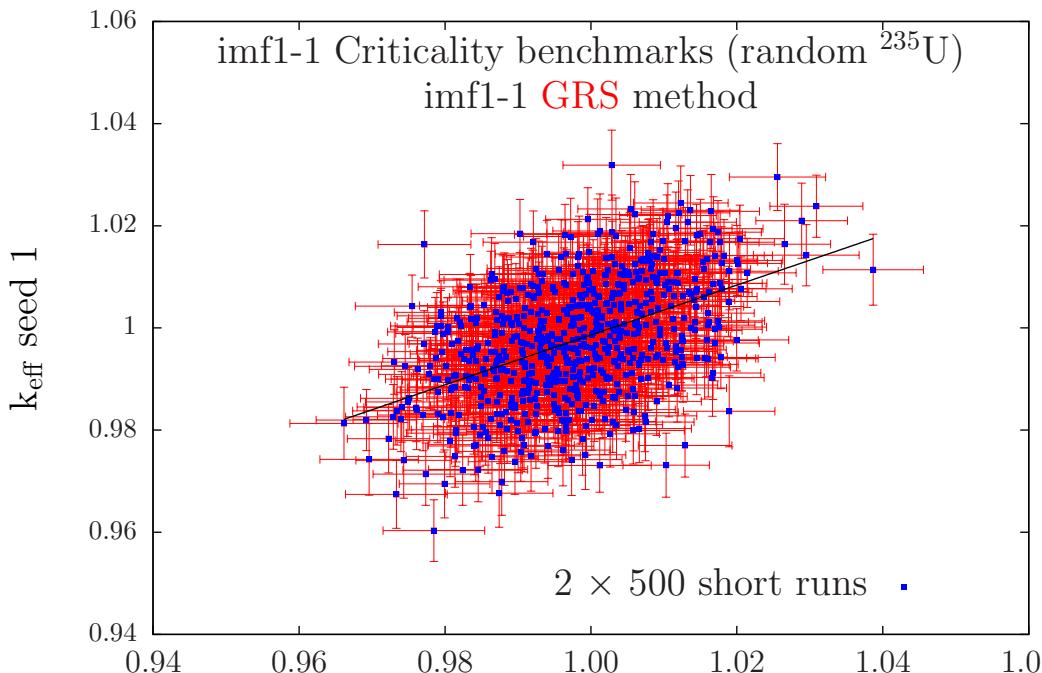
$$\sigma_{\text{nuclear data}} = \sqrt{\text{cov}(k^{(1)}, k^{(2)})}$$

In practice:

1. perform  $i = 1..500$  MCNP short calculations with random nuclear data and a fixed seed  $s_1 \implies k_{\text{eff}}^{(1)}(i)$
2. repeat for  $j = 1..500$ , same random nuclear data but fixed seed  $s_2 \implies k_{\text{eff}}^{(2)}(j)$

There is no necessity to have small  $\sigma_{\text{statistics}}$  !!  
each run can be (very) short

# fast GRS method



$2 \times 500$  "short" runs  $\sim 2 \times$  "long" run in time

If a single calculation takes  $m$  histories ( $\sigma_{\text{stat}}$  small enough),  
then repeat it  $n$  times with  $m/n$  histories,  
random nuclear data and random seeds.

$$\sigma_{\text{total}}^2 = \sigma_{\text{statistics}}^2 + \sigma_{\text{nuclear data}}^2 \text{ still holds.}$$

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## The fast methods

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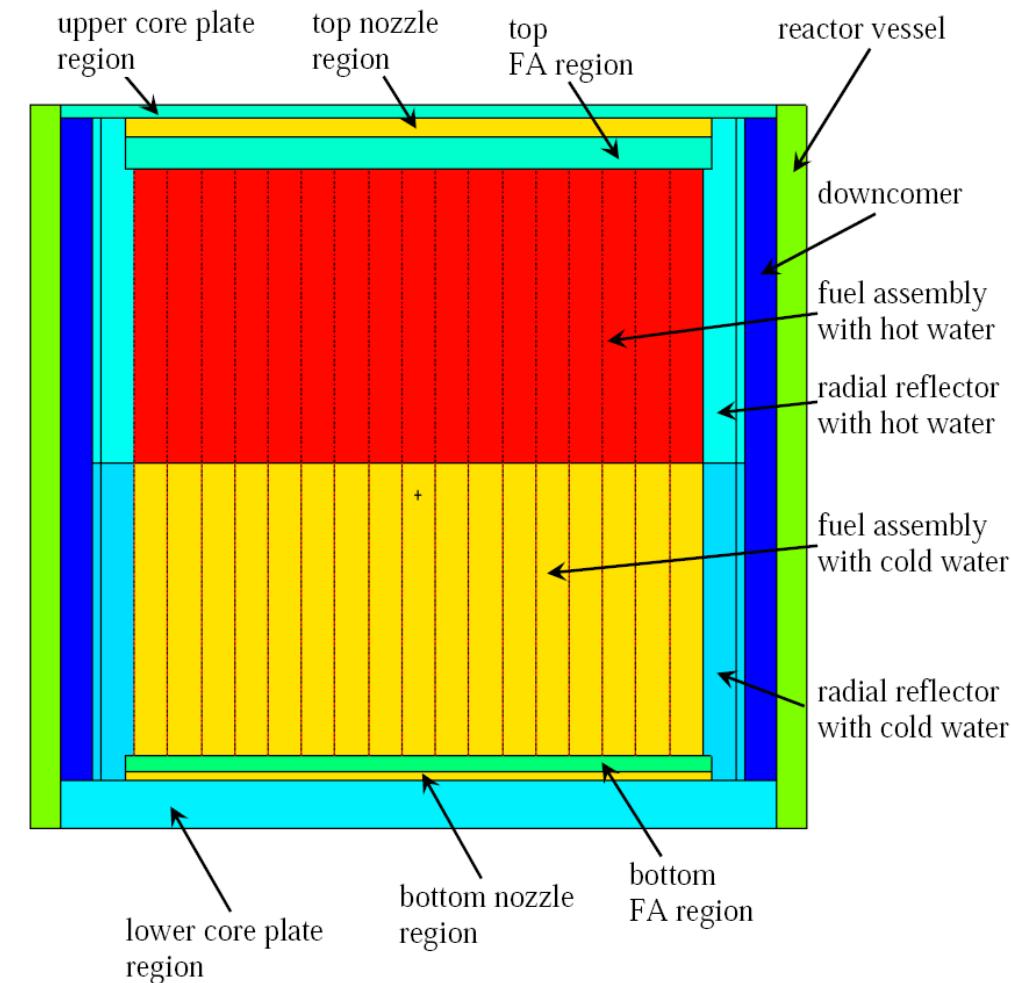
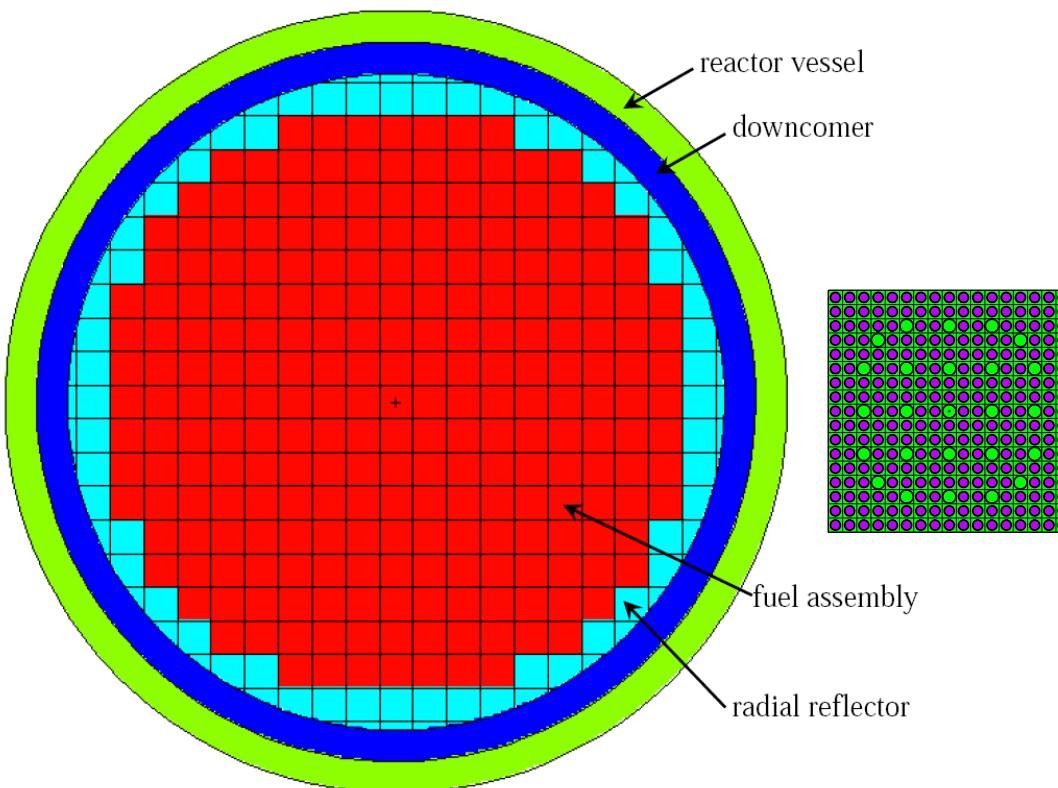


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- ☺ as fast as S/U methods ( $1-2 \times$  longer than 1 single calculation),
- ☺ tested on criticality & shielding benchmarks, burn-up ( $k_{\text{eff}}$  and inventory),
- ☺ Example: the Martin-Hoogenboom benchmark

MCNP6 model: 241 fuel assemblies,  
with 264 fuel pins each



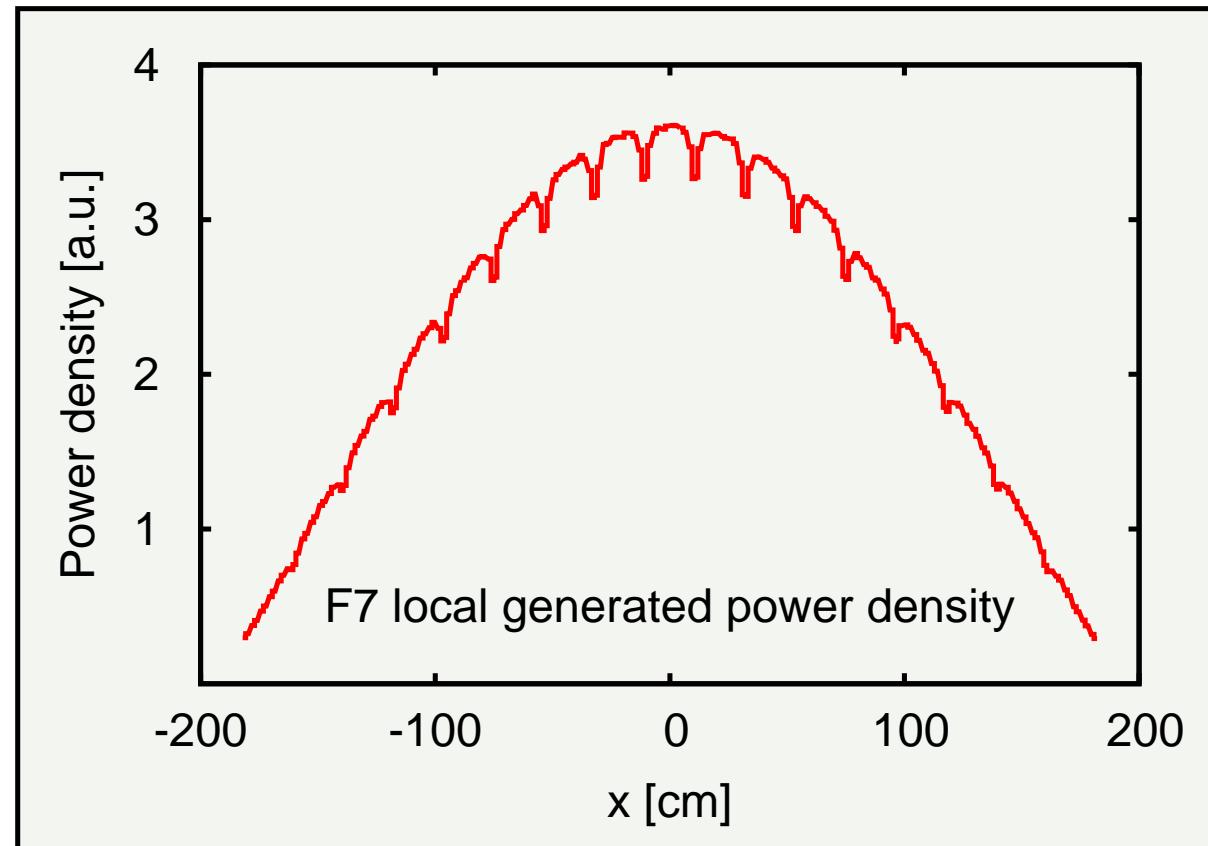
## Fast TMC & GRS methods on a full core



- ⌘  $357 \times 357 \times 100$  regions ( $1.26 \times 1.26 \times 3.66 \text{ cm}^3$ ): 6.4 million cells for generated power (f7)
- ⌘ 1 calculation takes  $2 \times 10^{11}$  histories ( $\sigma_{\text{statistics}} = 0.25 \%$  at the center, **500 weeks** on 1 cpu)

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- ⇒ Uncertainty on local pin power due to  $^{235}\text{U}$ ,  $^{238}\text{U}$ ,  $^{239}\text{Pu}$  and H in  $\text{H}_2\text{O}$  thermal scattering in **each cell** ?



## Fast TMC & GRS methods on a full core



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## (1) Source convergence

- For both methods, a first calculation is run with fixed nuclear data to obtain a reasonably converged fission source.
- All subsequent short simulations start with this fission source:
  - each with 10 inactive cycles and 90 active cycles of  $4 \times 10^6$  histories, and random nuclear data,
  - source convergence tested with the MCNP6 built-in indicator (fission source entropy).
  - **362** short runs out of 508 were then accepted for fast TMC.
  - **2 × 122** short runs out of  $2 \times 328$  were then accepted for fast GRS.

## (2) Statistical uncertainty estimation

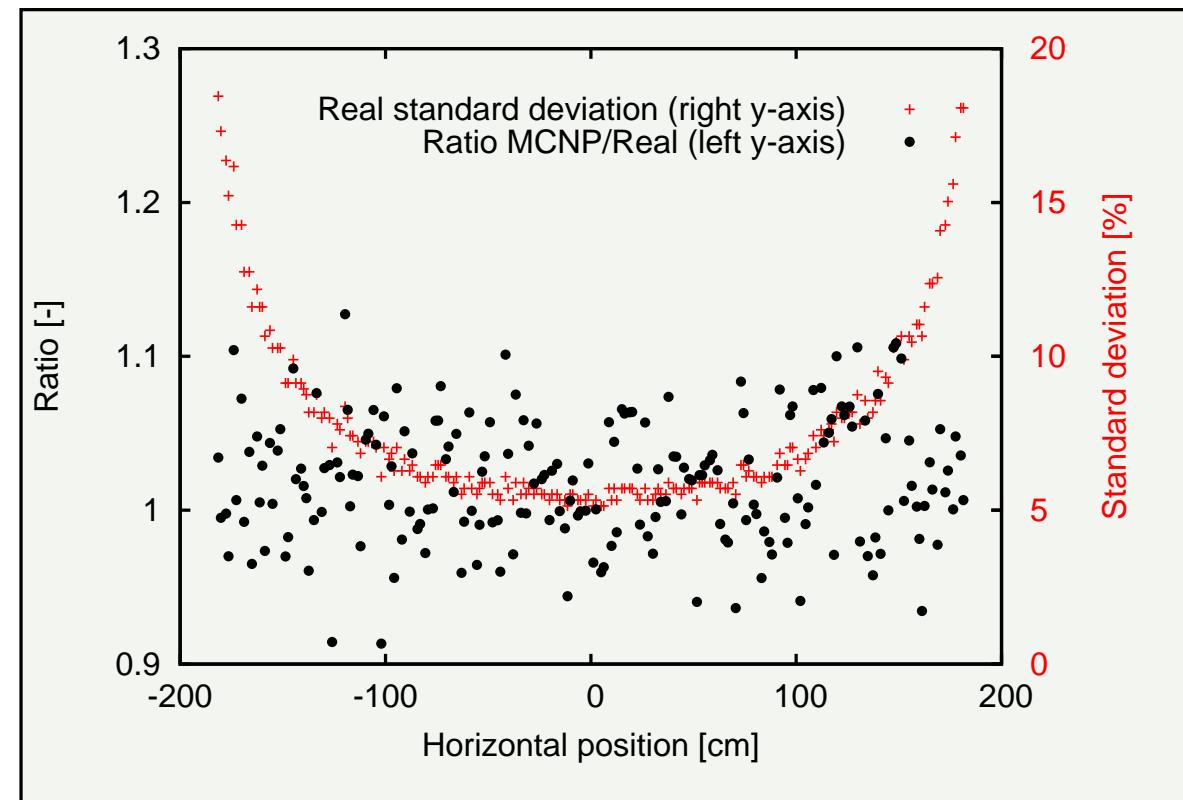
- ⌘ In MCNP eigenvalue calculation,  $\sigma_{\text{stat}}$  is usually underestimated.
- ⌘ An independent estimation of  $\sigma_{\text{stat}}$  is therefore necessary for fast TMC,
- ⌘ From the 508 short runs, the first 389 were repeated with fixed nuclear data,
- ⌘ 274 were then accepted due to source convergence.

# Fast TMC & GRS methods on a full core

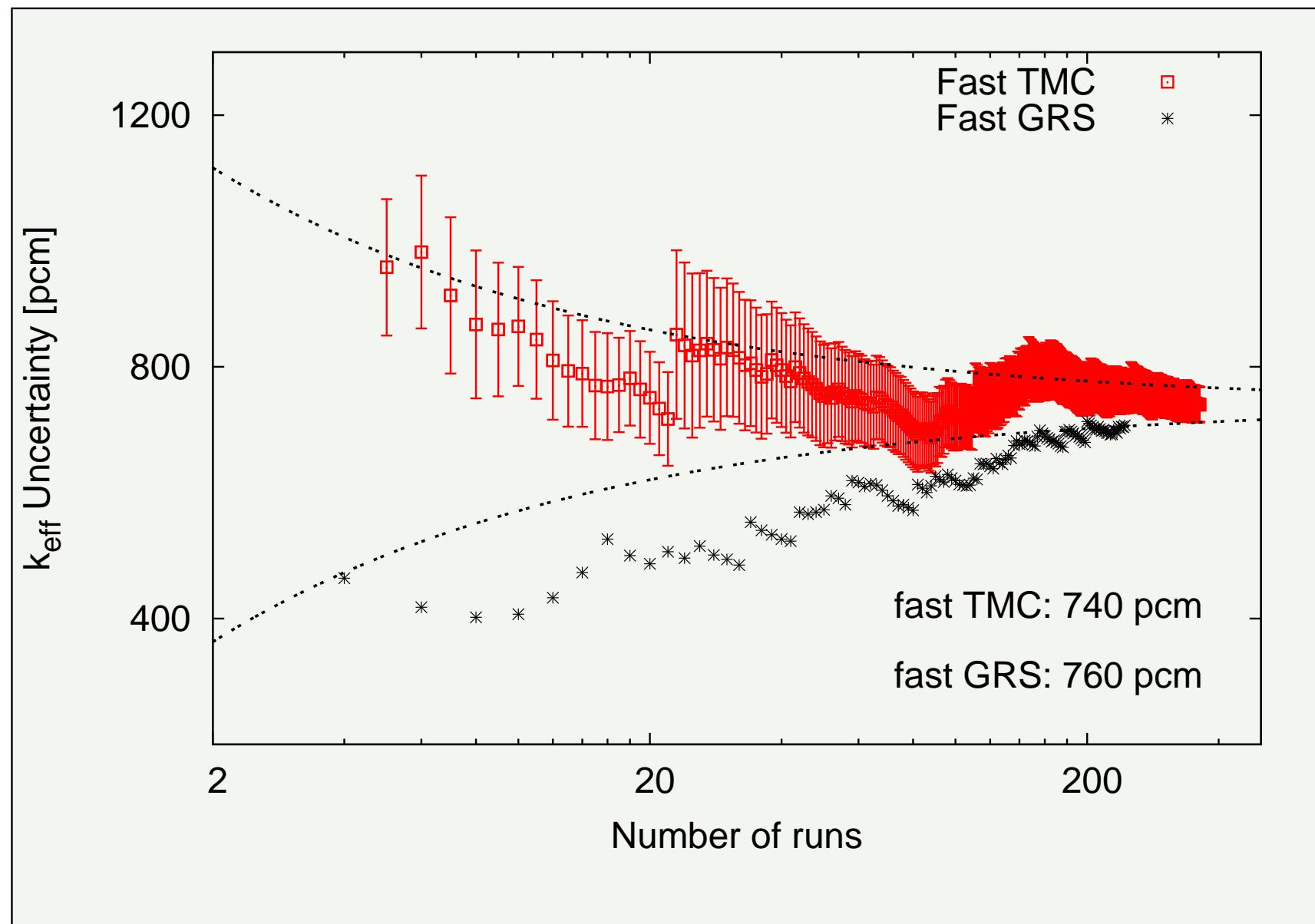
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- \* From the 508 short runs, the first 389 were repeated with fixed nuclear data,
- \* 274 were then accepted due to source convergence.
- \* 9 % difference for  $k_{\text{eff}}$
- \* for generated power ( $f_7$ ):  
ratio is  $1.019 \pm 0.040$ .

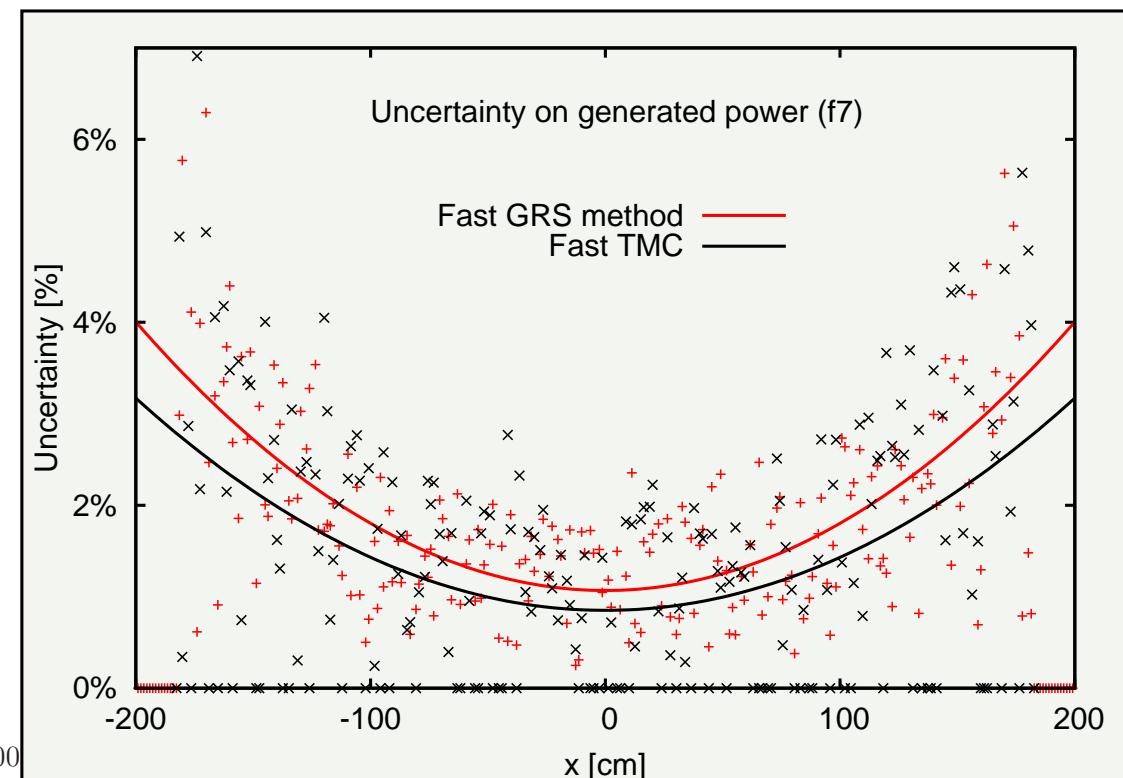
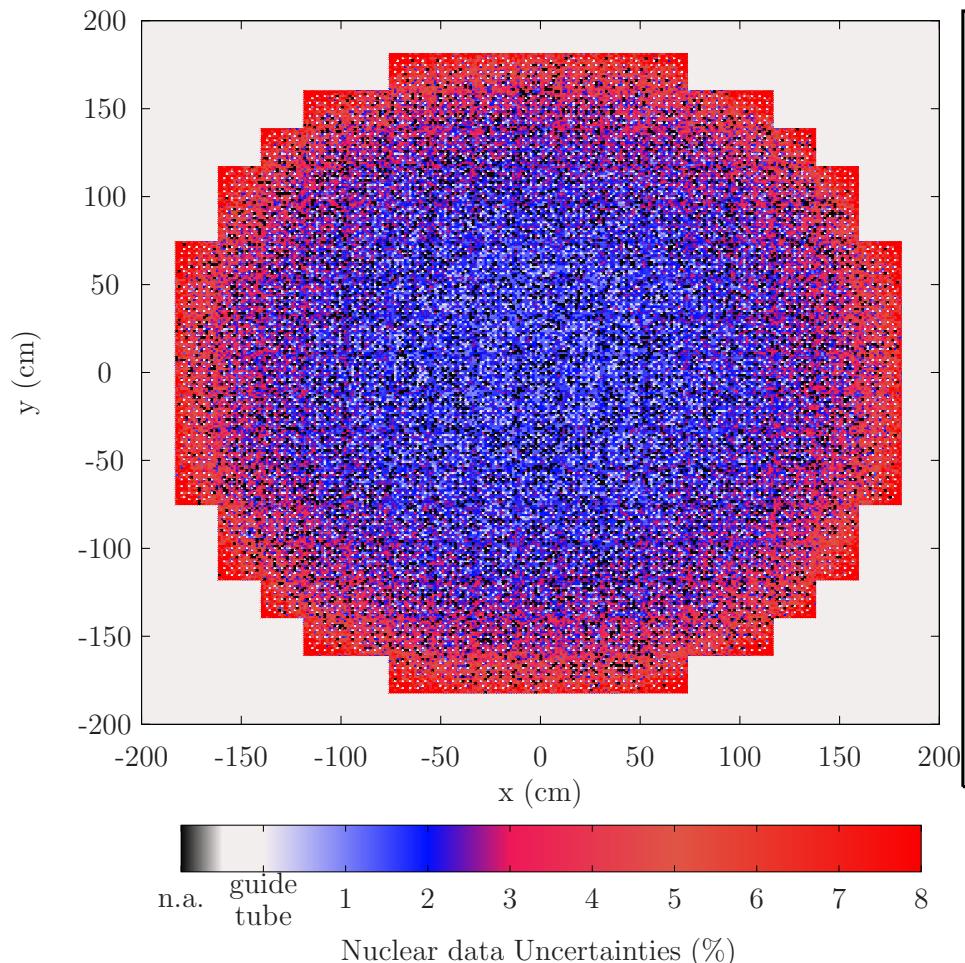
Therefore, for local power,  
the MCNP estimation of  $\sigma_{\text{stat}}$  is  
good enough.



# Fast TMC & GRS methods on a full core: $k_{\text{eff}}$ uncertainty



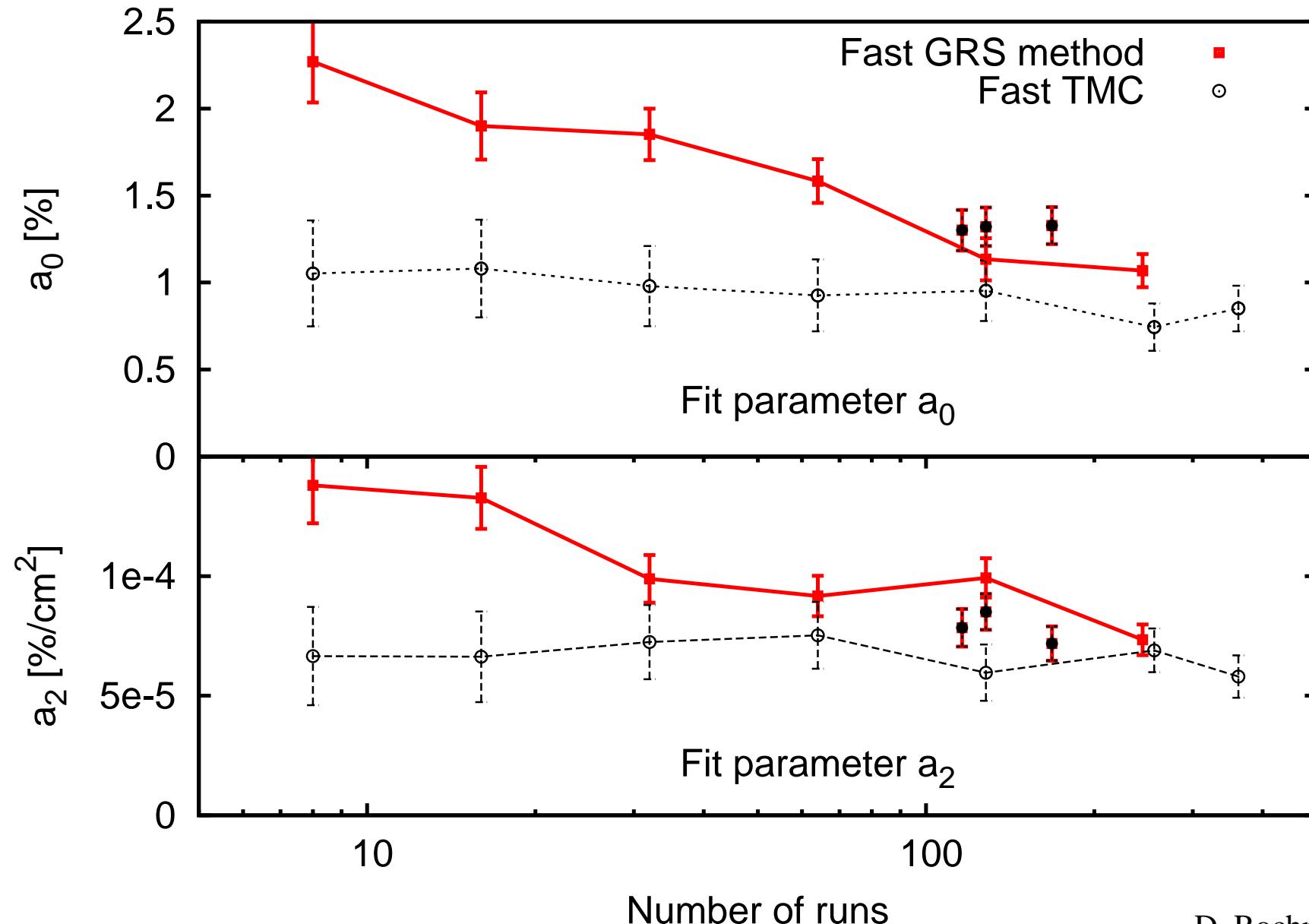
# Fast TMC & GRS methods on a full core: generated local power



# Fast TMC & GRS methods on a full core: generated local power



\* The previous uncertainties can be fitted using  $f(x) = a_0 + a_2x^2$



# Conclusions

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fast TMC and GRS methods:  
*If we can do a calculation **once**, we can also get  
nuclear data uncertainties in **twice** the time  
(or less).*

