

Living without covariance files

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- ① Motivations for a change:
 \implies *a roadmap to circumvent problems with covariance files*
- ② Concept:
 \implies *Monte Carlo from nuclear data to large-scale systems*
- ③ How does it work ?
- ④ Examples with Pb isotopes:
 \implies *k_{eff} benchmarks and reactors*
- ⑤ Examples on global scale:
 \implies *k_{eff} benchmarks, fusion shielding, reactivity swing*
- ⑥ Pros & Cons
- ⑦ Conclusions

Introduction: Motivations for a change



Usual procedures in uncertainty propagation imply:

- ☞ rigid format, fixed libraries of cross sections, simplification of covariances,
- ☞ need for processing, sensitivity and perturbation codes, group scheme,
- ☞ necessity of linearizing inherently nonlinear relationships, and so on...

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“Researchers should cease trying to be clever in devising refinements to old methods that were developed when computational resources were limited.

*Instead, their creative instincts should be redirected to unleashing the full potential of computers for **brute force** analysis”*

D. Smith, Santa Fe 2004

⇒ Most straightforward way: Total Monte Carlo Approach !

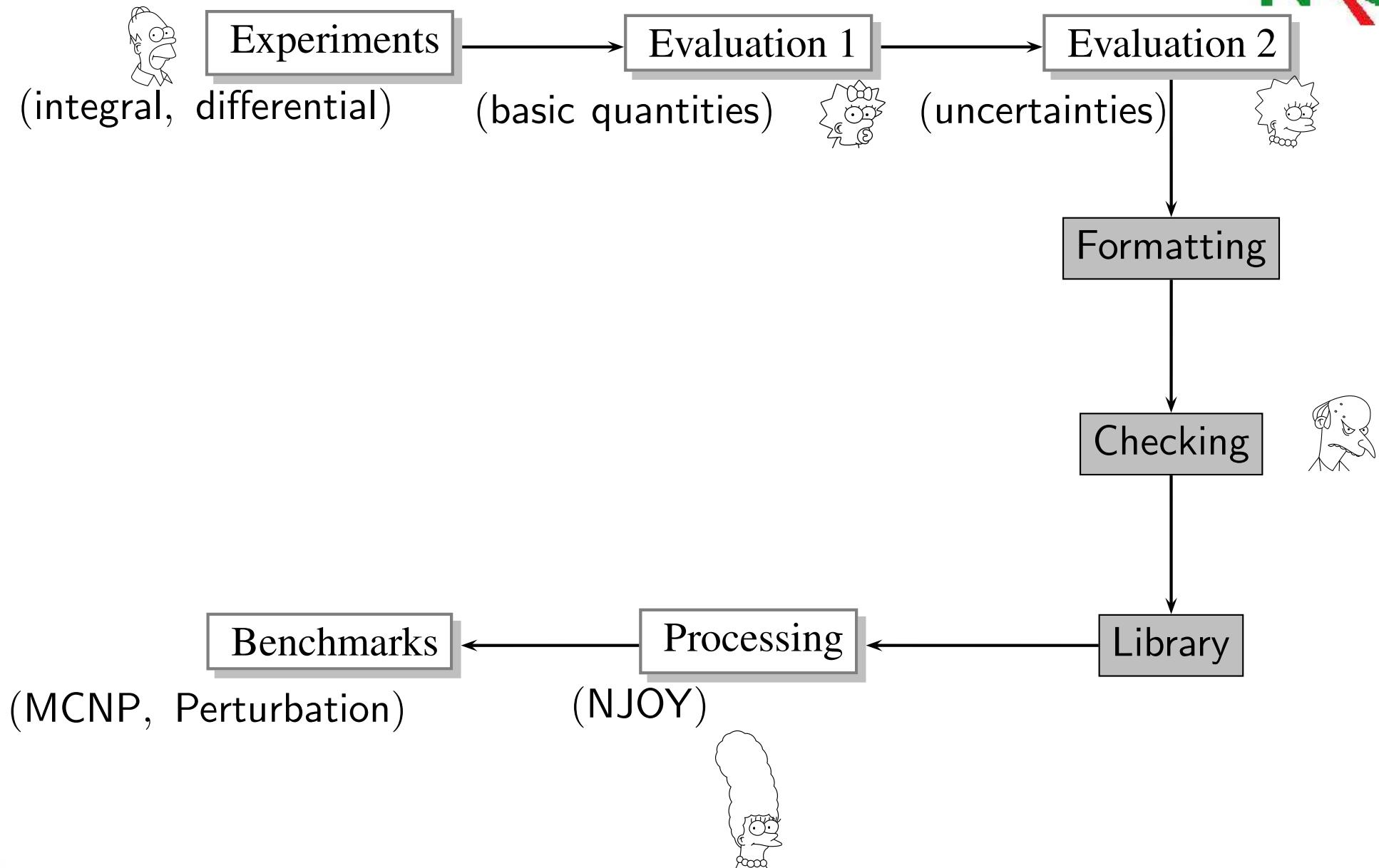
Total Monte Carlo Approach



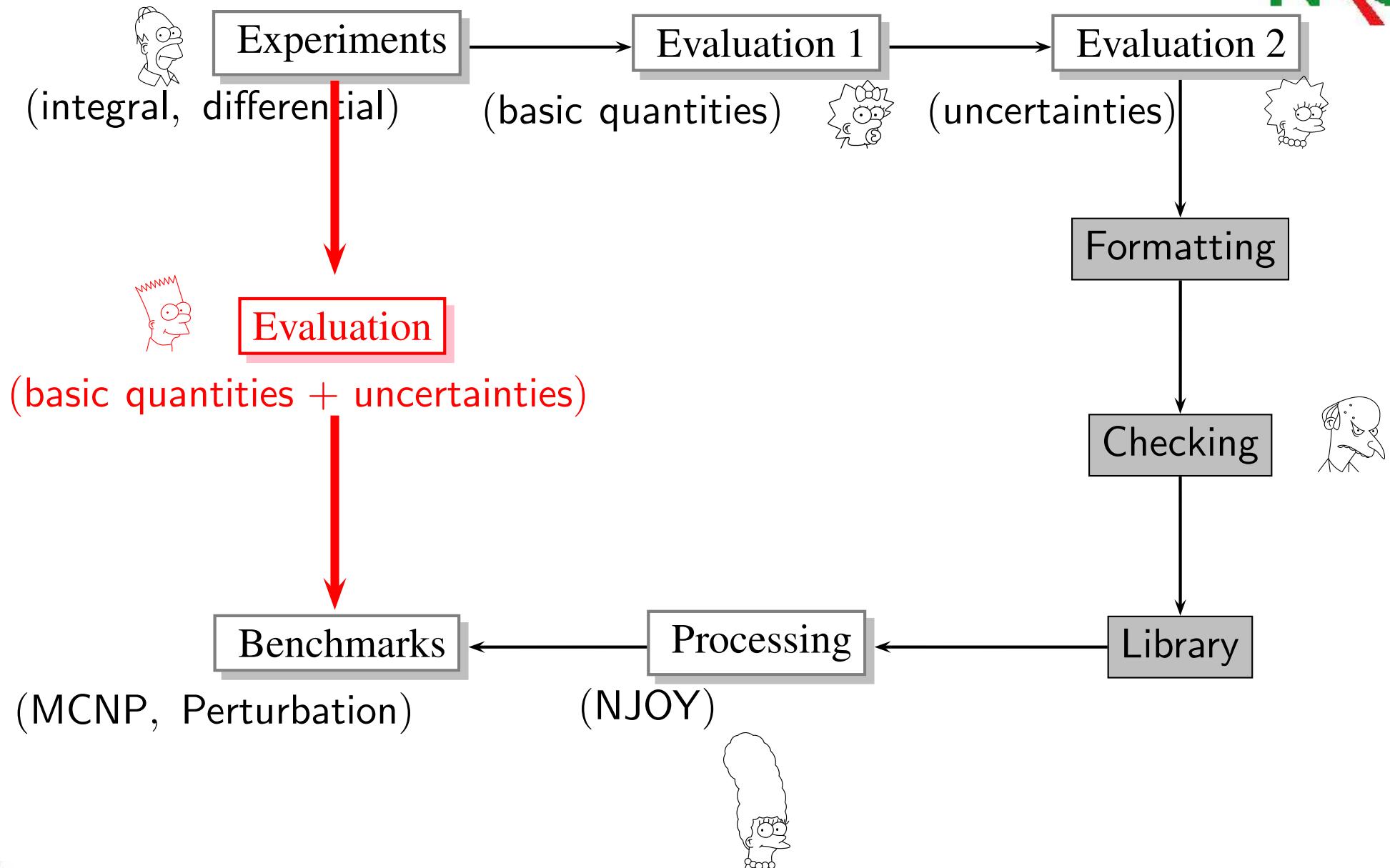
- ✍ Stable Nuclear reaction code:**TALYS**
- ✍ Talys input parameters + uncertainties
- ✍ Resonance parameters + uncertainties

Produce **5000** random,
complete ENDF-6 files per isotope

We are proposing a conceptual revolution

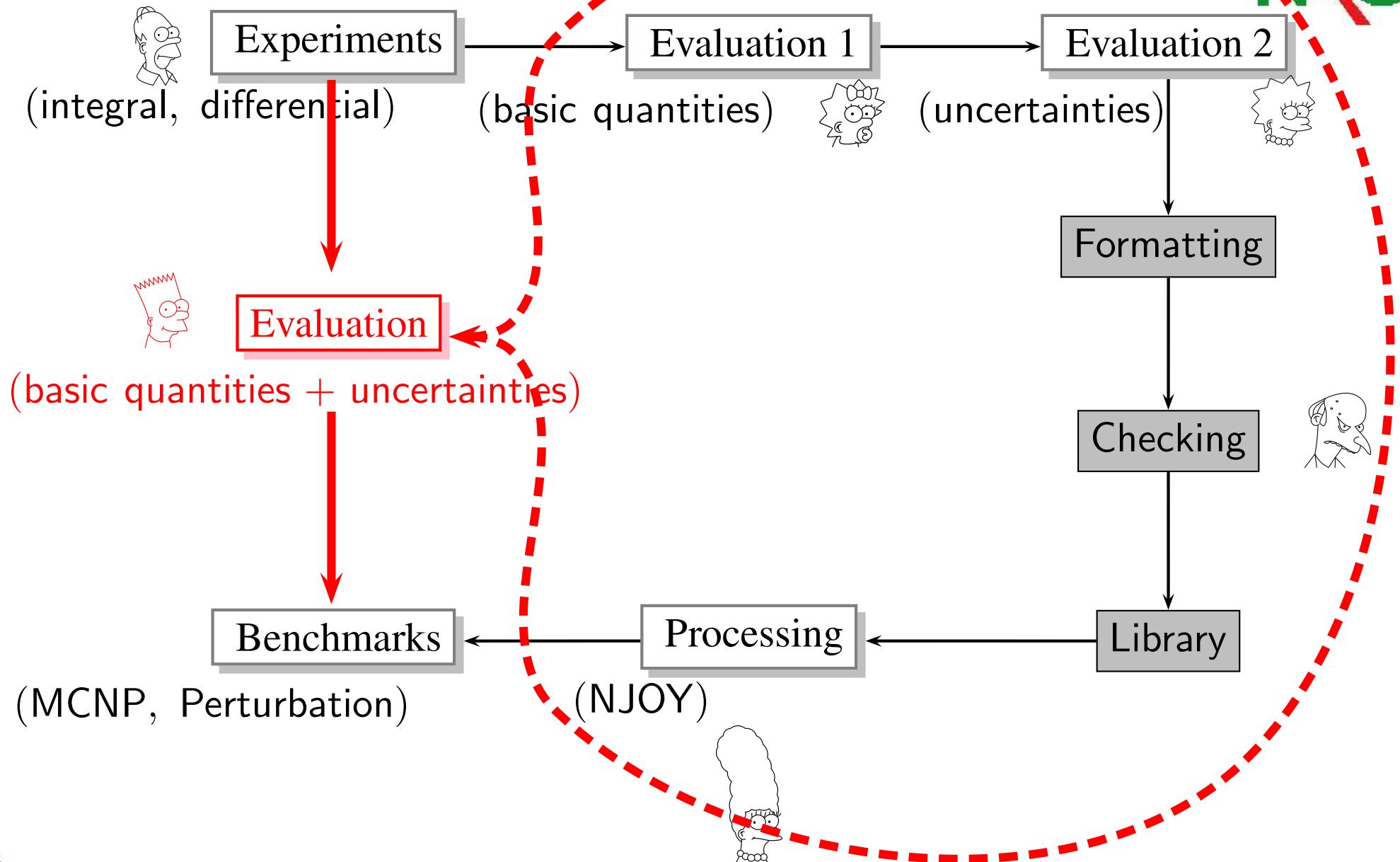


We are proposing a conceptual revolution

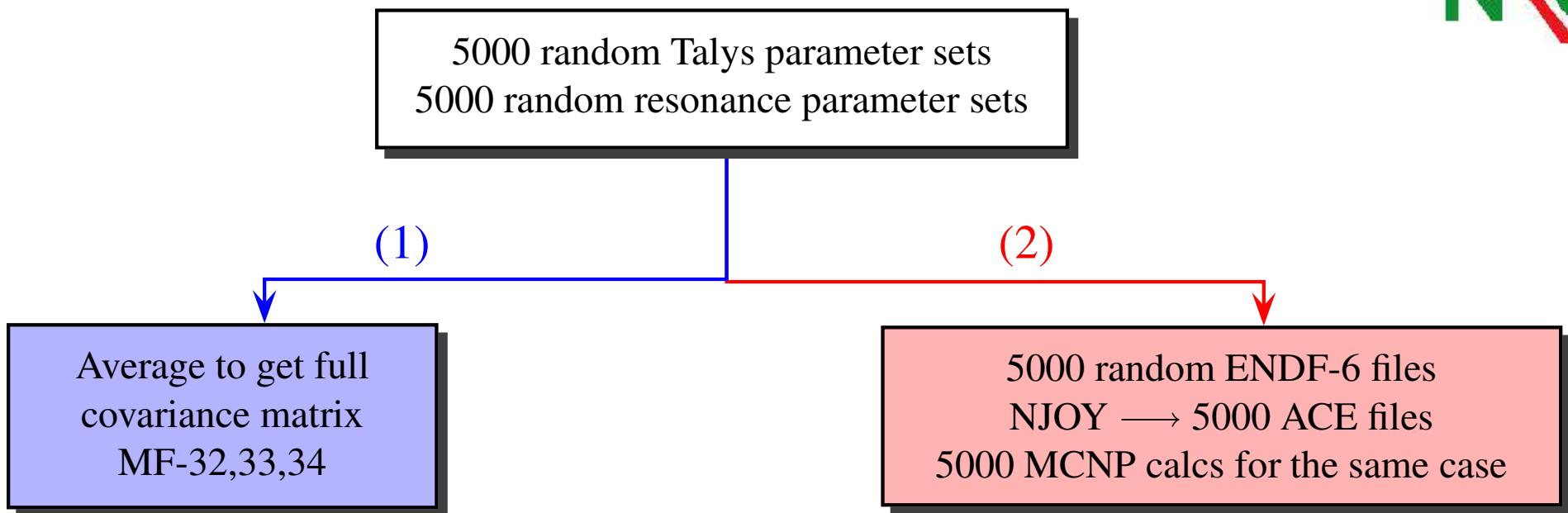


We are proposing a conceptual revolution

NRG

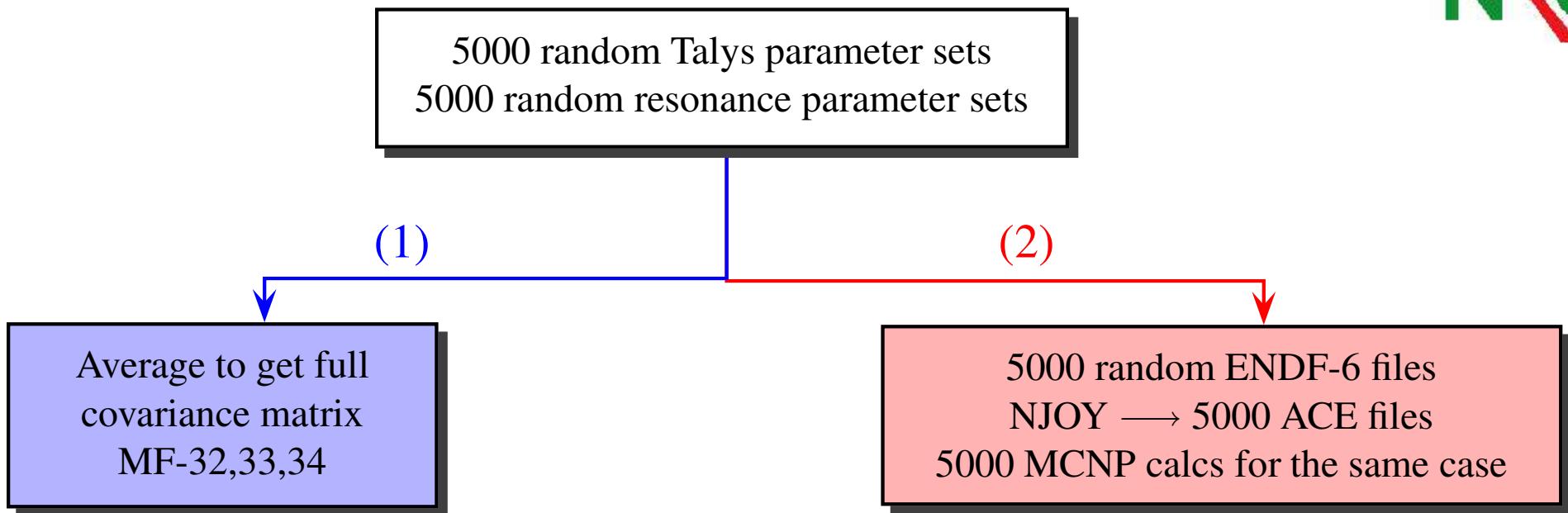


New (and most simple) path



We have both routes, but one is easier and more exact to take than the second one.

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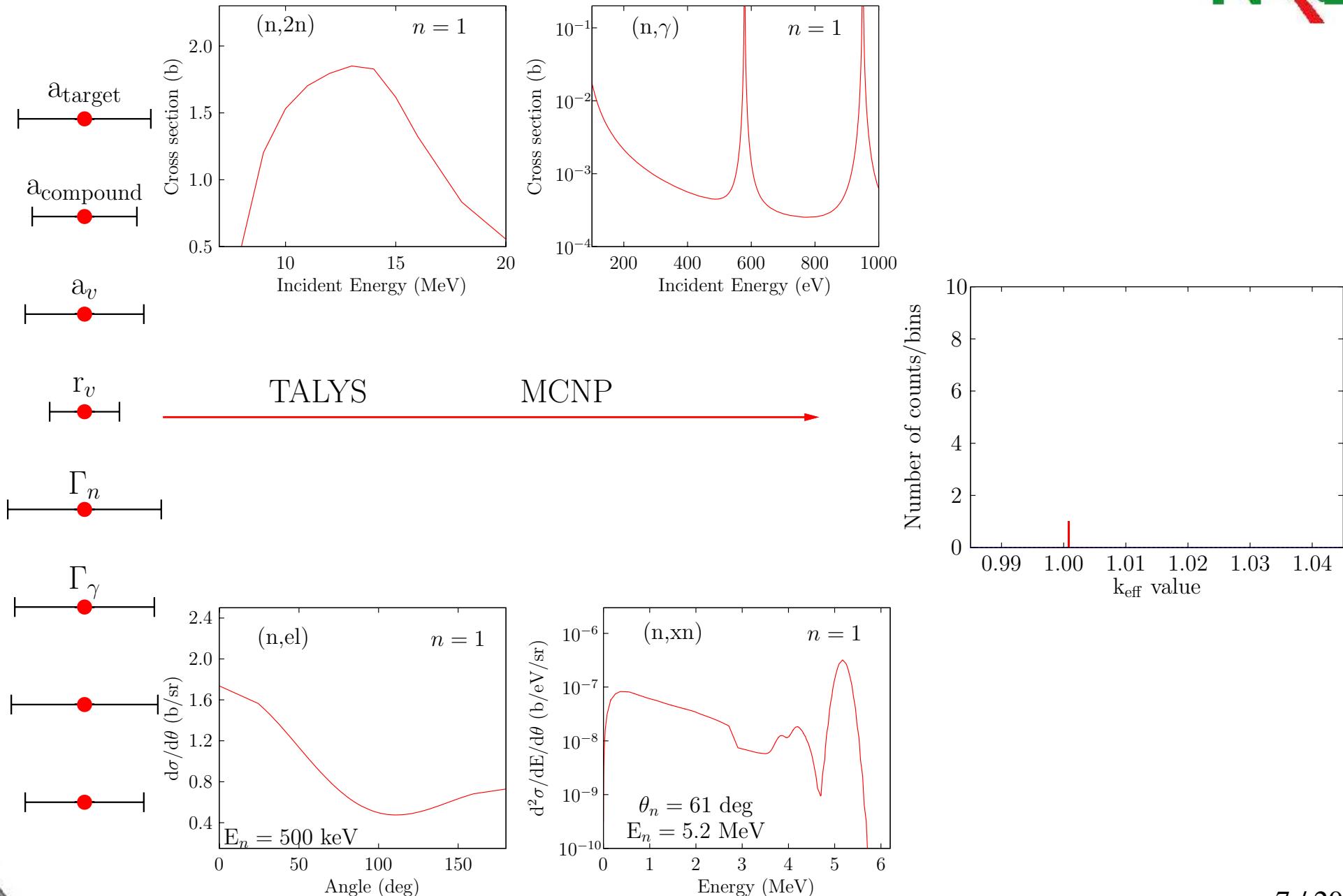
In solution (1):

Problem 1: ENDF format for covariances for fission yields, thermal scattering, branching ratios, DDX, γ -production

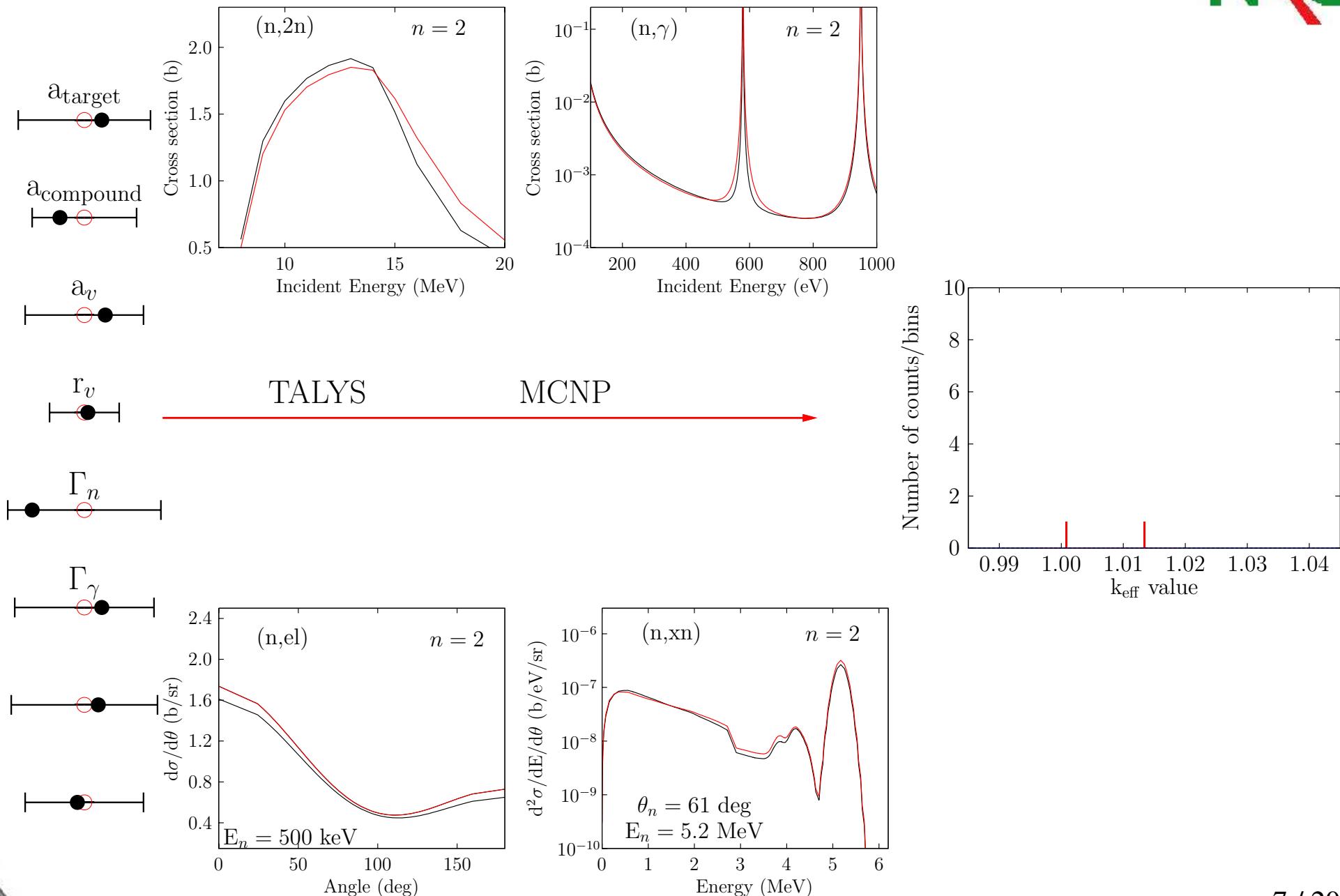
Problem 2: Processing of these covariances

Problem 3: Neutronics with covariances: perturbation codes.
Are these generally available and working?

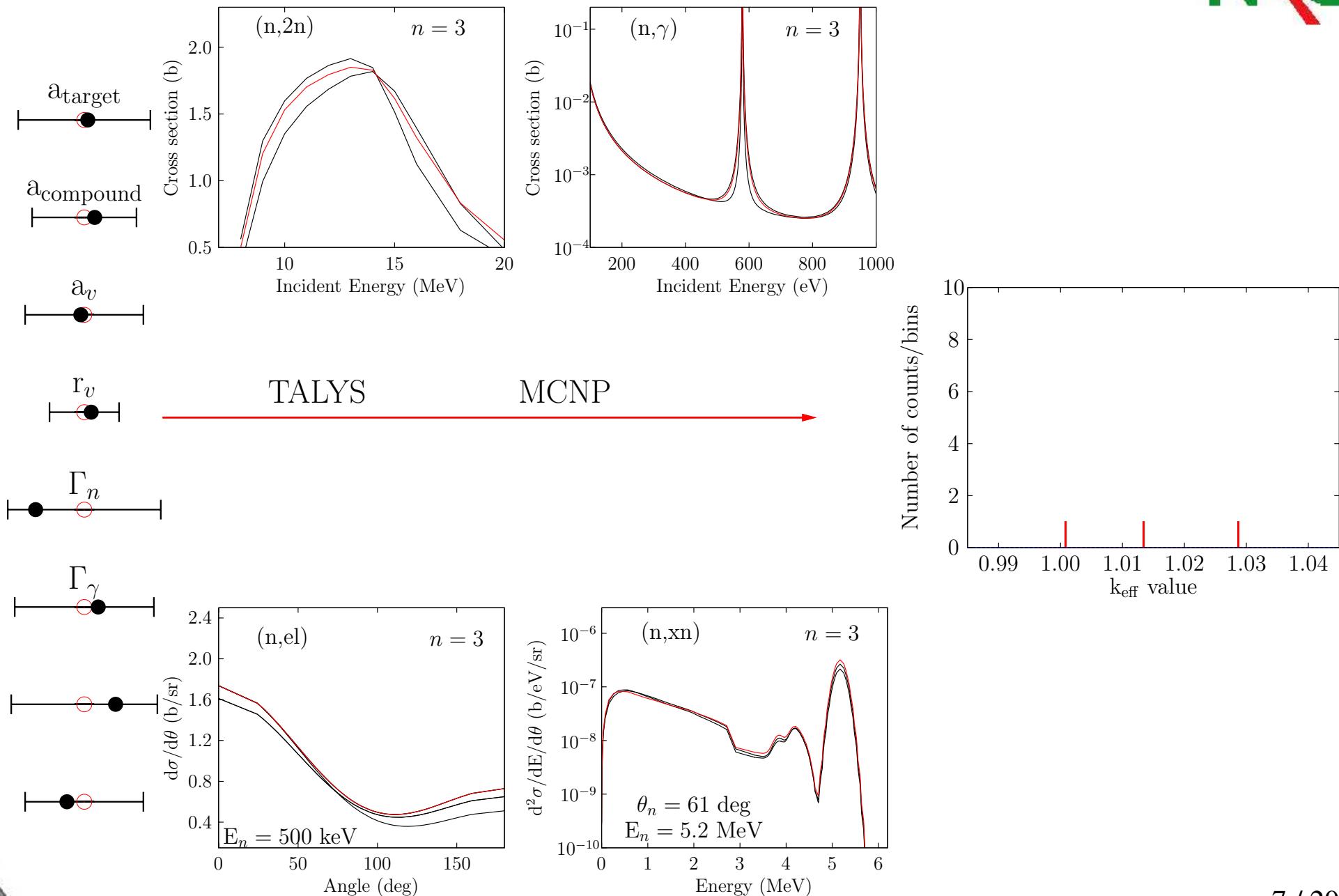
Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”

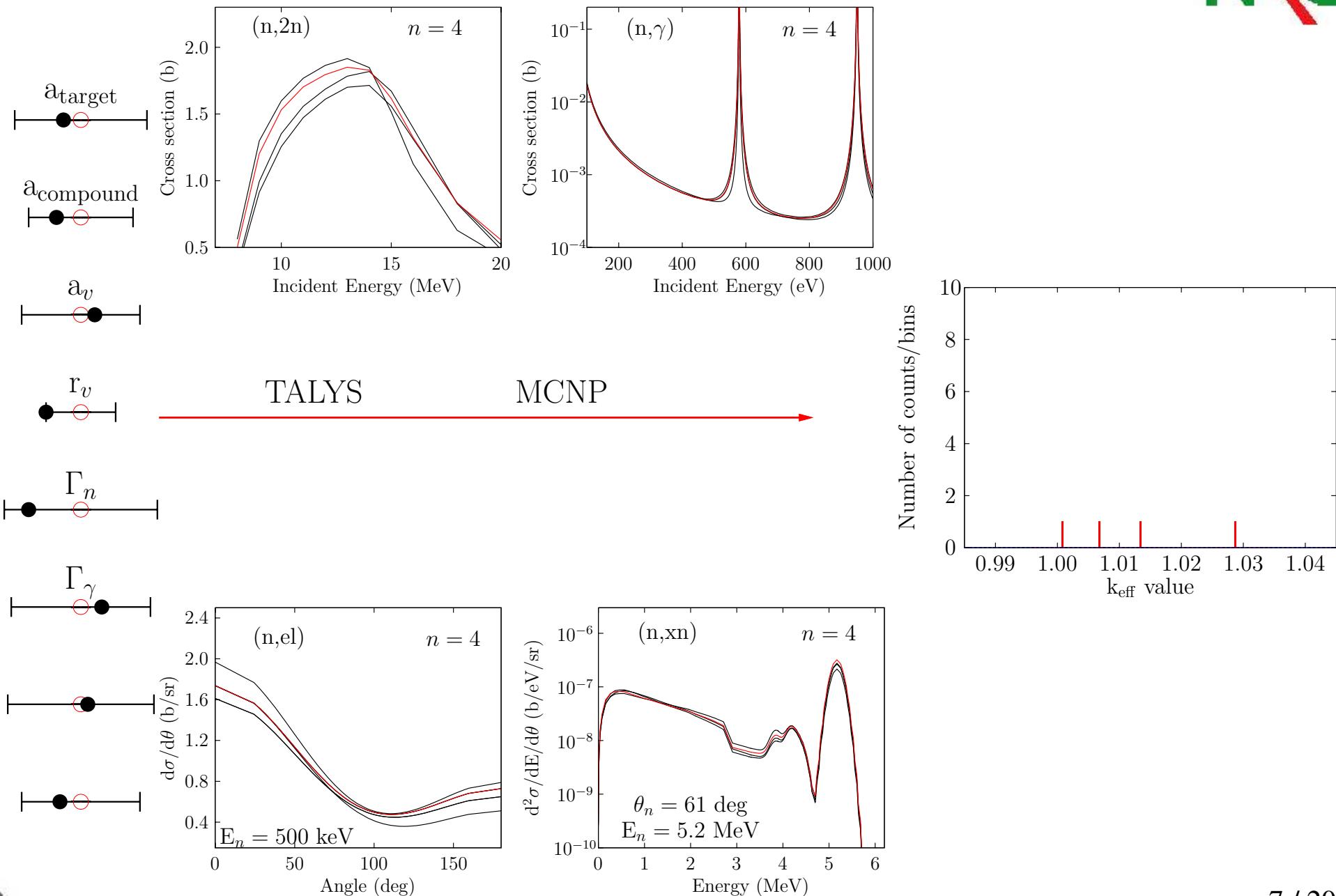
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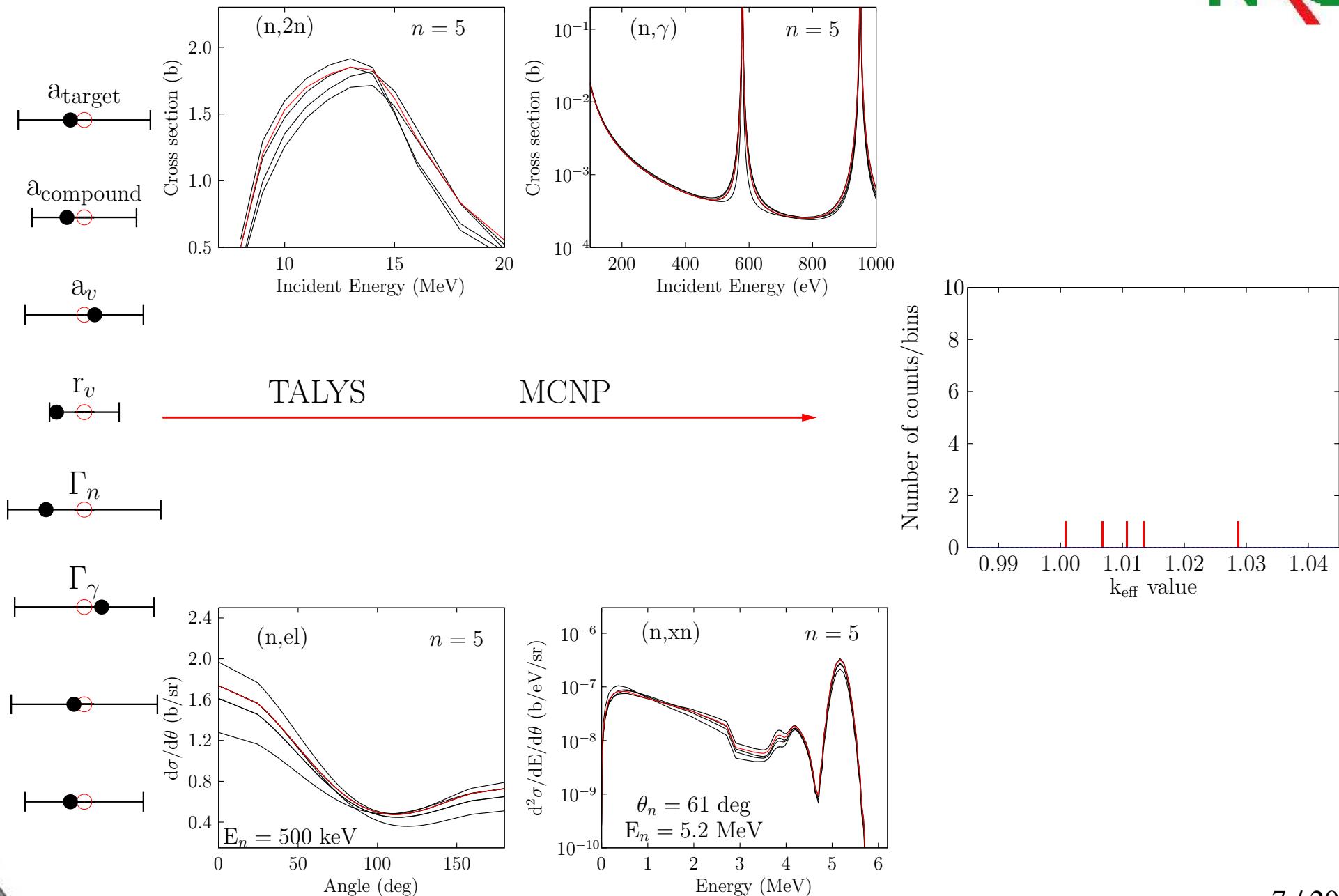
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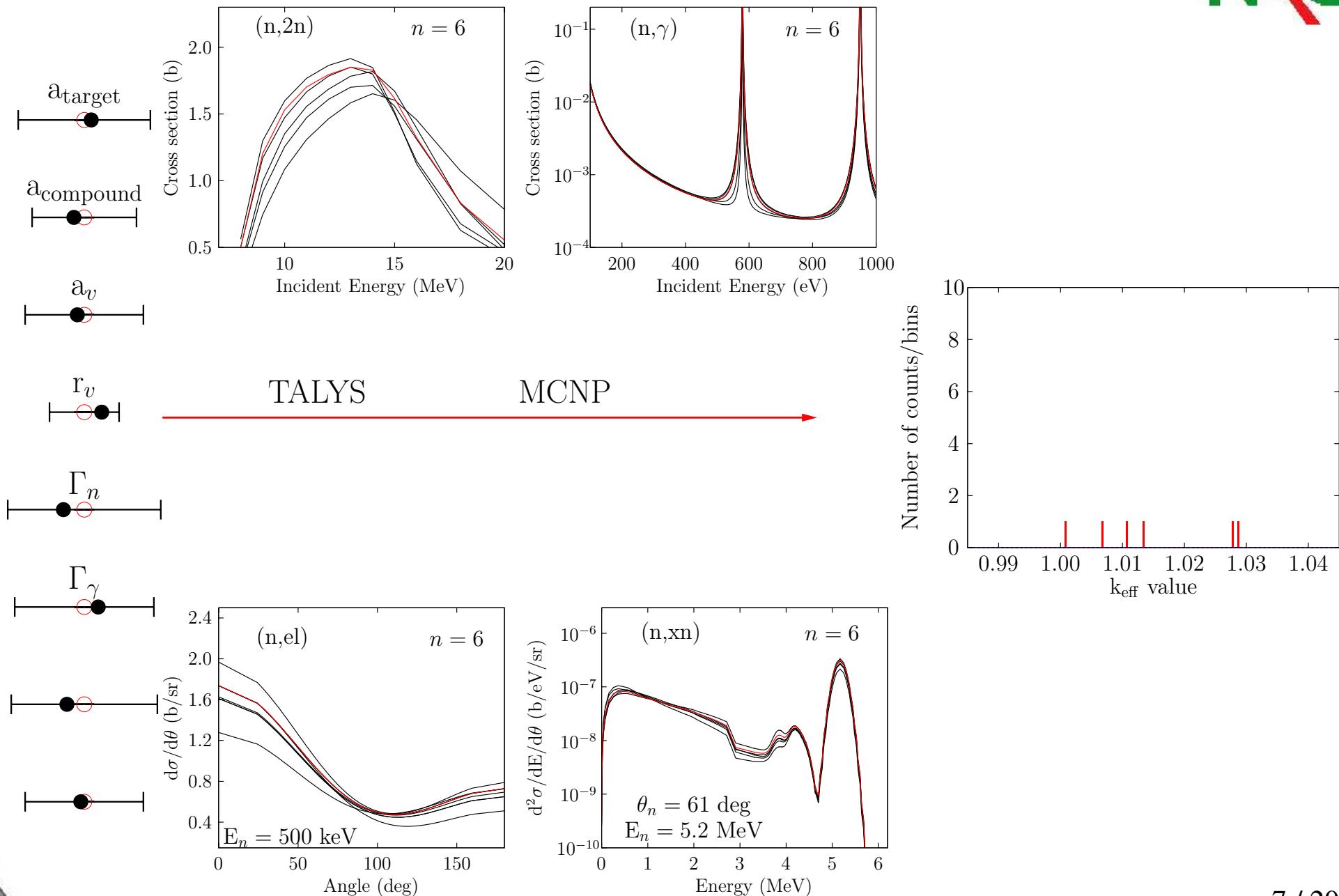
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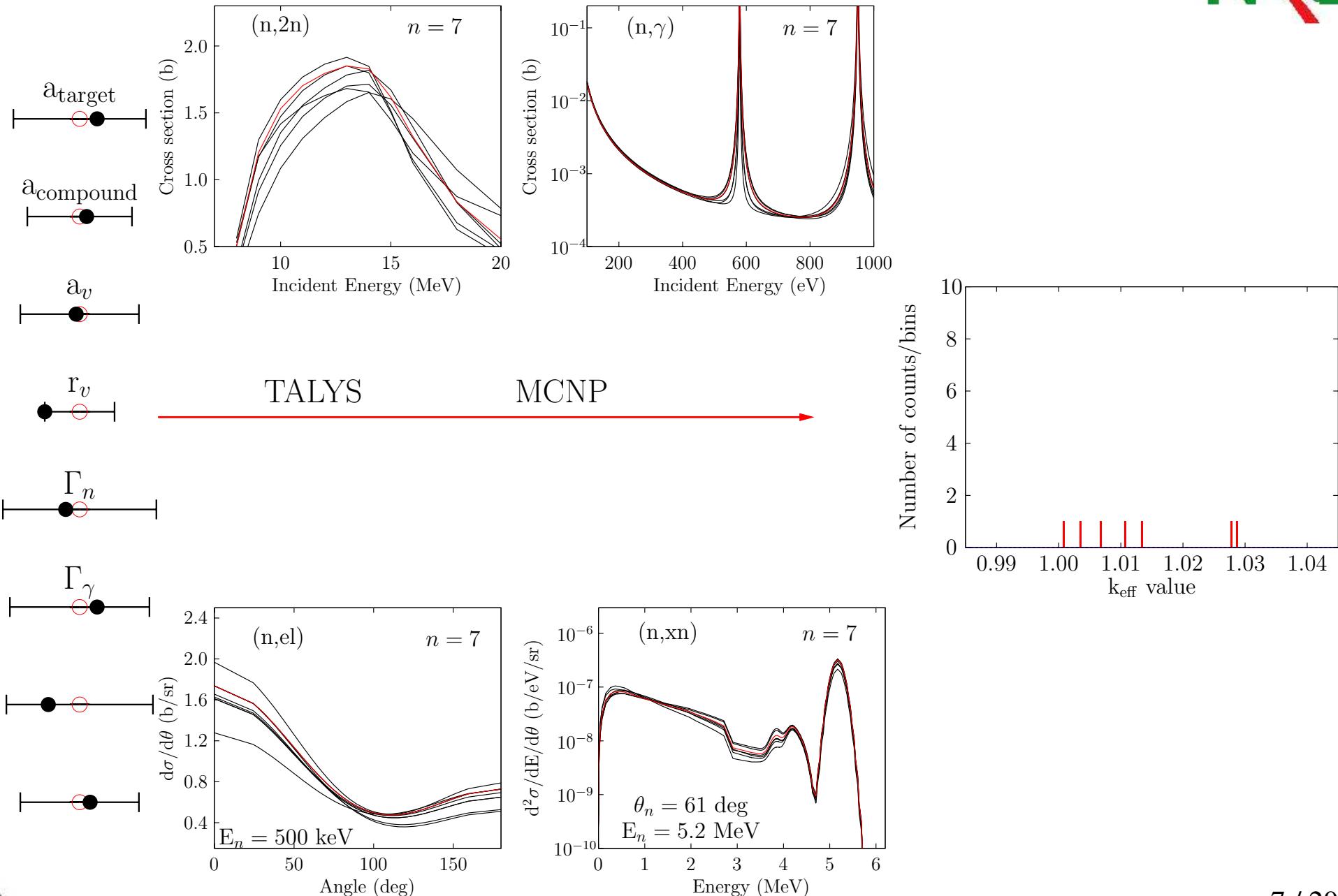
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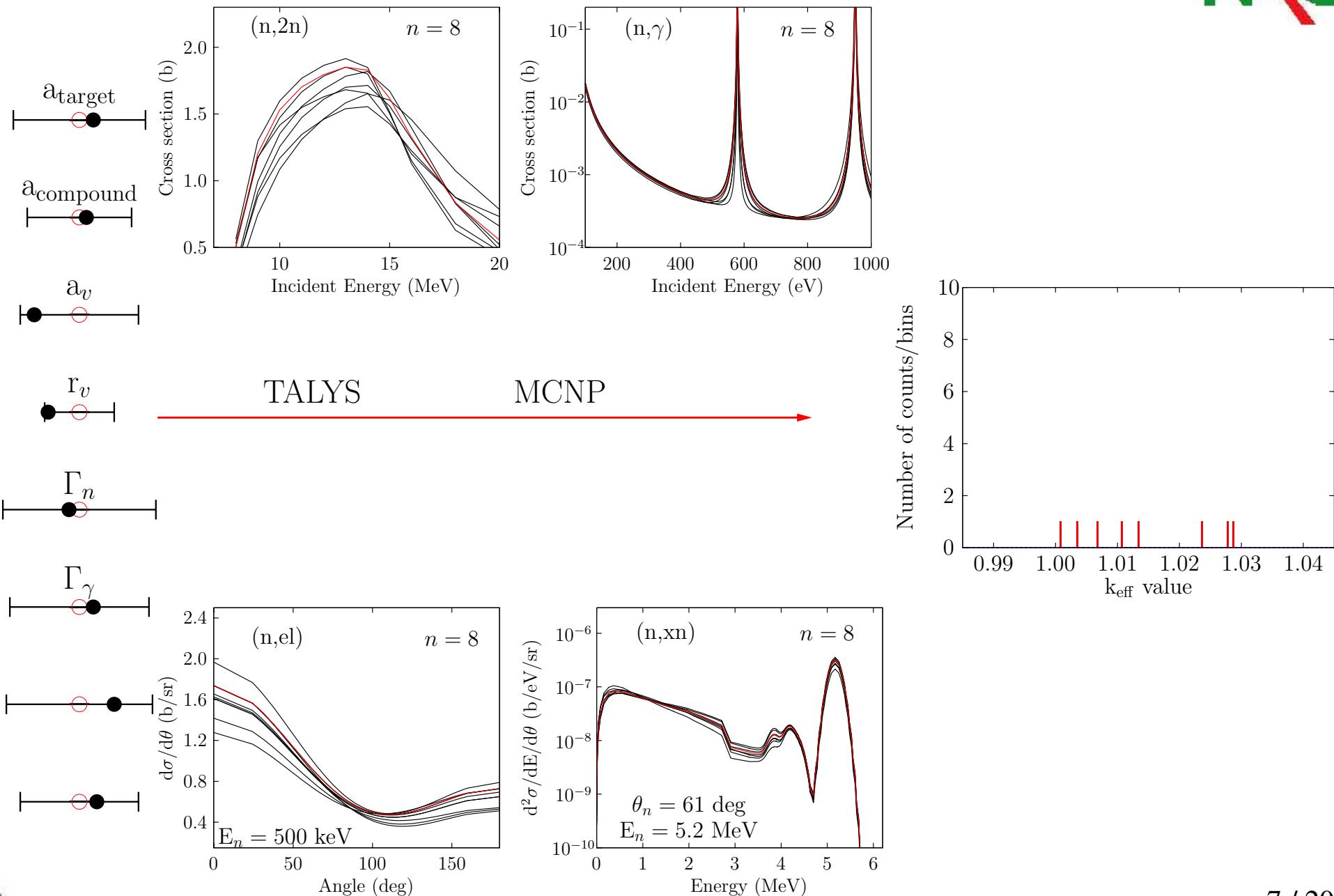
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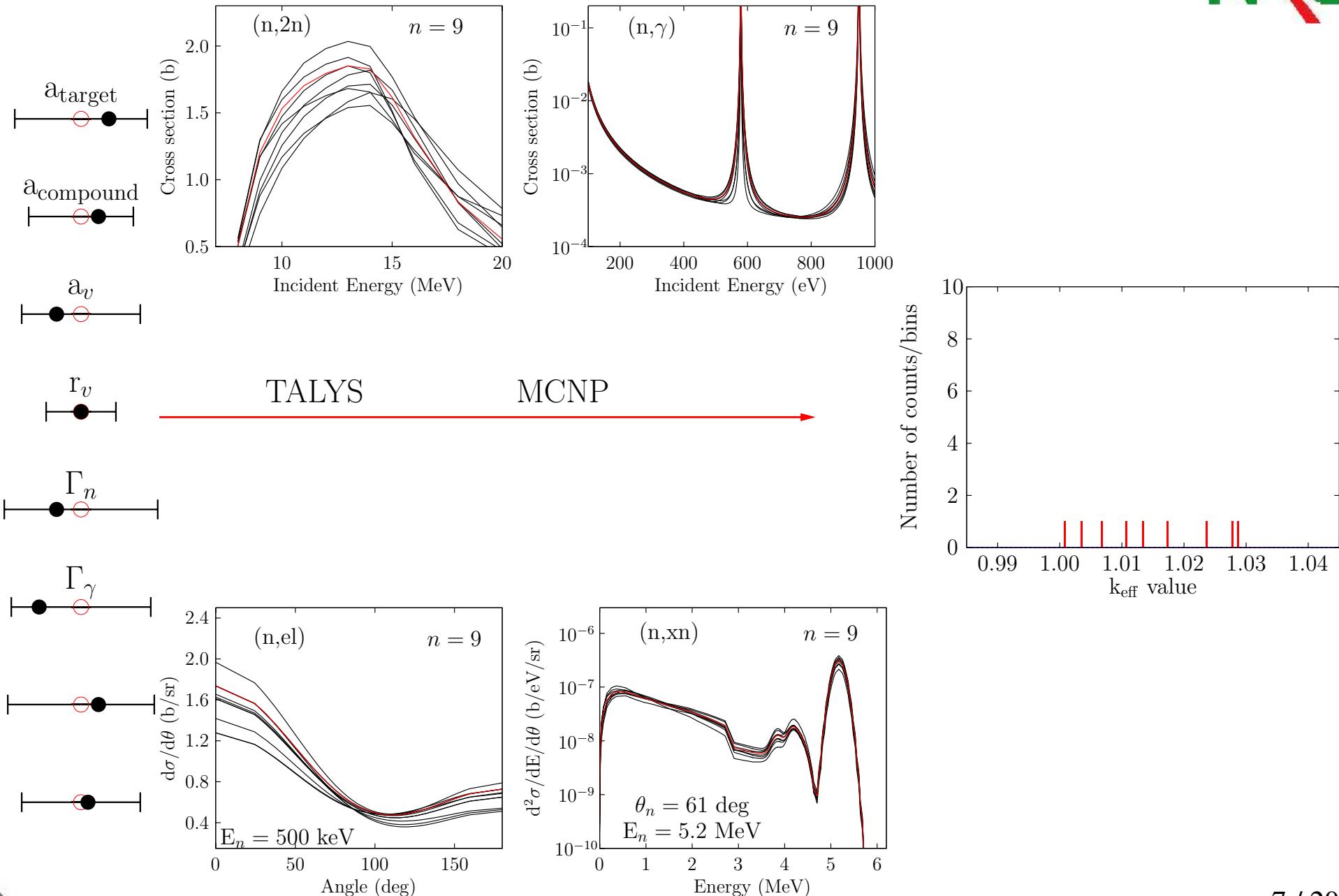
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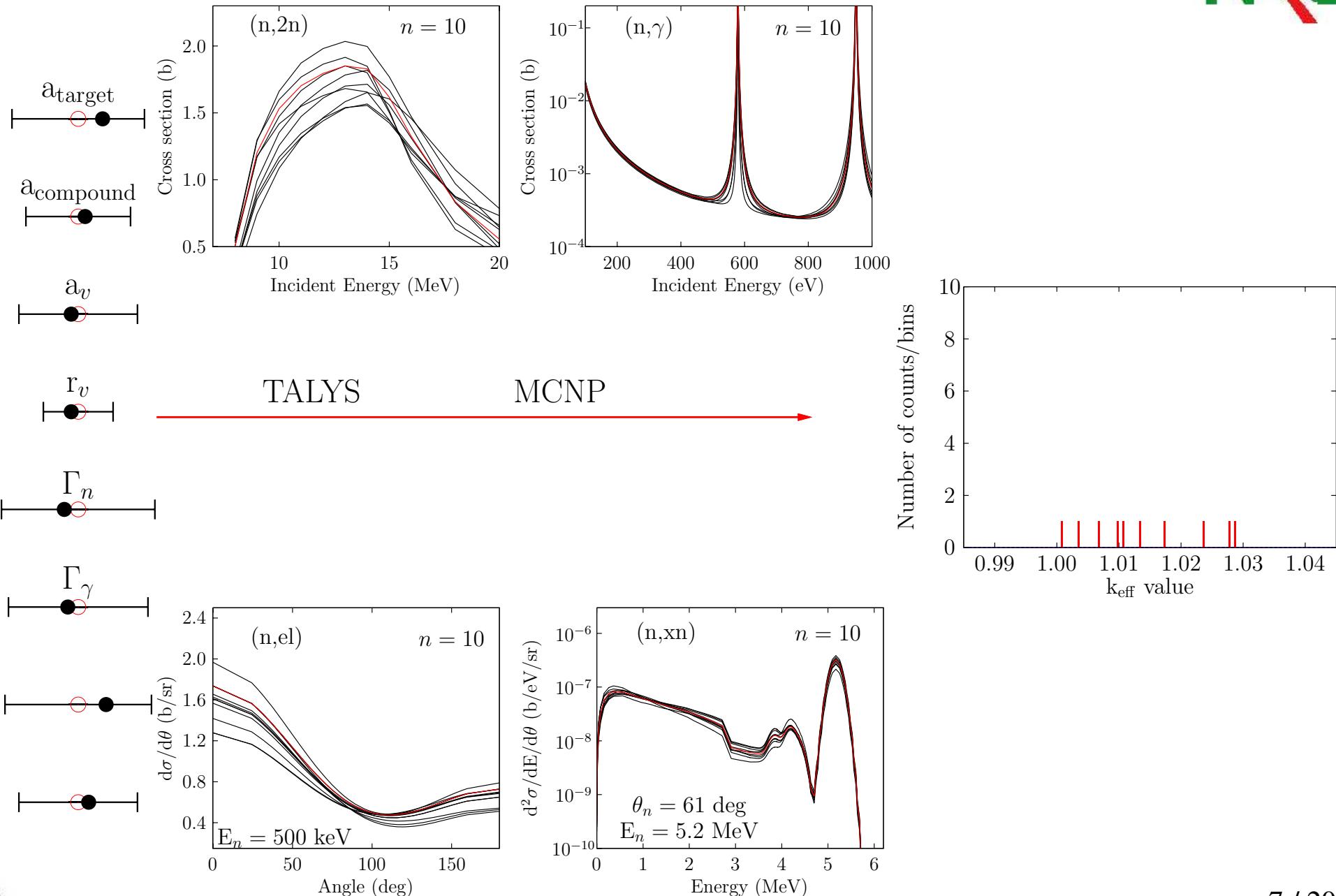
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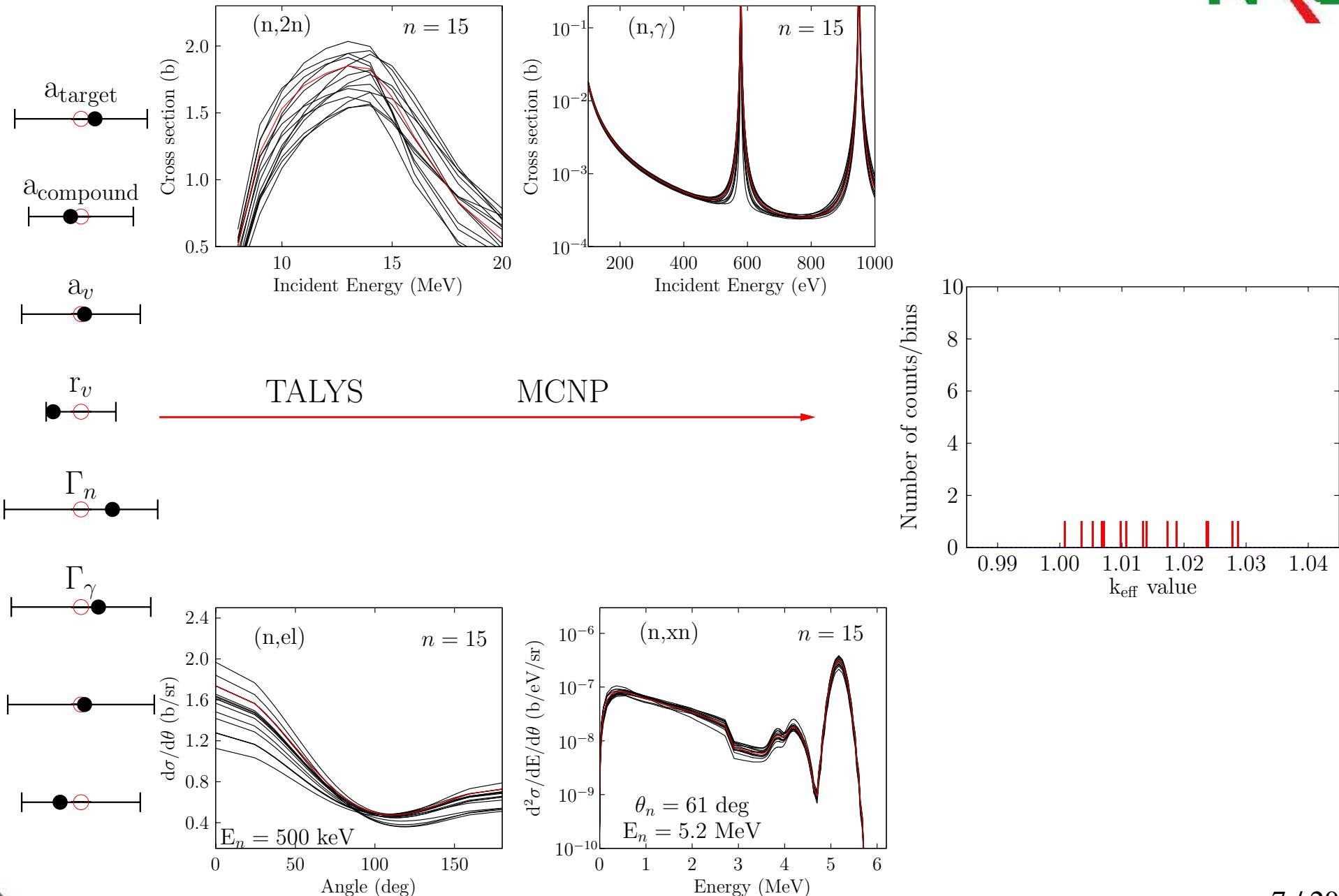
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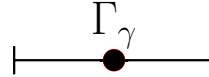
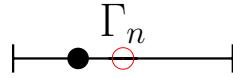
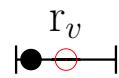
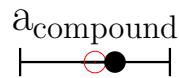
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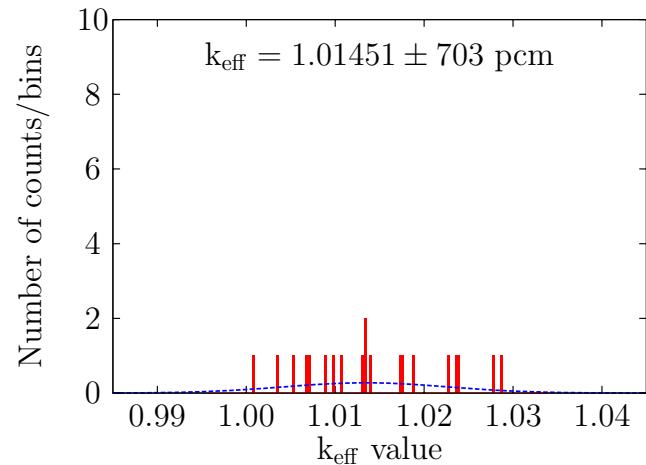
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TALYS

MCNP

$n = 20$



Hands on “ $1000 \times$ (Talys + ENDF + NJOY + MCNP) calculations”



a_{target}

a_{compound}

a_v

r_v

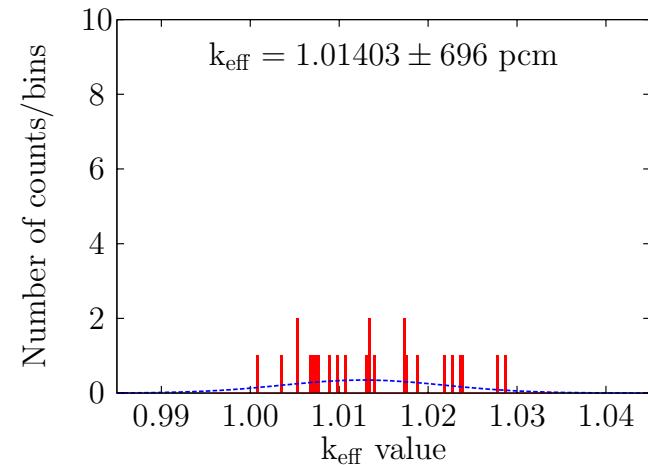
Γ_n

Γ_γ

$n = 25$

MCNP

TALYS



Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



$$a_{\text{target}}$$

$$a_{\text{compound}}$$

$$a_v$$

$$r_v$$

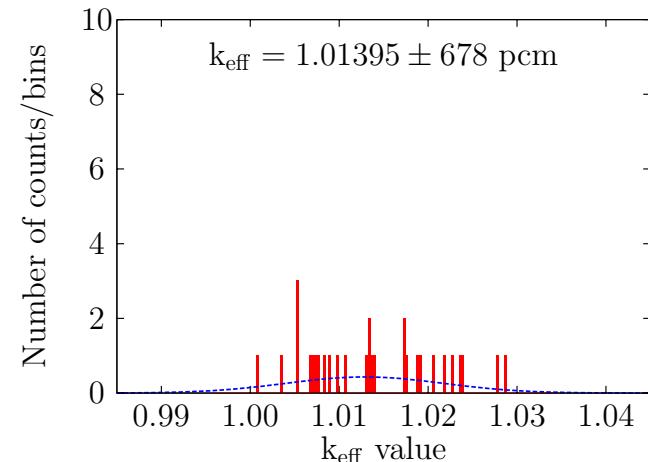
TALYS

MCNP

$$\Gamma_n$$

$$\Gamma_\gamma$$

$n = 30$



Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



$$a_{\text{target}}$$

$$a_{\text{compound}}$$

$$a_v$$

$$r_v$$

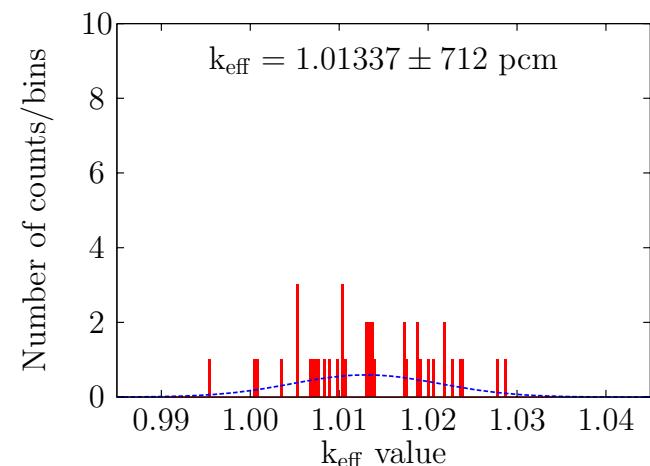
TALYS

MCNP

$$\Gamma_n$$

$$\Gamma_\gamma$$

$n = 40$



Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



$$a_{\text{target}}$$

$$a_{\text{compound}}$$

$$a_v$$

$$r_v$$

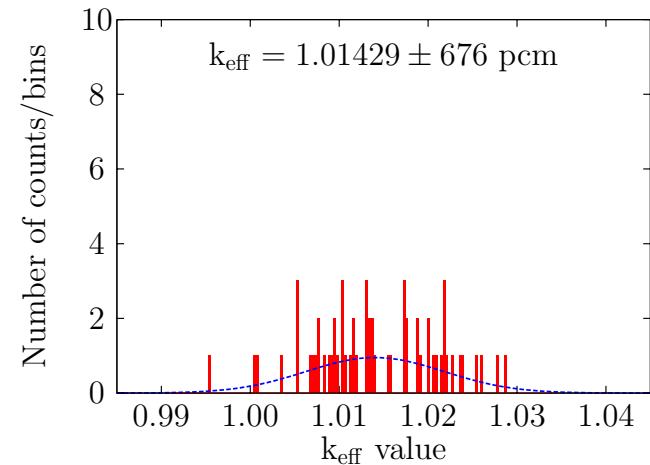
$$\Gamma_n$$

$$\Gamma_\gamma$$

TALYS

MCNP

$n = 60$



Hands on “ $1000 \times$ (Talys + ENDF + NJOY + MCNP) calculations”



$$a_{\text{target}}$$

$$a_{\text{compound}}$$

$$a_v$$

$$r_v$$

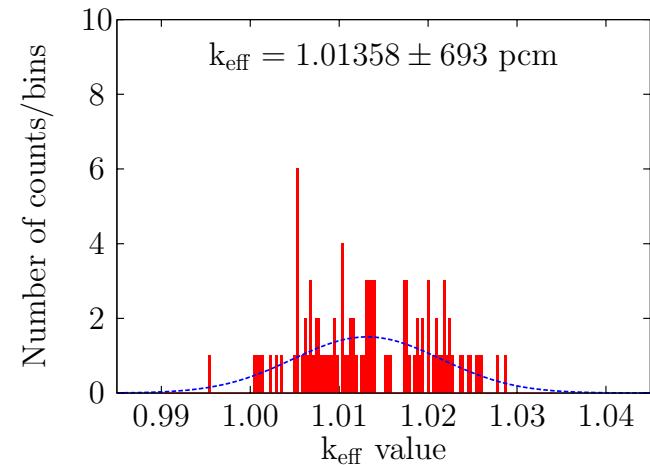
$$\Gamma_n$$

$$\Gamma_\gamma$$

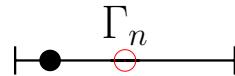
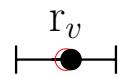
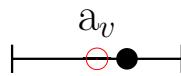
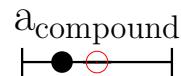
TALYS

MCNP

$n = 100$



Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”

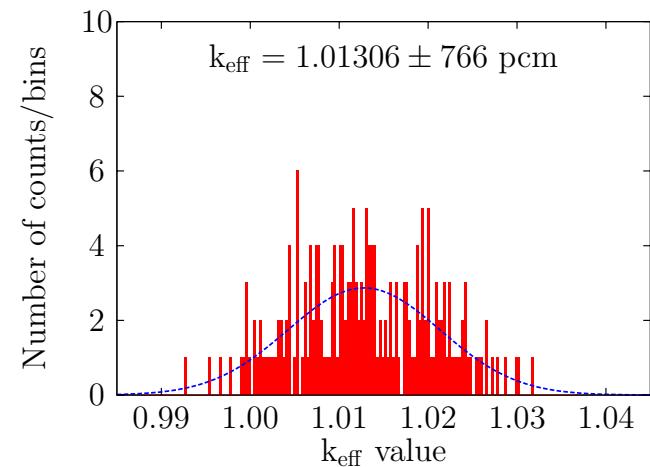


TALYS

MCNP



$n = 200$



Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



$$a_{\text{target}}$$

$$a_{\text{compound}}$$

$$a_v$$

$$r_v$$

$$\Gamma_n$$

$$\Gamma_\gamma$$

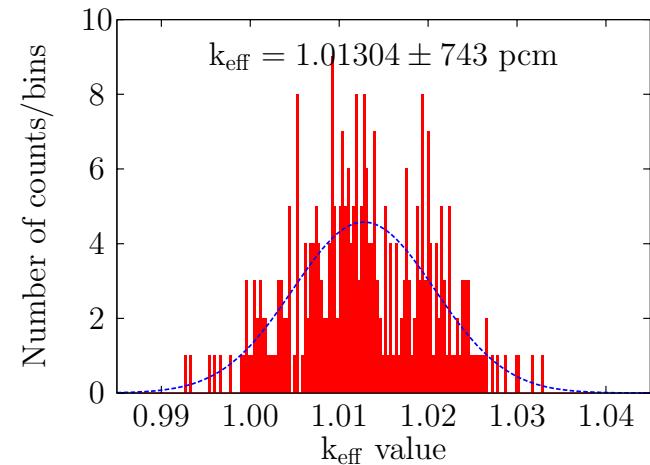
$$\dots$$

$$\dots$$

TALYS

MCNP

$n = 300$



Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



$$a_{\text{target}}$$

$$a_{\text{compound}}$$

$$a_v$$

$$r_v$$

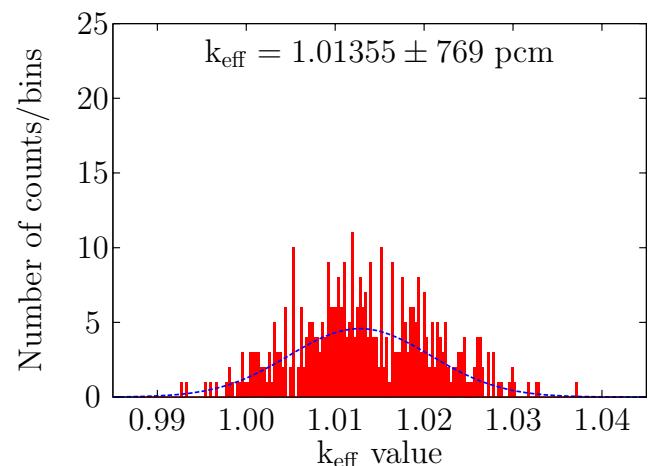
$$\Gamma_n$$

$$\Gamma_\gamma$$

TALYS

MCNP

$n = 400$



Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



a_{target}

a_{compound}

a_v

r_v

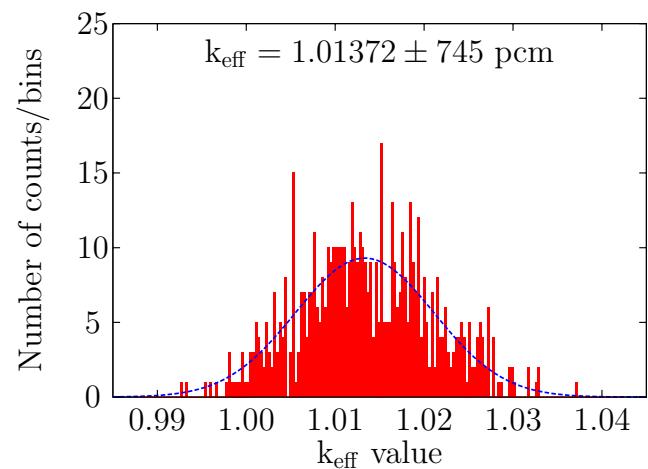
Γ_n

Γ_γ

TALYS

MCNP

$n = 600$



Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



$$a_{\text{target}}$$

$$a_{\text{compound}}$$

$$a_v$$

$$r_v$$

$$\Gamma_n$$

$$\Gamma_\gamma$$

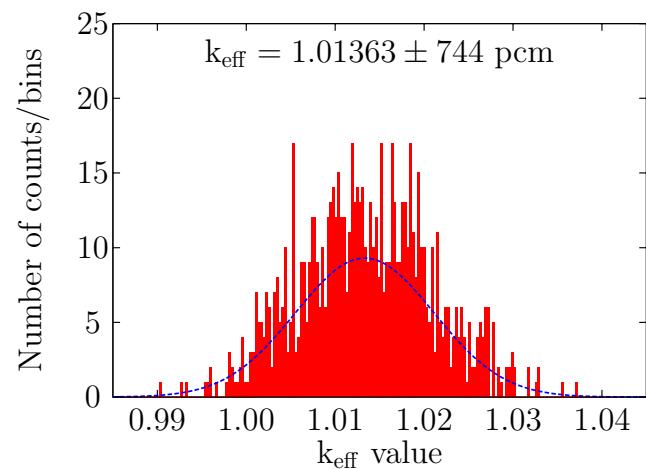
$$\dots$$

$$\dots$$

TALYS

MCNP

$n = 800$



Hands on “ $1000 \times (\text{Talys} + \text{ENDF} + \text{NJOY} + \text{MCNP})$ calculations”



a_{target}

a_{compound}

a_v

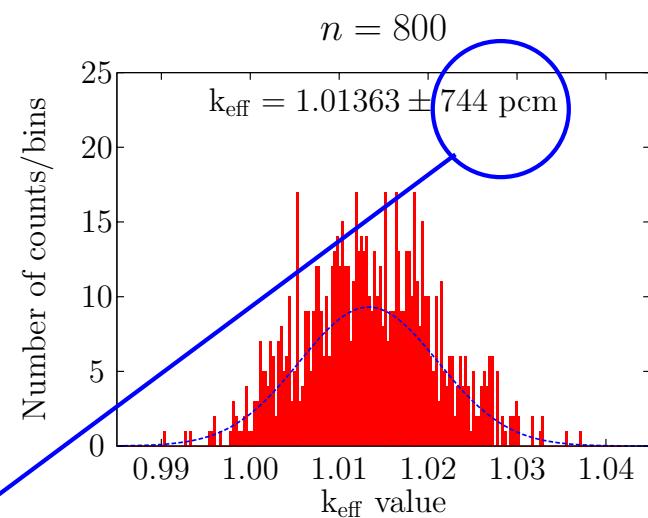
r_v

Γ_n

Γ_γ

TALYS

MCNP



Statistical uncertainty $\simeq 68 \text{ pcm}$

\Rightarrow uncertainty due to nuclear data $\simeq 740 \text{ pcm}$

Where can we apply it and examples with Pb isotopes



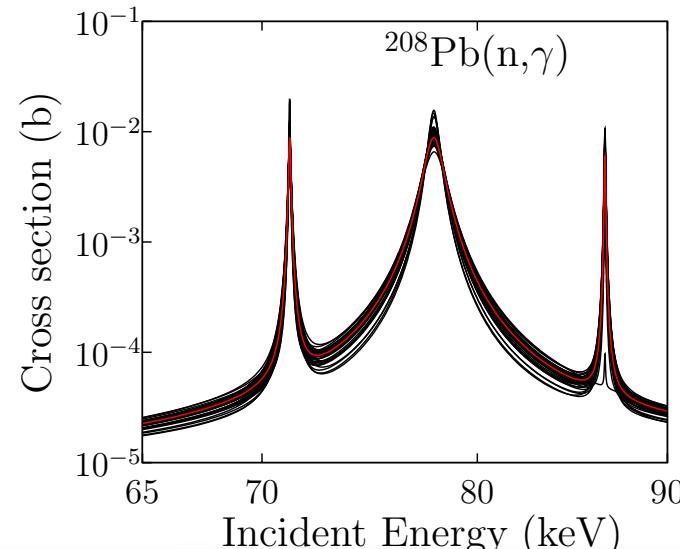
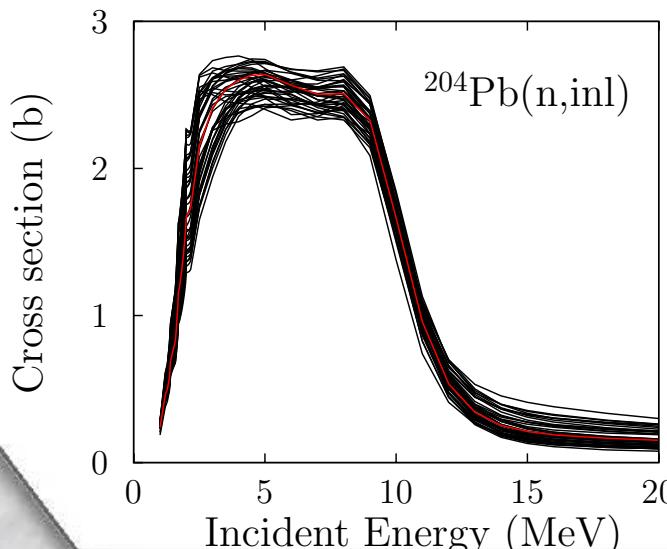
- ☞ Monte Carlo codes (MCNP, Tripoli), Deterministic codes (APOLLO, WIMS)
 - ☞ Quantities: criticality, flux (+ all from SG-26), shielding and fusion
-

Where can we apply it and examples with Pb isotopes

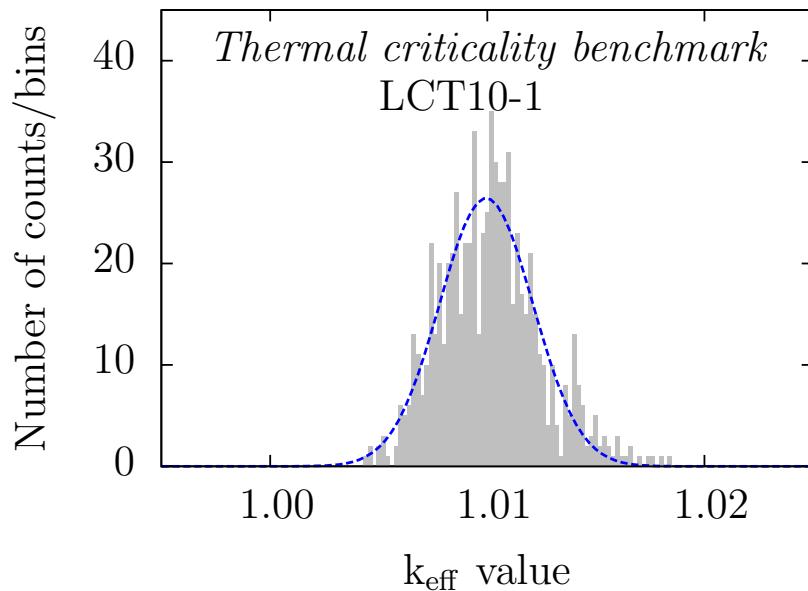


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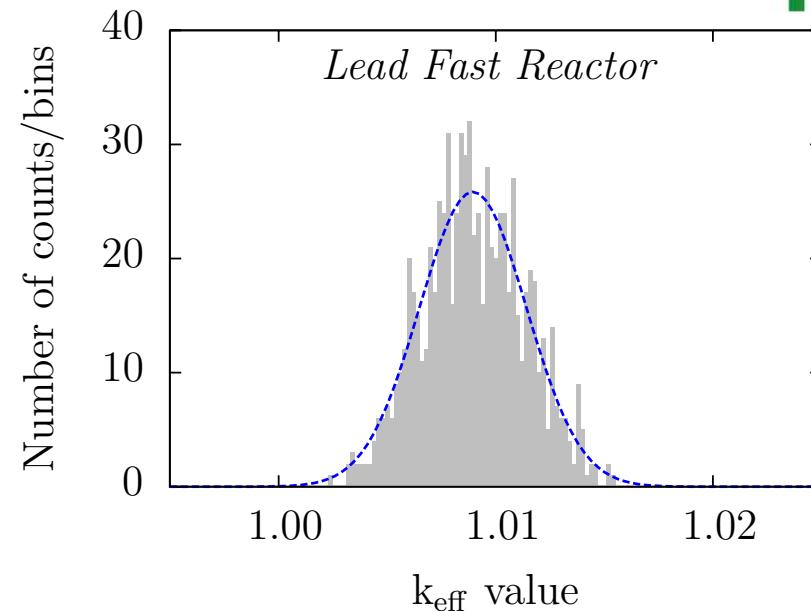
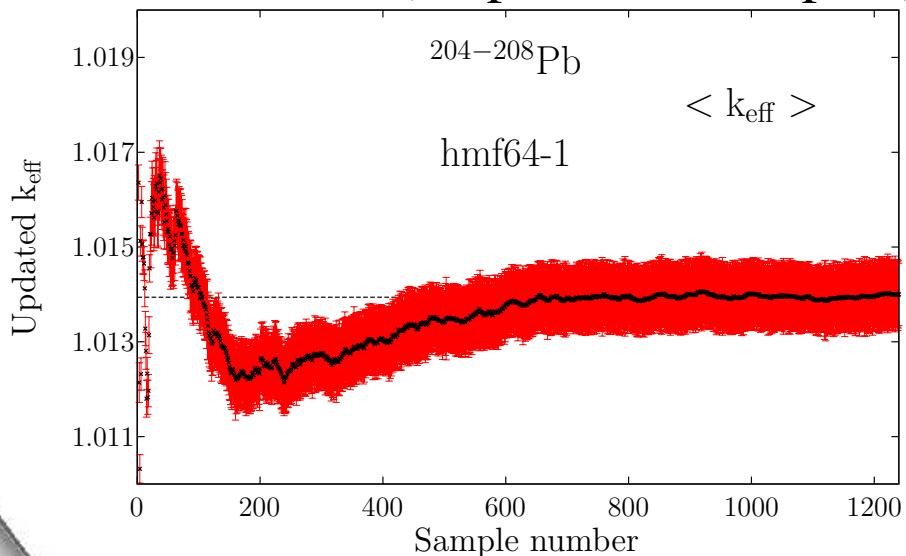
-
- * $^{204-208}\text{Pb}$ evaluations (NIM A589 (2008) 85) + **5000** random ENDF files
 - * Applied on k_{eff} and β_{eff} for criticality benchmarks (LCT-10 and HMF-64) and to ADS and LFR



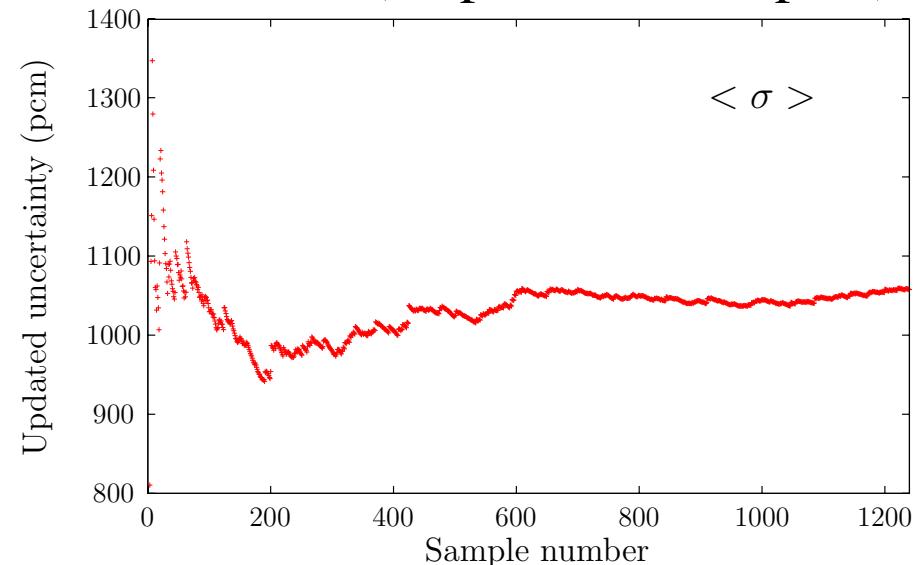
Examples with Pb isotopes



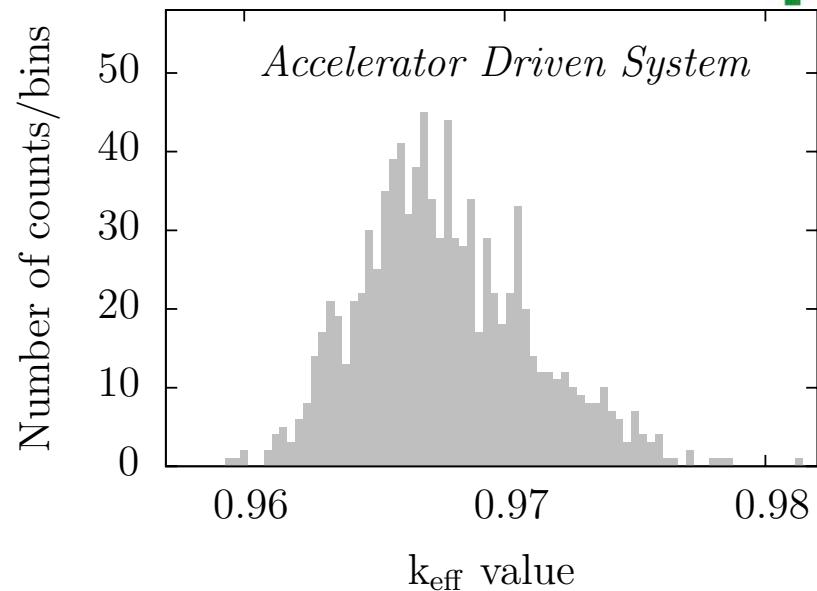
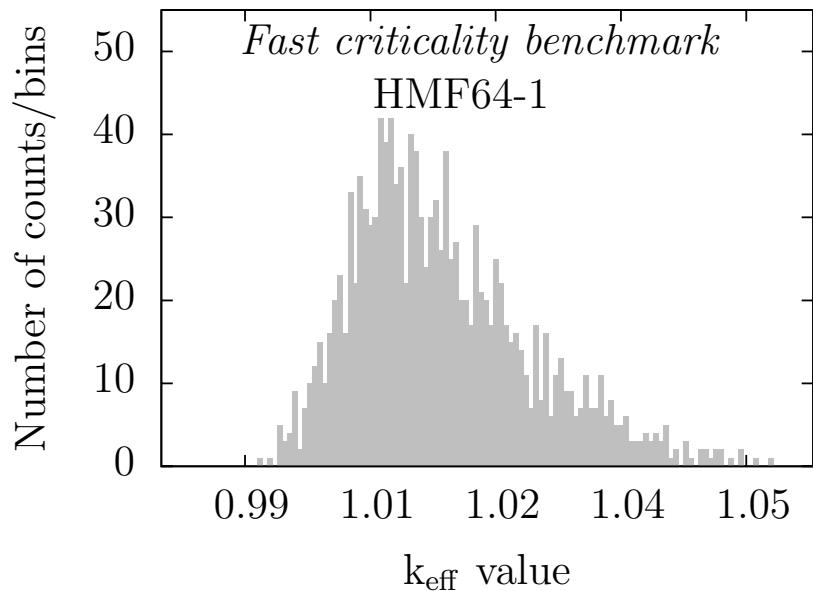
$$k_{\text{eff}} = 1.01028 \pm (60 \text{ pcm and } 212 \text{ pcm})$$



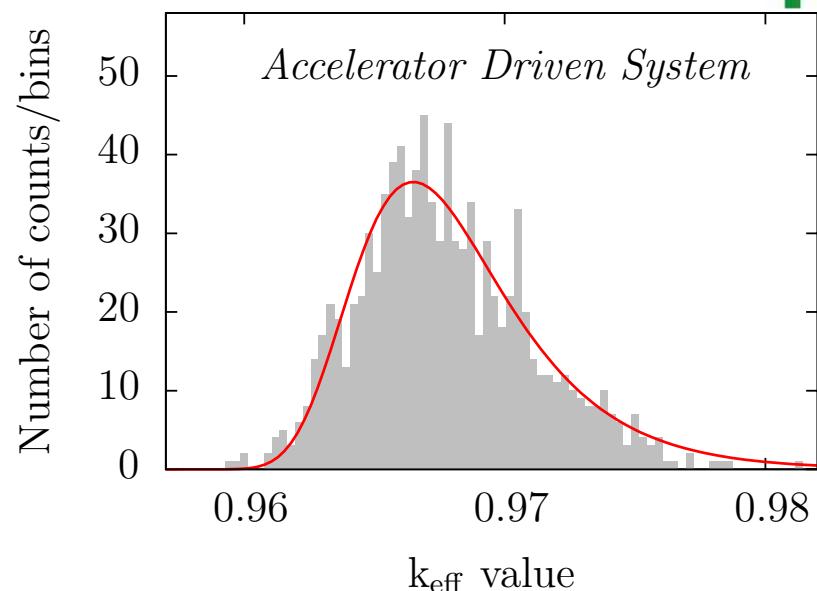
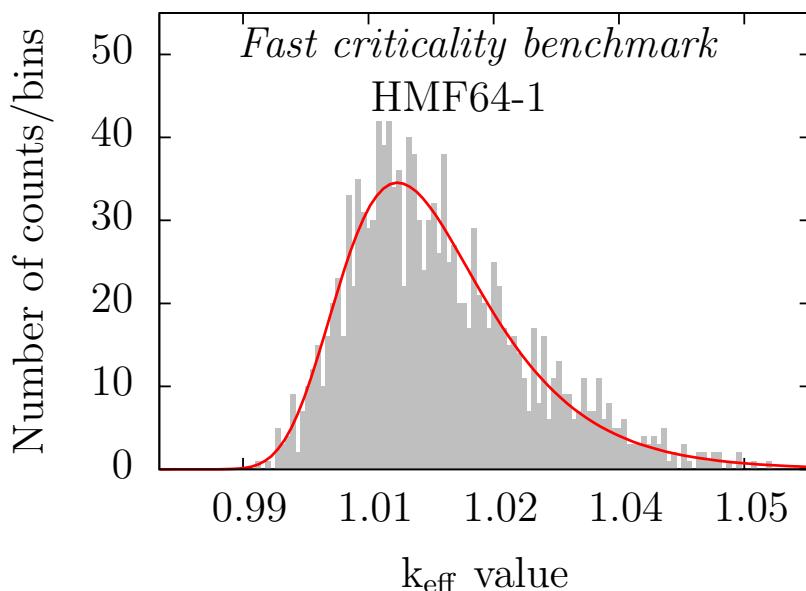
$$k_{\text{eff}} = 1.00894 \pm (60 \text{ pcm and } 240 \text{ pcm})$$



Examples with Pb isotopes



Examples with Pb isotopes

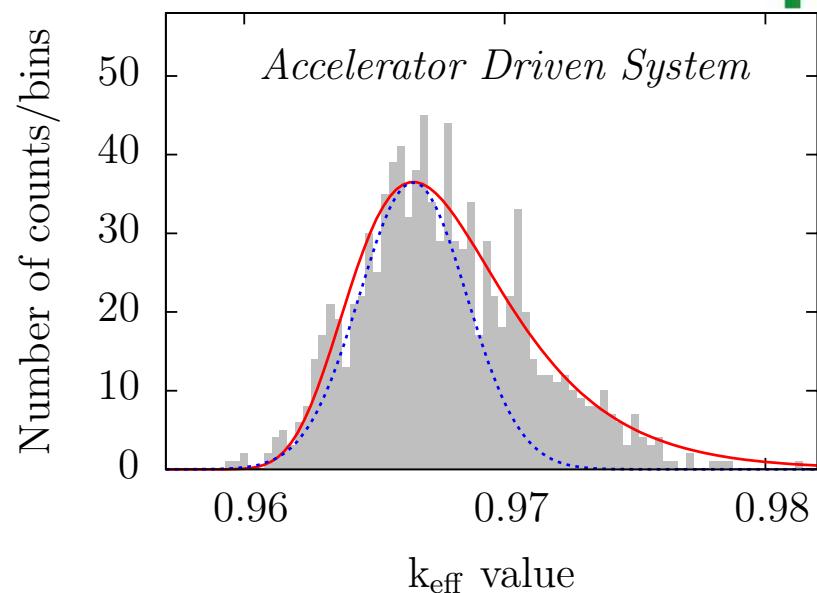
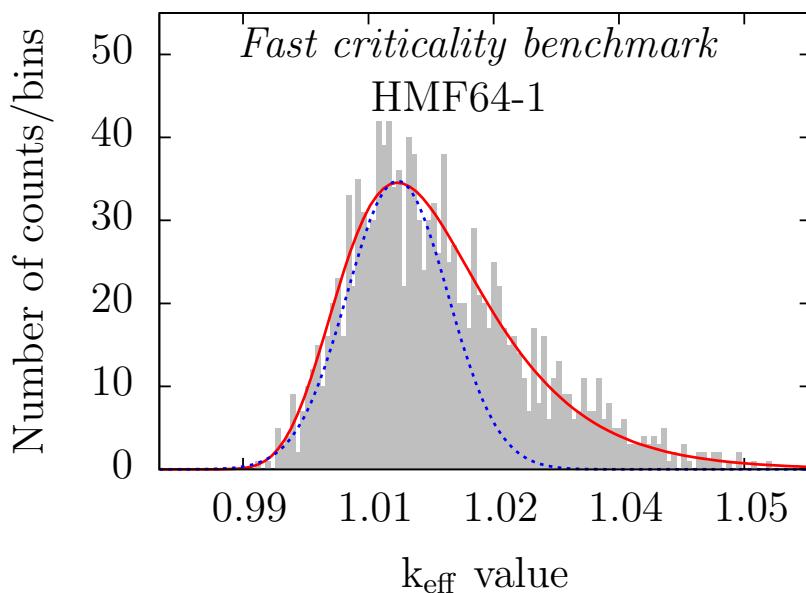


Better fit with the “*Extreme Value Theory*”, or EVT:

$$F(z) = e^{-z} - e^{-z} \text{ with } z = \frac{X-\mu}{\sigma}$$

$$\begin{aligned} \text{Mean } \mu' &= \mu + \gamma\sigma \\ \text{Standard Deviation } \sigma' &= \sigma \frac{\pi}{\sqrt{6}} \end{aligned}$$

Examples with Pb isotopes



Better fit with the “*Extreme Value Theory*”, or EVT:

$$F(z) = e^{-z} - e^{-z} \text{ with } z = \frac{X-\mu}{\sigma}$$

$$\text{Mean } \mu' = \mu + \gamma\sigma$$

$$\text{Standard Deviation } \sigma' = \sigma \frac{\pi}{\sqrt{6}}$$

	HMF-64.1	ADS
k_{eff}	1.00848	0.96648
$\mu' = 1.01394$	$\mu' = 0.96785$	
$\sigma_k \times 10^5$	855	291
	$\sigma' = 1097$	$\sigma' = 345$

Global calculations: from ^{12}C to ^{240}Pu



'In general, this paper will or will not be a breakthrough in methodology if the [practicality and robustness] can or can not be demonstrated.',

ANE Referee, May 2008

'What about actinides, what about real systems ?',

JEFF & WPEC meetings, May-June 2008

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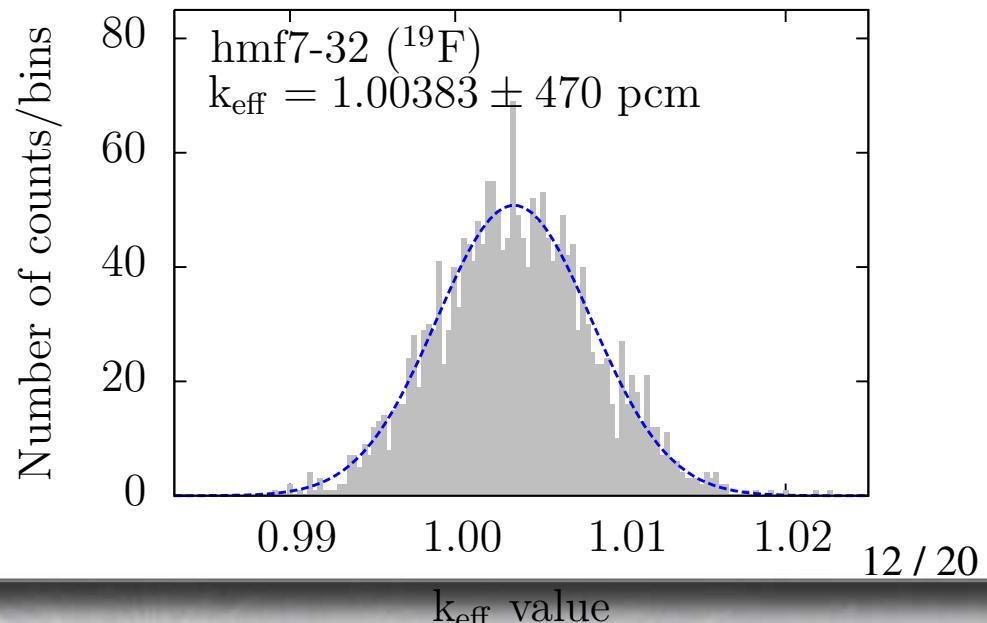
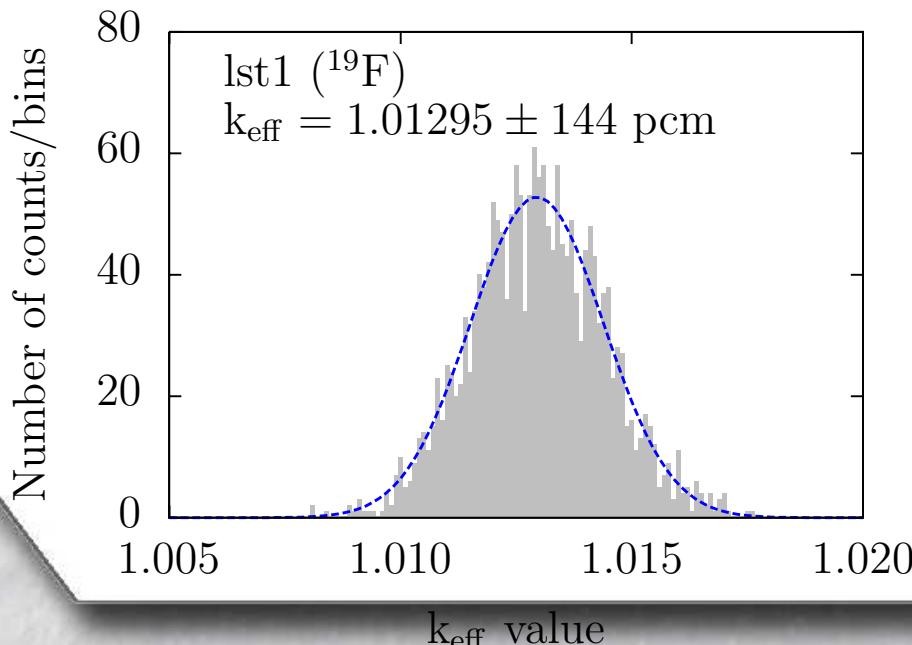
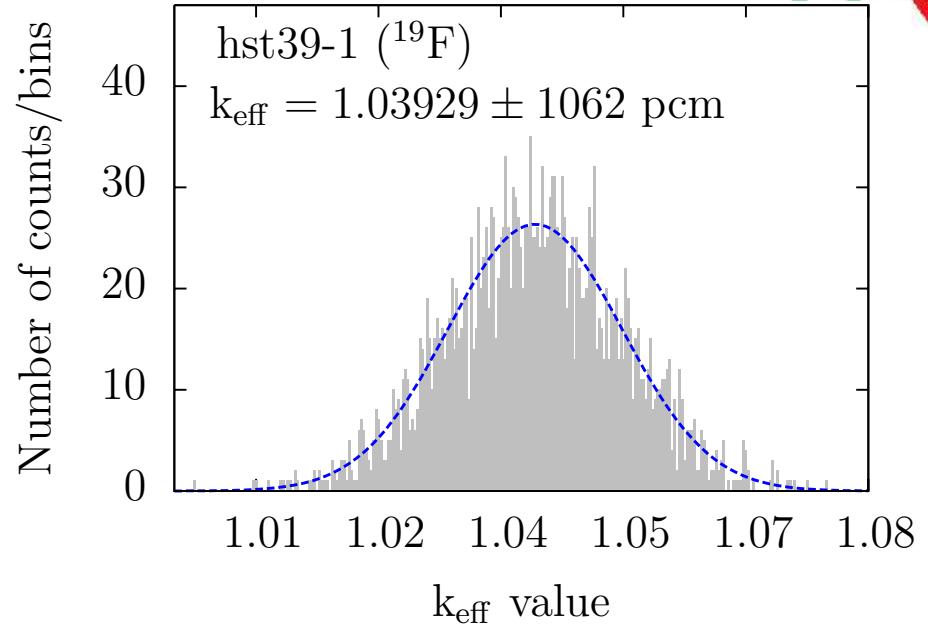
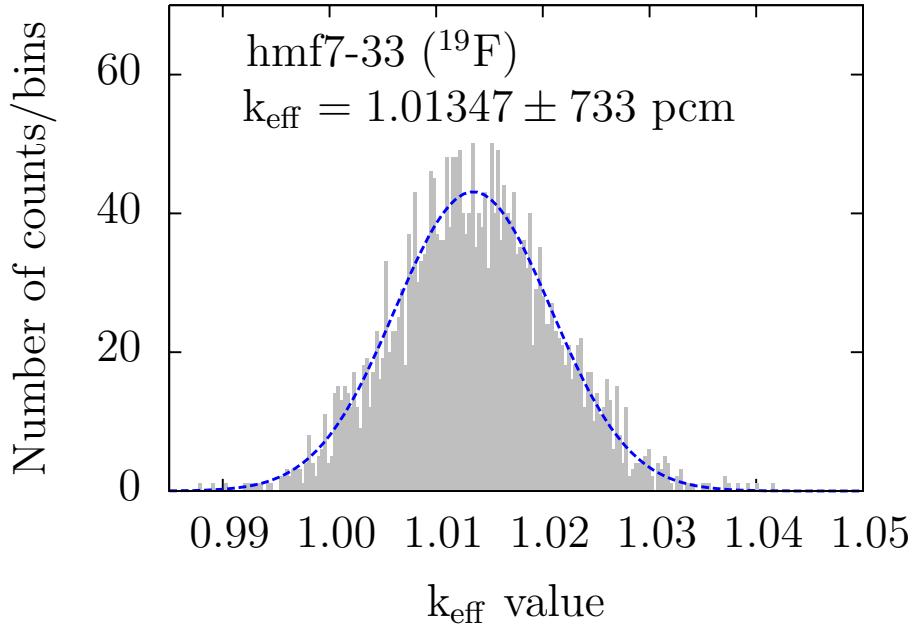
JEFF & WPEC meetings, May-June 2008

Okay, let's go from academic solutions (☕) to mass/applied production (💻) !

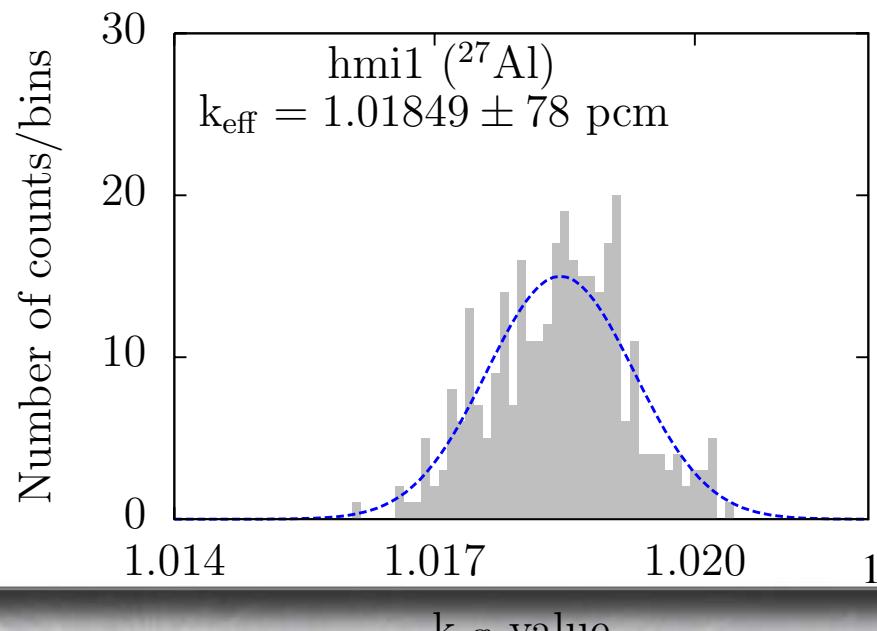
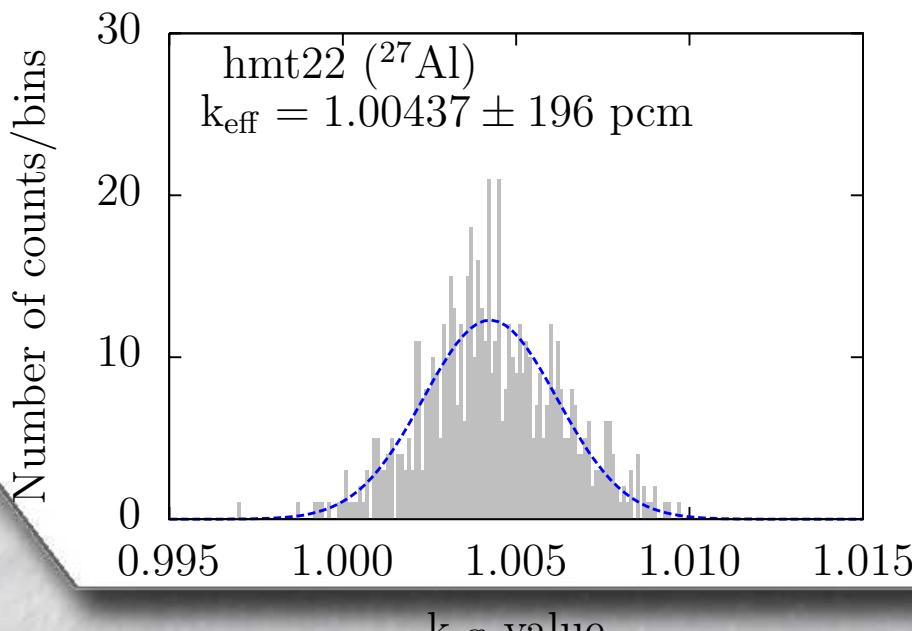
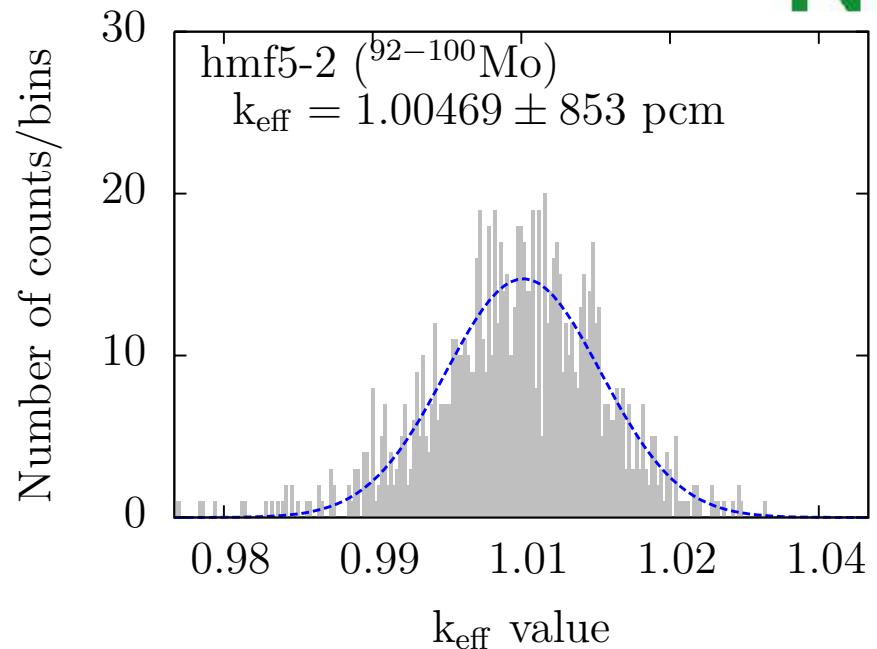
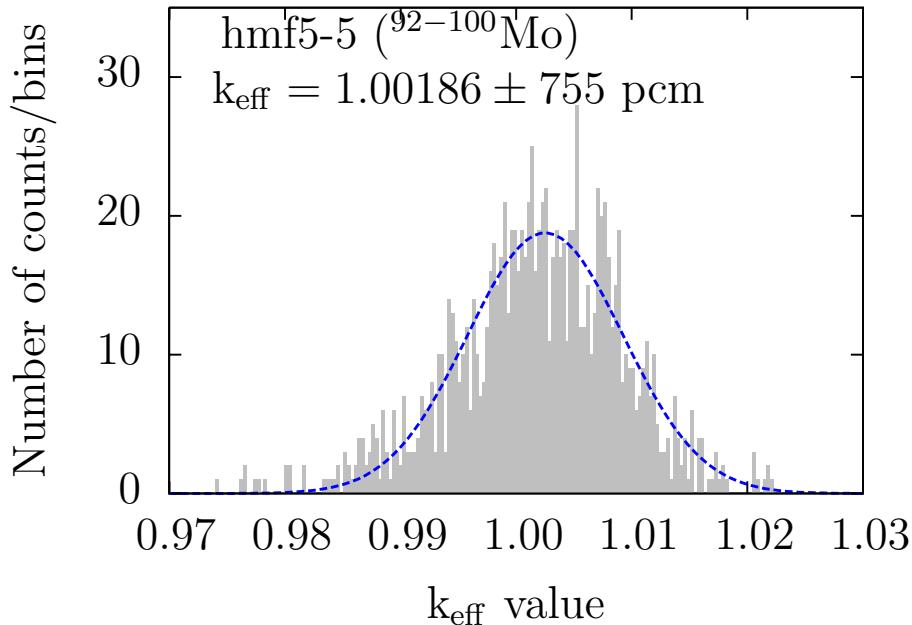
- 🚲 Default TALYS calculation + Resonance parameters (RP) + uncertainties
- 🚲 100 to 2000 ENDF files per isotope from ^{12}C to ^{240}Pu (\simeq 100 isotopes)
- 🚲 190 criticality-safety benchmarks (> 60 000 calculations) from the ICSBP
- 🚲 All Oktavian shielding benchmarks (neutrons and gammas)
- 🚲 Reactivity swing for a LWR using an “Inert Matrix Fuel” (Pu and Mo)
- 🚲 k_{eff} for a HTR (PBMR), ESKOM specifications

Examples of k_{eff} benchmarks for ^{19}F

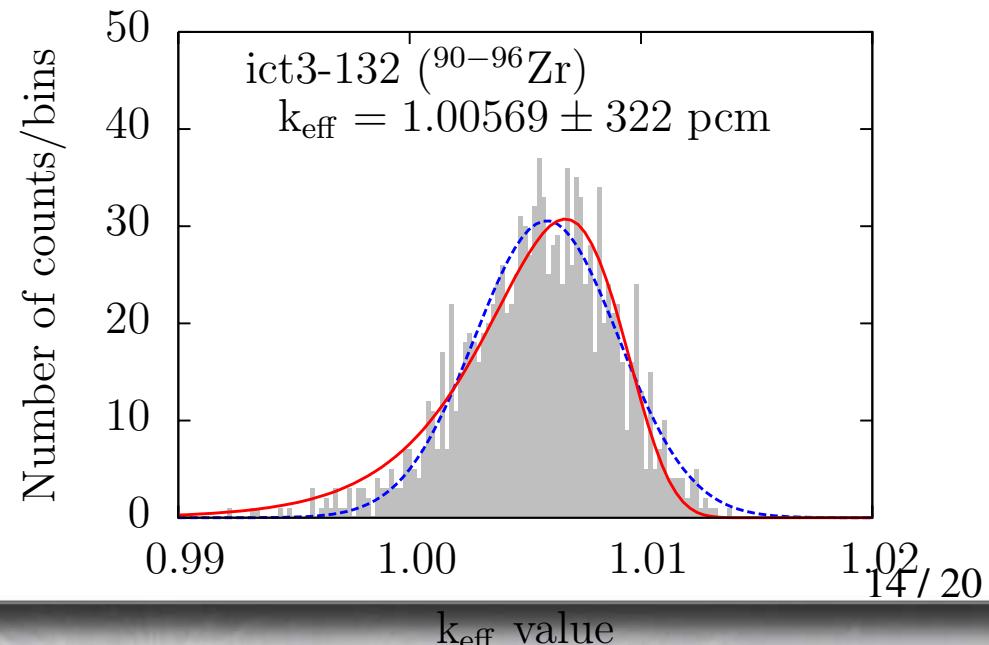
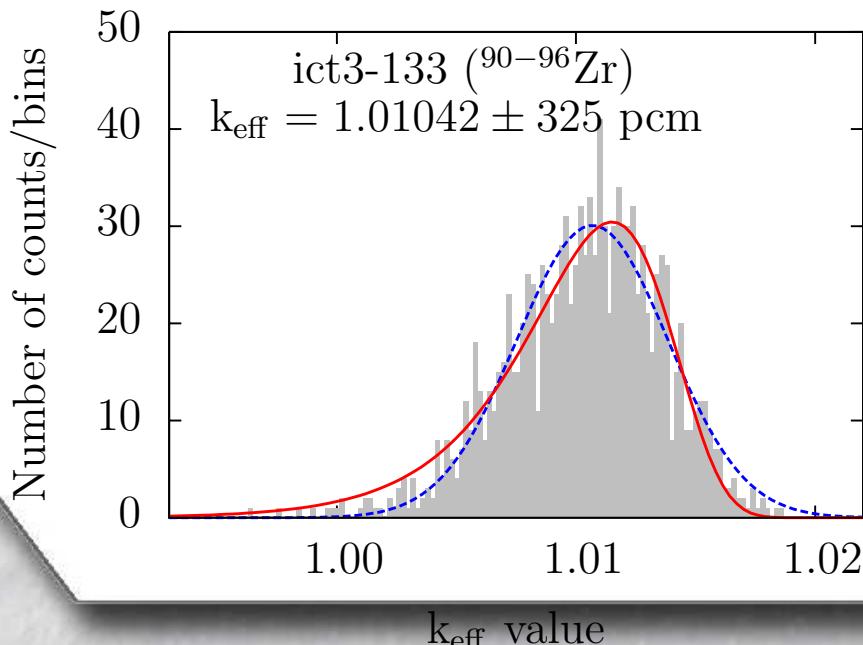
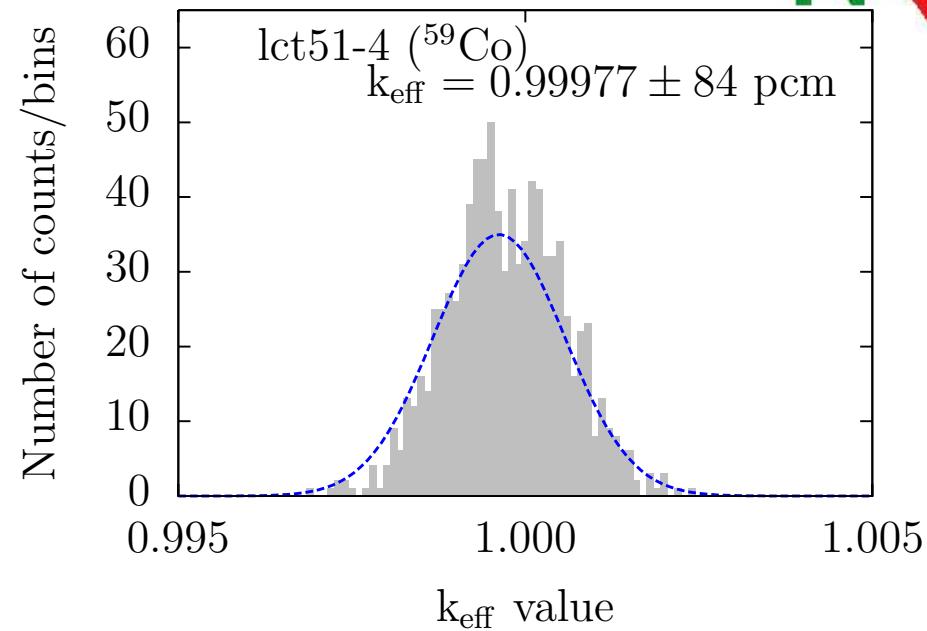
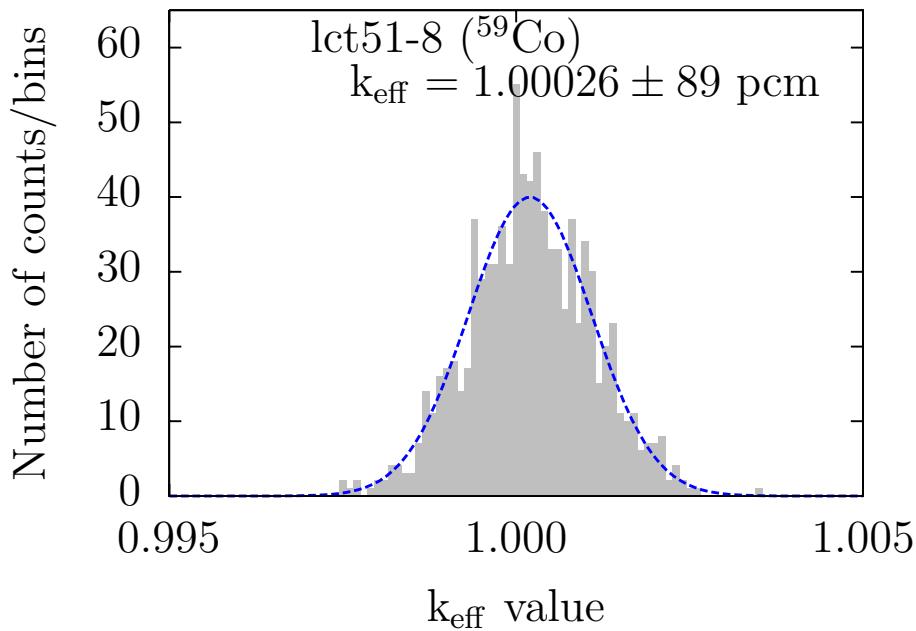
NRG



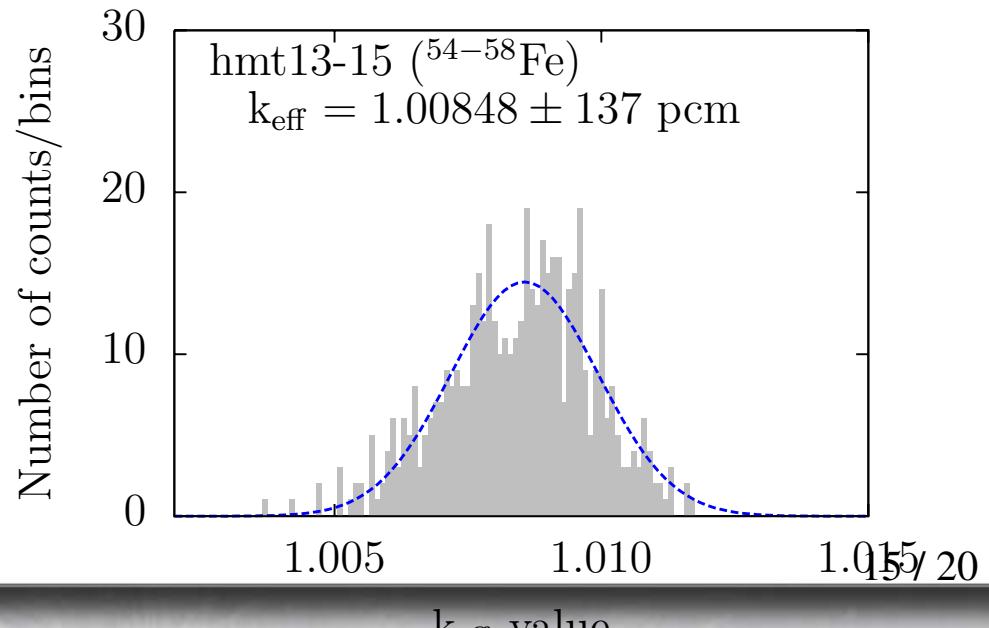
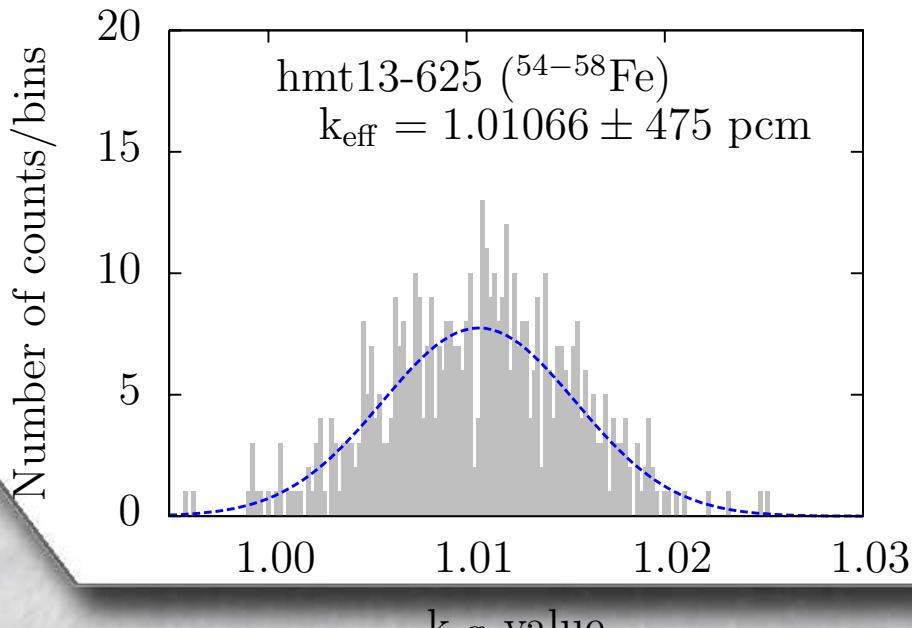
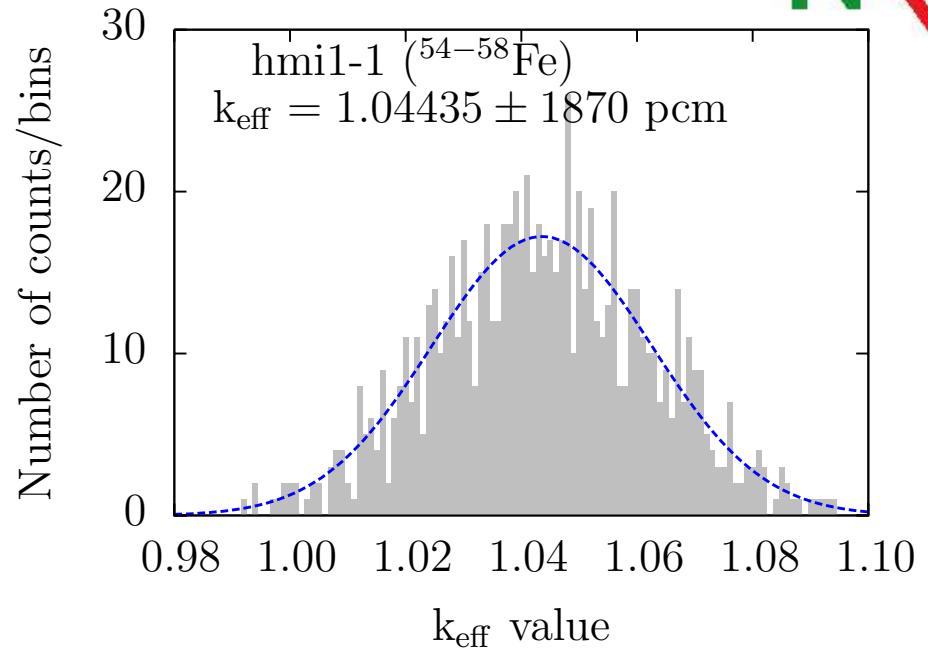
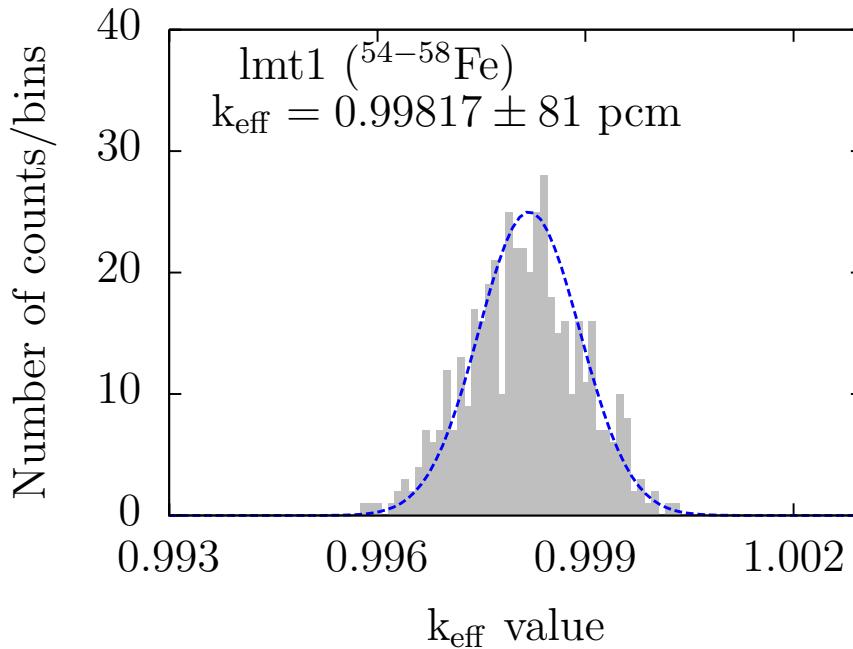
Examples of k_{eff} benchmarks for ^{27}Al and $^{92-100}\text{Mo}$



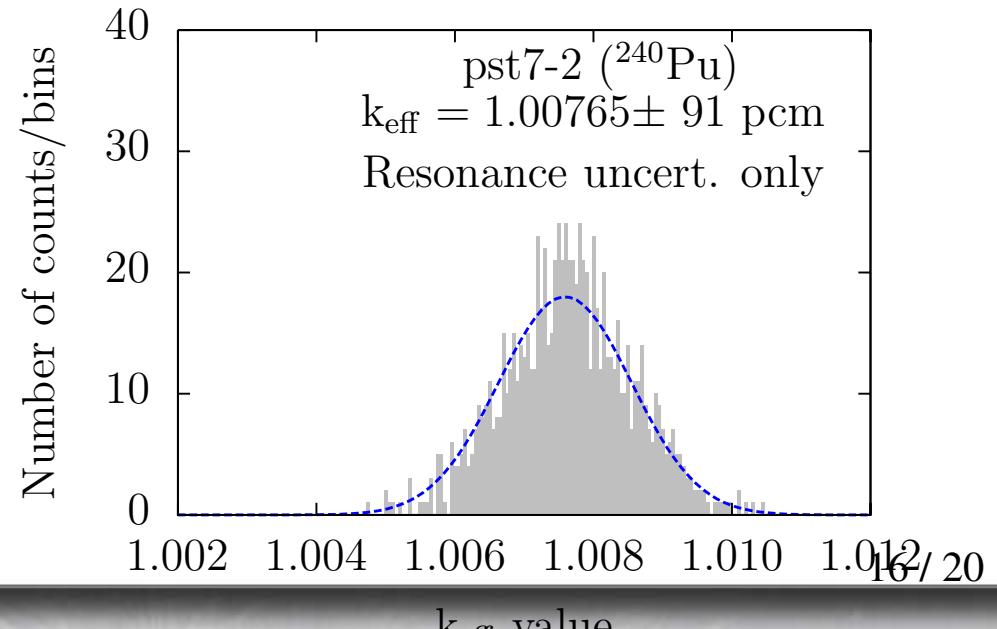
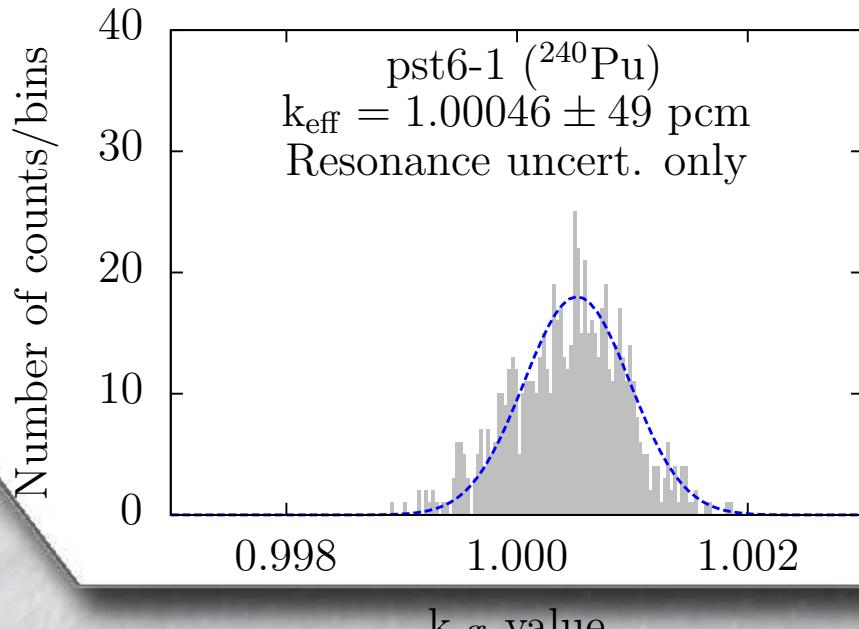
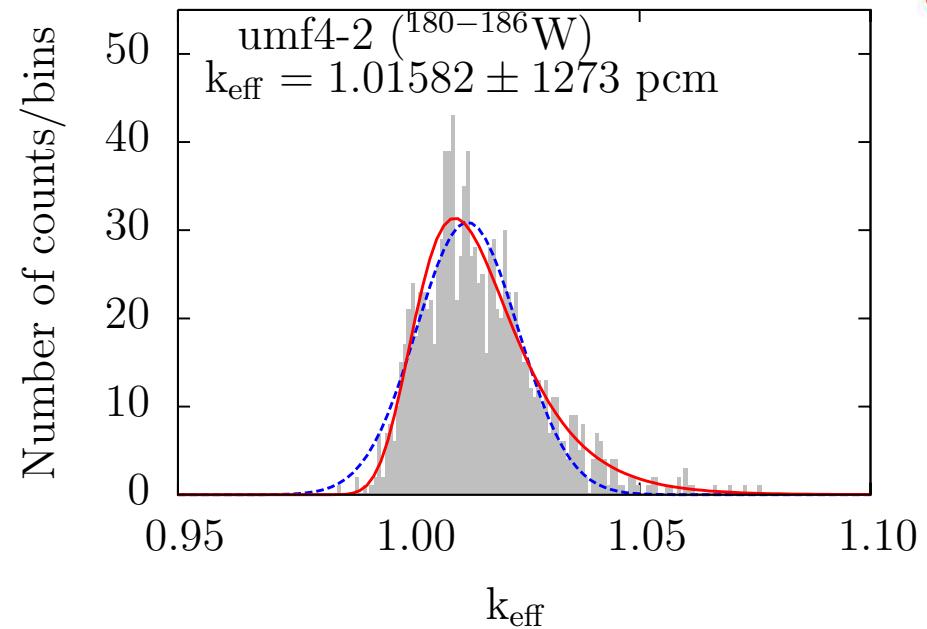
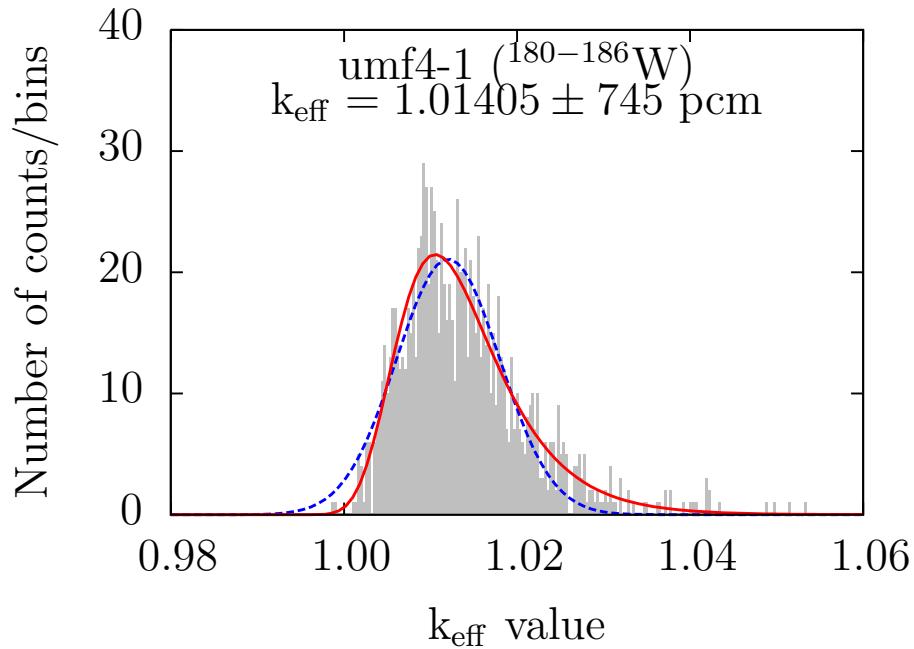
Examples of k_{eff} benchmarks for ^{59}Co and $^{90-96}\text{Zr}$



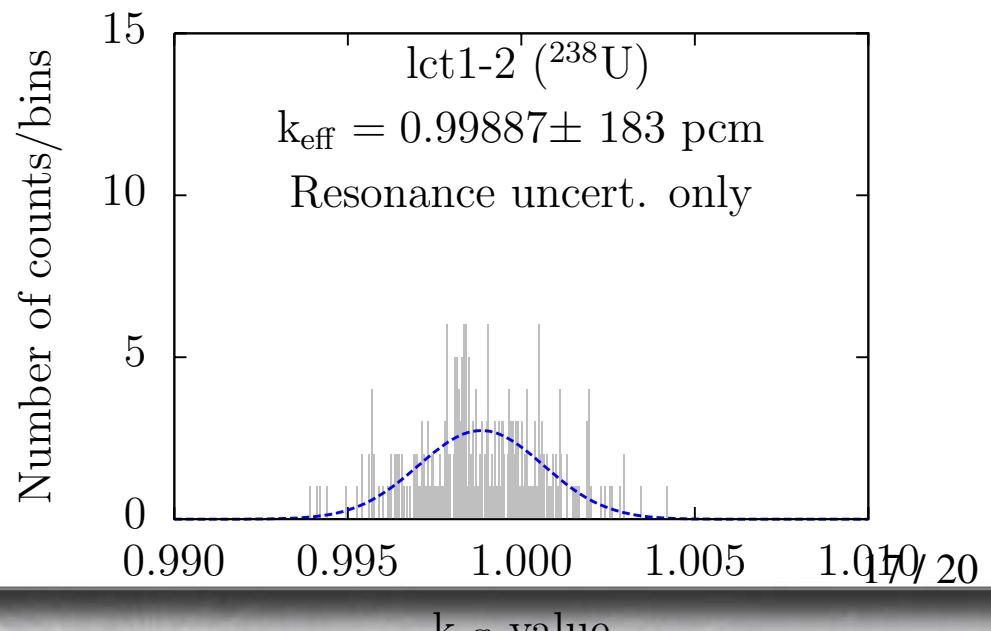
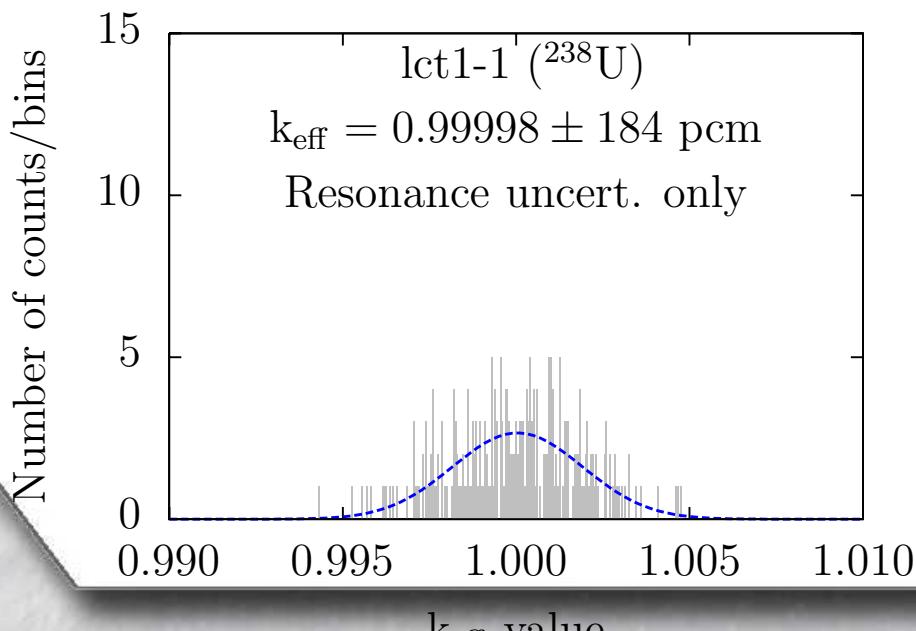
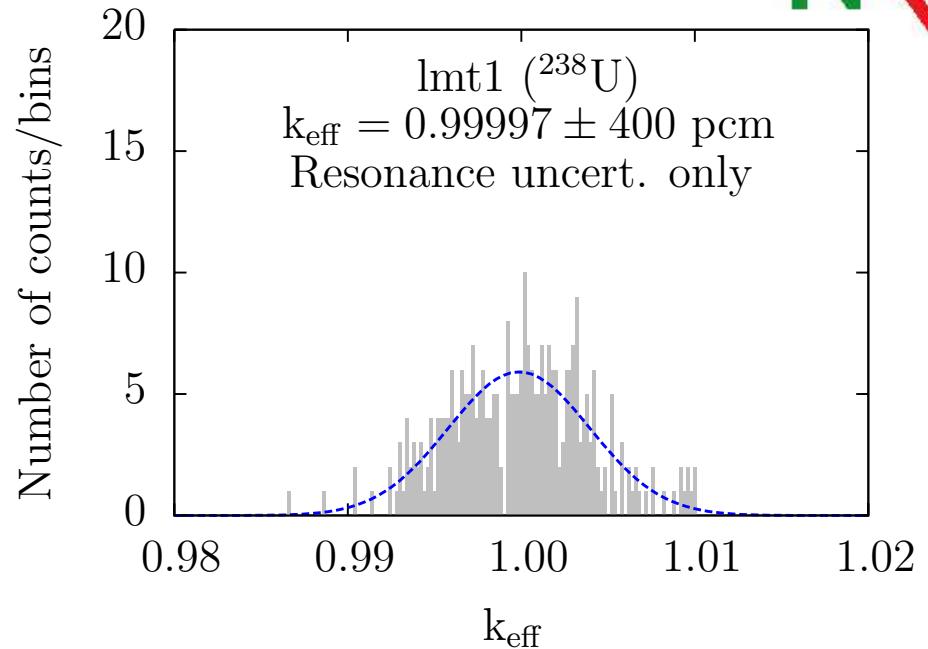
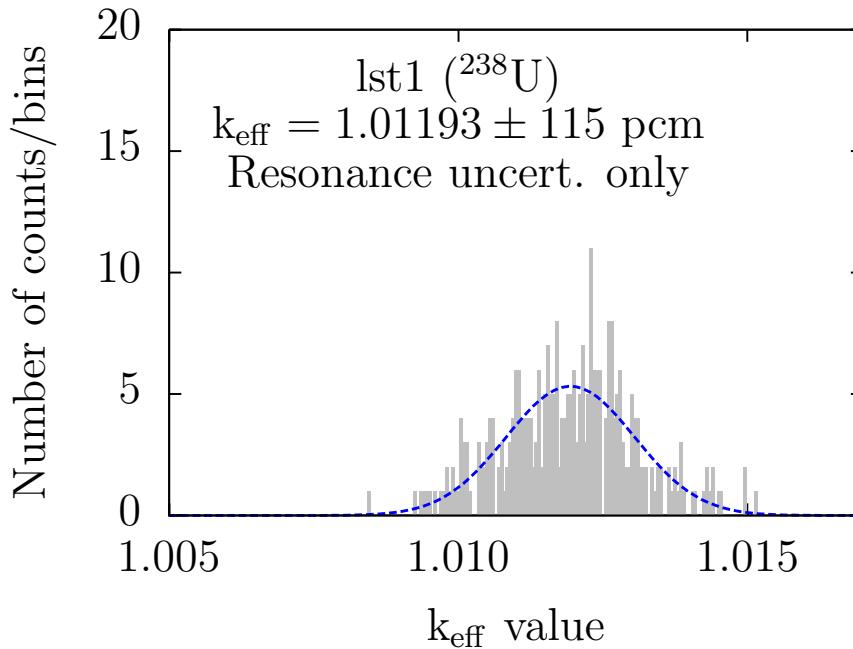
Examples of k_{eff} benchmarks for $^{54-58}\text{Fe}$



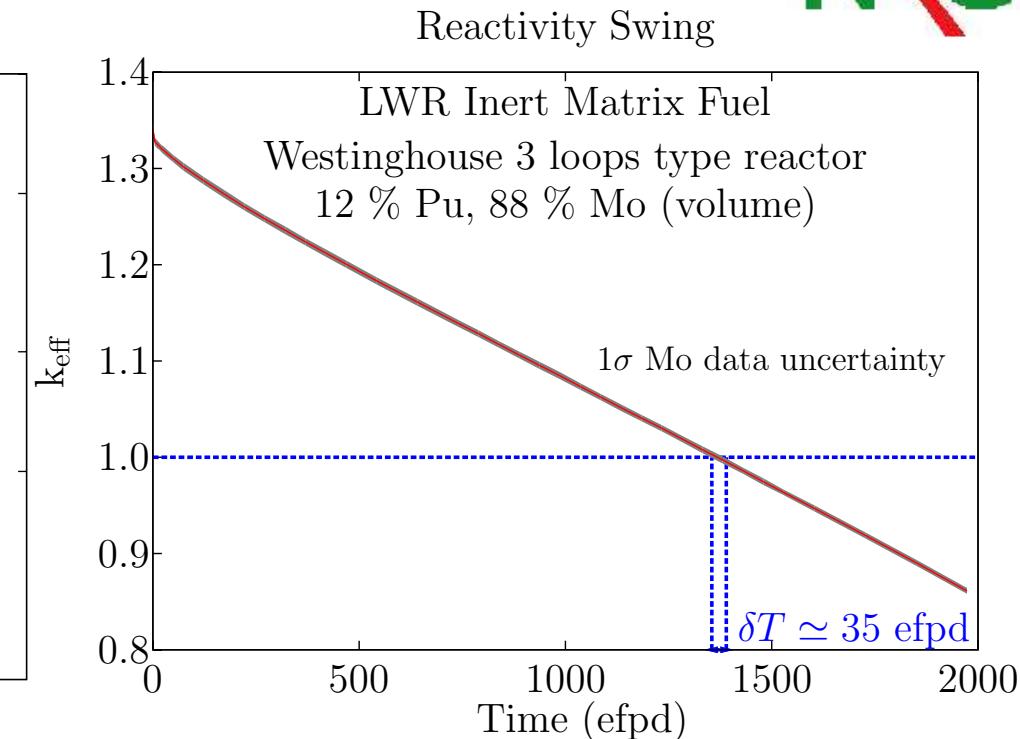
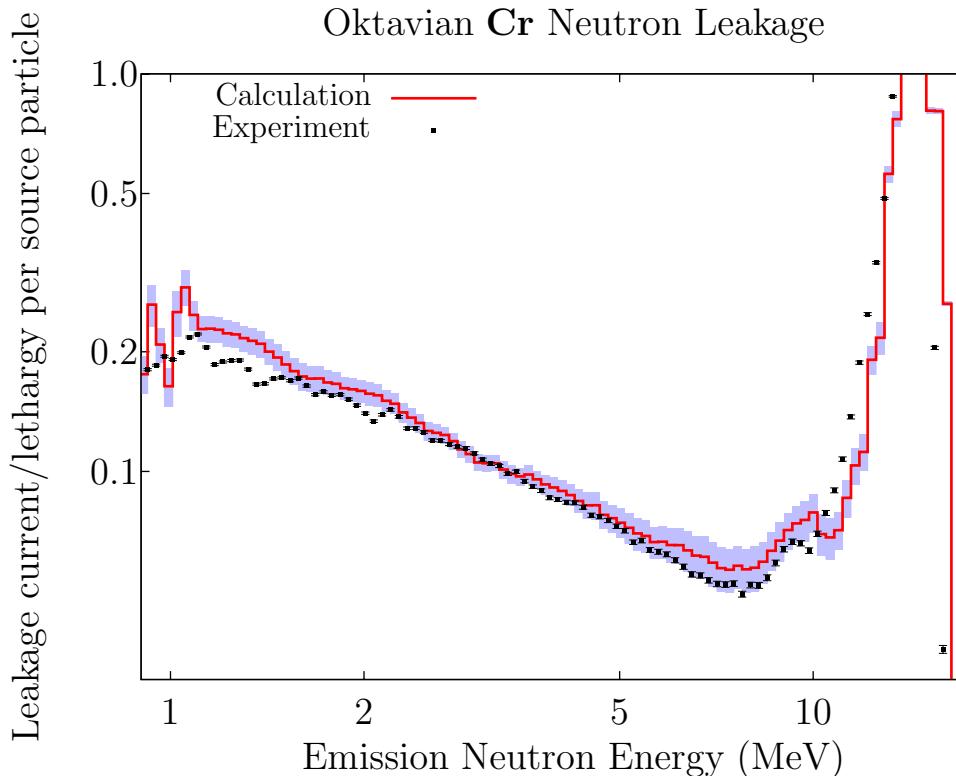
Examples of k_{eff} benchmarks for $^{180-186}\text{W}$ and ^{240}Pu



Examples of k_{eff} benchmarks for ^{238}U



Examples of shielding benchmarks and reactivity swing



(Blind Talys calculations)

- Also applied to Mn, Co, Al, Cu Oktavian benchmarks
- and industrial PWR reactor for life-time extension (uncertainty on the reactor pressure vessel damage)

Pros and Cons



- 😊 + No MF 32-35 (no 2 Gb files) **but** every possible cross correlation included
- 😊 + No approximation **but** true probability distribution
- 😊 + Only essential info for an evaluation is stored
- 😊 + No perturbation code necessary, **only** “essential” codes
- 😊 + Feedback to model parameters
- 😊 + QA
- 😢 - Needs discipline to reproduce
- 😢 - Memory and computer time
- 😢 - Complexity for full reactor core calculation not fully investigated
- 😢 - Role of data centers would change

Conclusions and future improvements

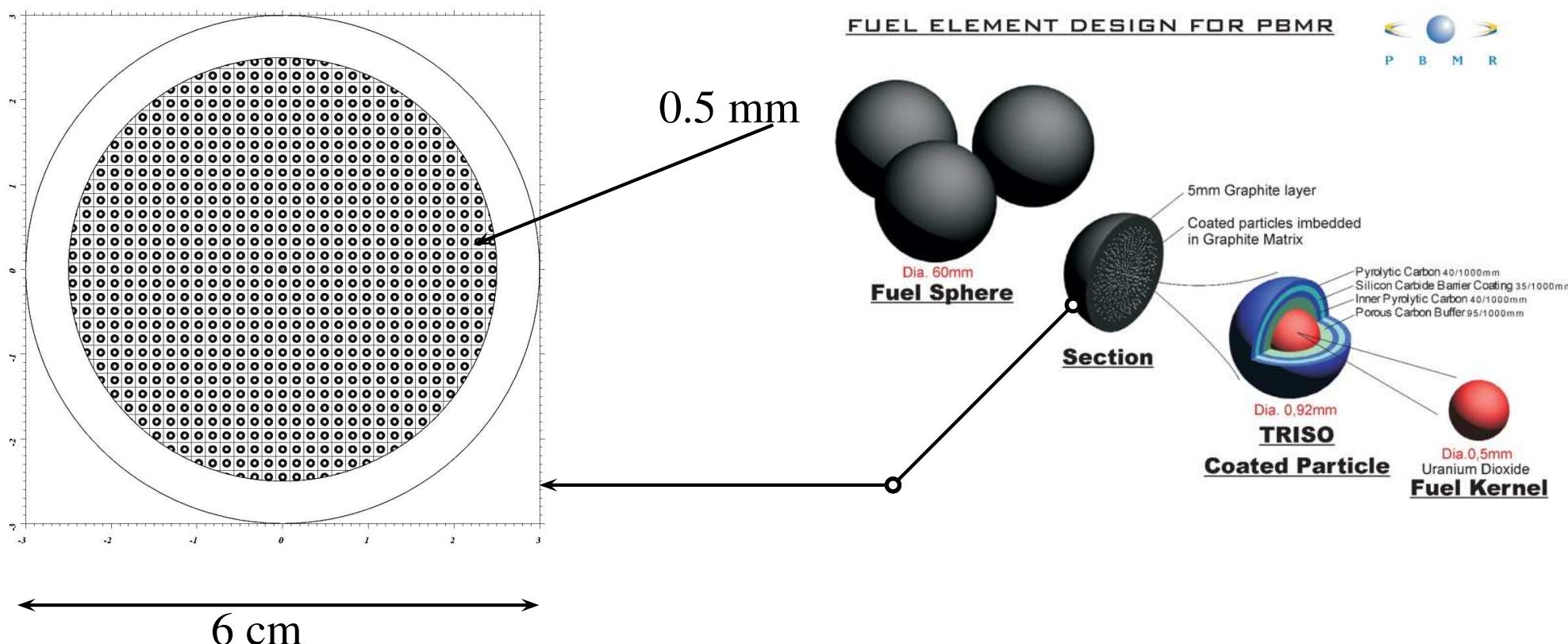


- ☒ New methodology to propagate nuclear data uncertainty to integral quantities (k_{eff} benchmarks, shielding benchmarks, reactivity swing, neutron flux for commercial reactor) via Monte Carlo
- ☒ Proof of principle with high quality Pb evaluations
- ☒ Mass production tested on more than 190 benchmarks
- ☒ “Paper to present the principle”: under revision for ANE
- ☒ “Application to a real complex system”: PBMR
- Needs for better sampling in the resonance region
- Needs for a better “accept-reject” mechanism
- What if nuclear modeling does not match the accuracy of the measurements ? (how to sample ?)
- Needs to develop best central-value evaluations (non-fissile and fissile) ?

Application to a Pebble Bed Modular Reactor (PBMR)



- * Model of a fuel pebble
- * Fuel particles, surrounded by coating layers, explicitly modelled
- * Regular rectangular lattice of fuel particles

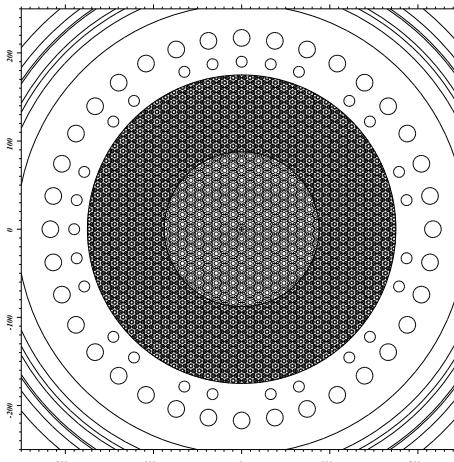


Application to a Pebble Bed Modular Reactor (PBMR)

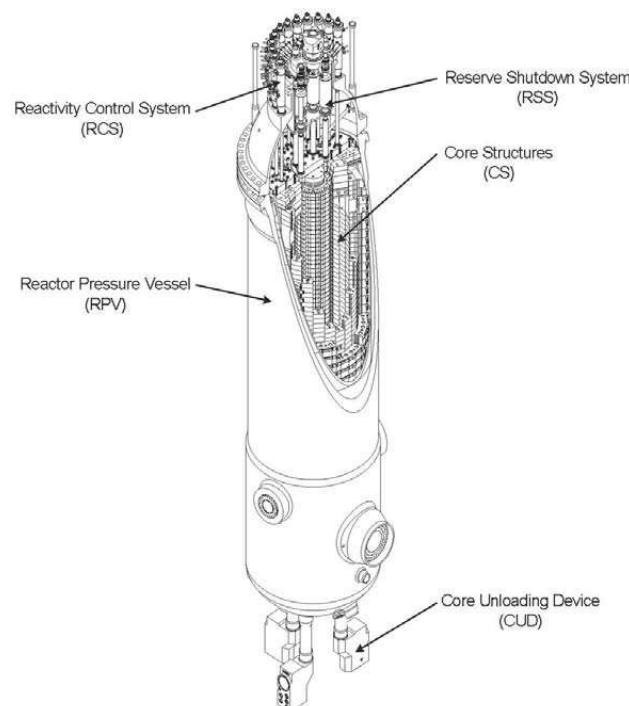
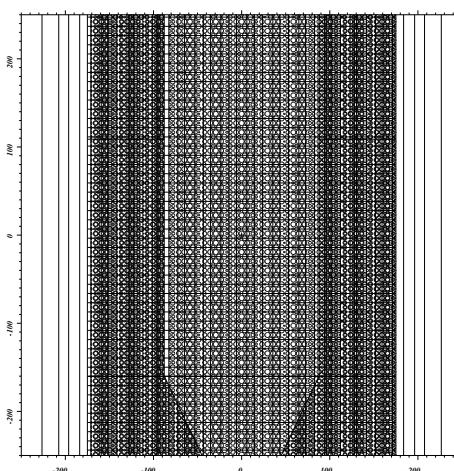


- * Hexagonal close packed lattice
- * Moderator region consists of homogeneous moderator pebbles as the fuel, reflectors and shields as defined by ESKOM

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PBMR core analysis; production  
of surface source  
  
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( 0.000000, 1.000000, 0.000000)  
( 1.000000, 0.000000, 0.000000)  
origin:  
( 0.00, 0.00, 500.00)  
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```



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of surface source  
  
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( 0.00, 0.00, 500.00)  
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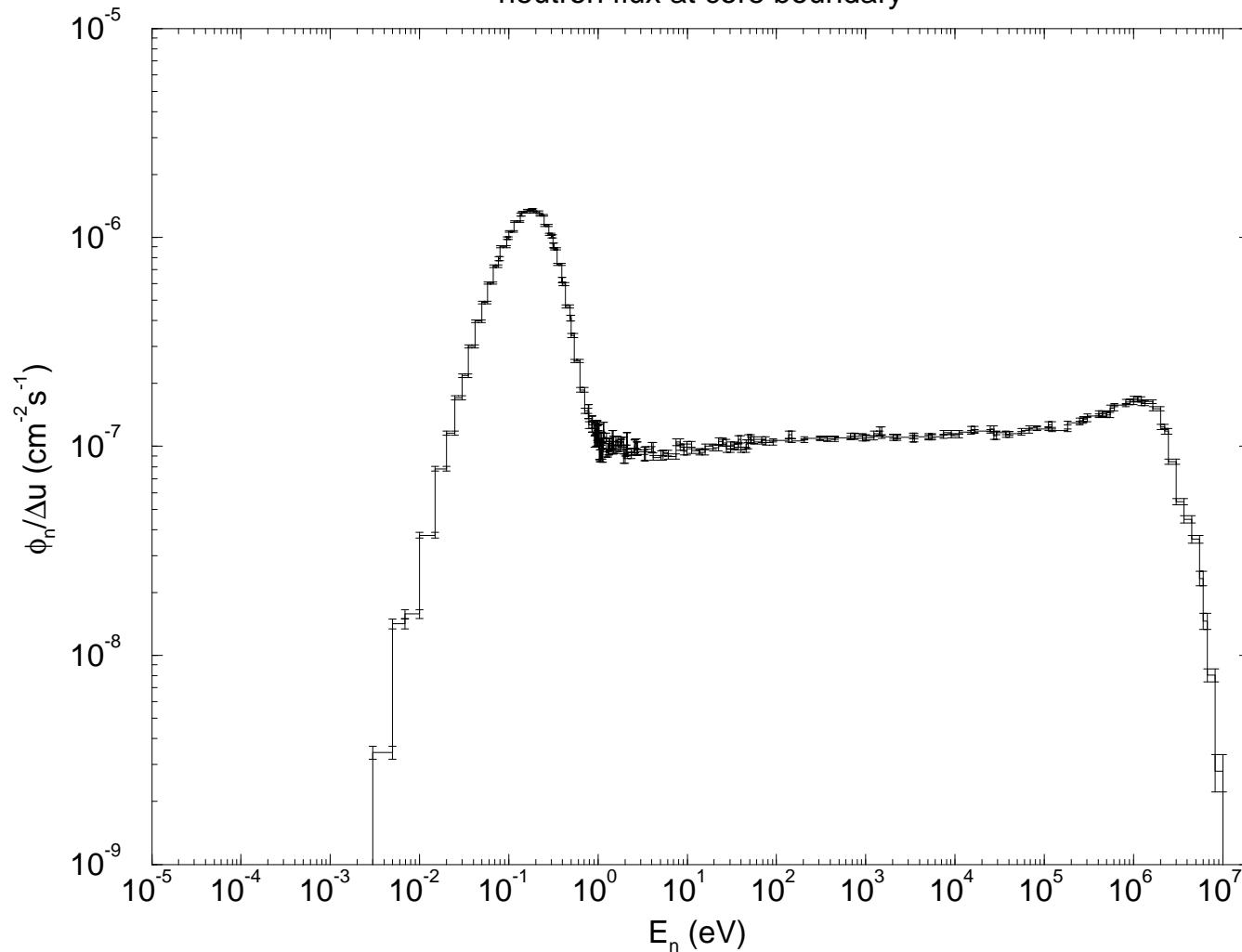


PBMR: Neutron Flux spectrum



PBMR design

neutron flux at core boundary

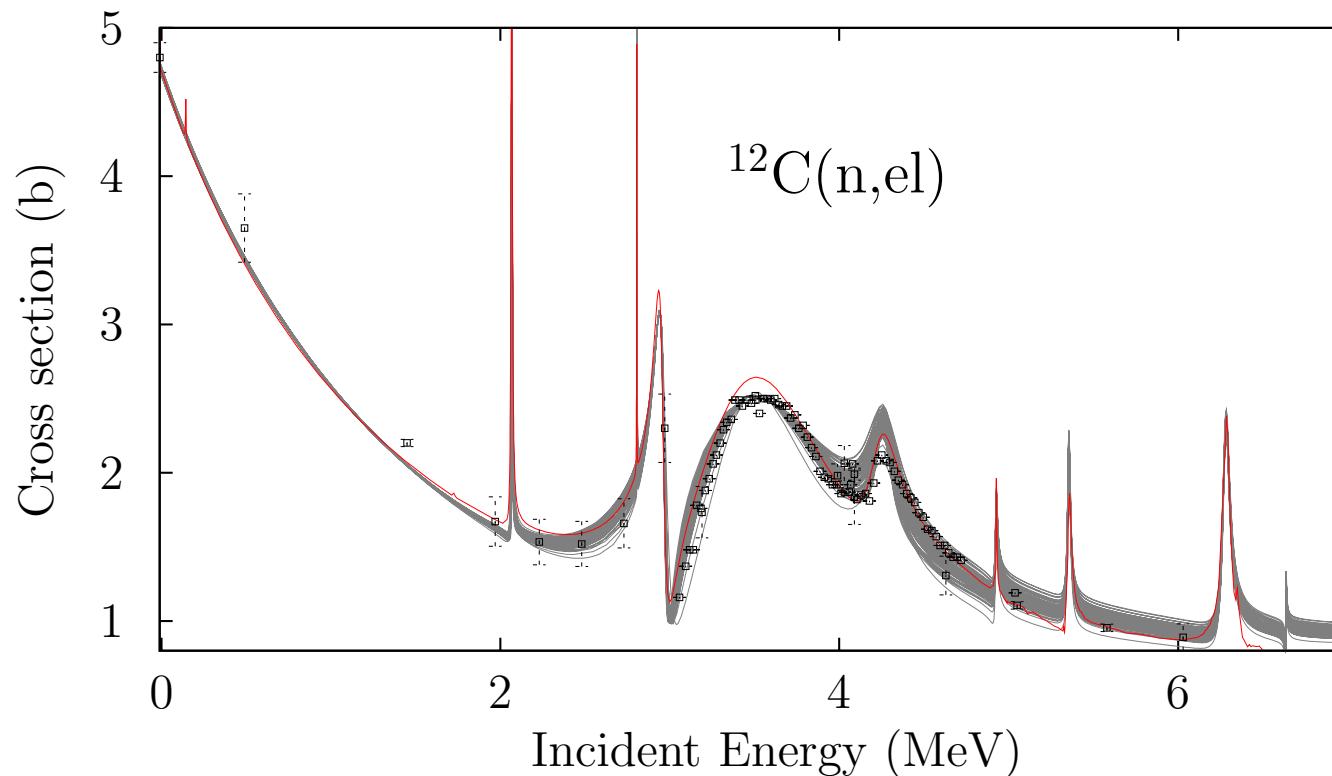


Neutron flux spectrum at the radial core boundary (Almost no neutron above few MeV)

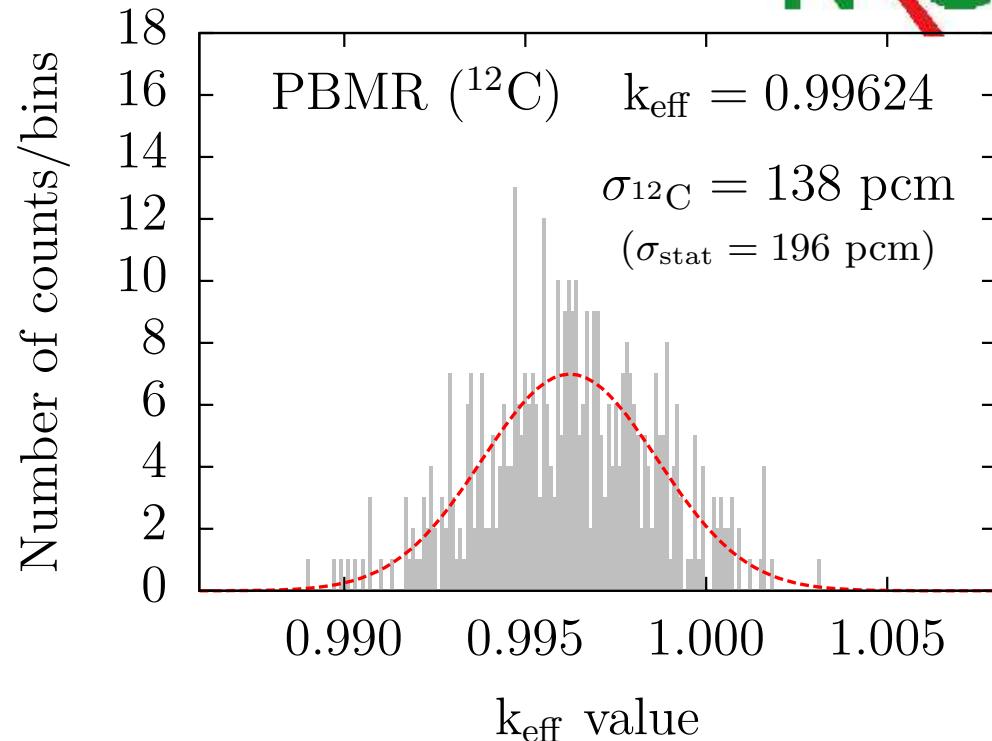
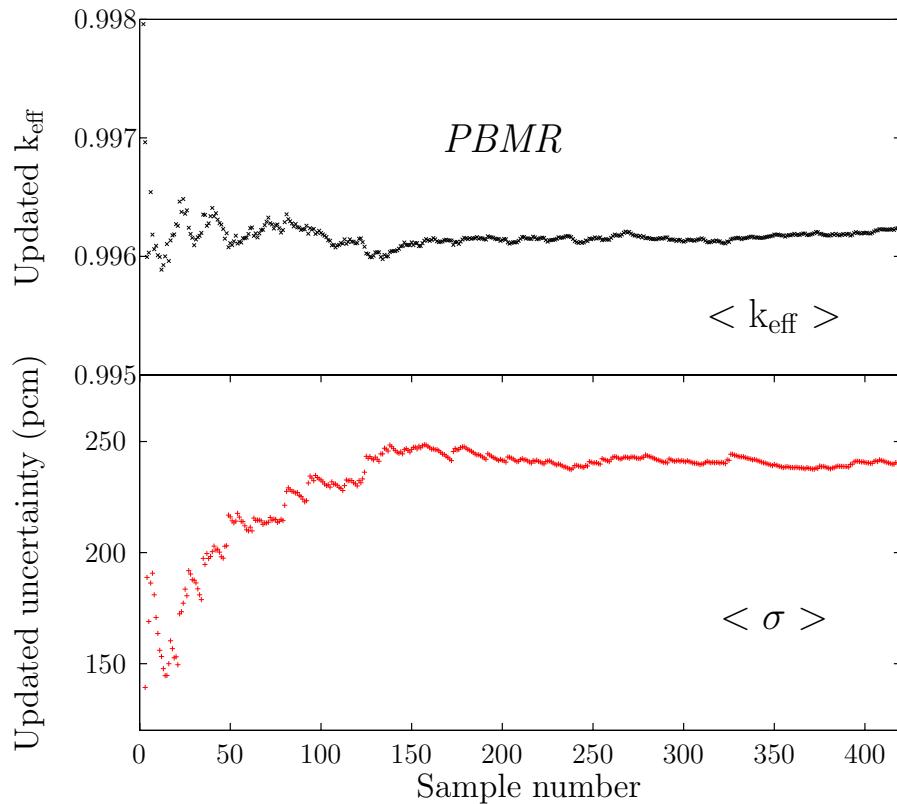
PBMR: ^{12}C nuclear data



- * For neutron energy lower than few MeV: only elastic and capture cross sections
- * JEFF-3.1: $\sigma_{\text{th}}(\text{n},\text{el}) = 4.746 \pm 0.002 \text{b}$ and $\sigma_{\text{th}}(\text{n},\gamma) = 3.53 \pm 0.07 \text{mb}$
- * All (n,el) , (n,γ) , angular distribution and emission spectra randomly varied



PBMR: Results



- ⌘ Convergence achieved after $\simeq 350$ runs (10 days of 15 CPU)
- ⌘ More runs would be suitable
- ⌘ Effect of other isotopes (^{13}C , Si, fission products and of course actinides)

Table 1 (Preliminary)

Benchmark	Isotopes	$k_{\text{eff}}/(k_{\text{eff,JEFF-3.1}})$ ratio	Statistical uncertainty (pcm)	Uncertainty from nuclear data (pcm)
hmt8d	^{234}U	1.00	46	30
hmt8s	^{234}U	1.00	46	19
hmt9s	^{234}U	1.00	46	22
hmt10-15	^{234}U	1.00	45	12
hmt10-7	^{234}U	1.00	45	32
hmt18d	^{234}U	0.99	46	48
hmt18s	^{234}U	1.00	46	52
hmt14s	^{234}U	1.00	48	35
pst6-1	^{240}Pu	1.00	40	27
pst6-2	^{240}Pu	1.00	39	31
pst6-3	^{240}Pu	1.00	40	23
pst7-2	^{240}Pu	1.00	49	76
pst7-3	^{240}Pu	1.00	49	71
mmf11-1	^{241}Am	1.00	37	< 37

Table 2 (Preliminary)

Benchmark	Isotopes	$k_{\text{eff}}/(k_{\text{eff,JEFF-3.1}})$ ratio	Statistical uncertainty (pcm)	Uncertainty from nuclear data (pcm)
lst-1	^{238}U	1.00	26	108
lmt-1	^{238}U	1.00	61	405
lct1-1	^{238}U	1.00	69	176
lct1-2	^{238}U	1.00	69	165
lct2-1	^{238}U	1.00	79	110
lct2-2	^{238}U	1.00	80	117
lct2-3	^{238}U	1.00	79	130
lct2-4	^{238}U	1.00	78	100
lct2-5	^{238}U	1.00	77	105
lct3-1	^{238}U	1.00	34	132
lct3-2	^{238}U	1.00	39	134
lct3-3	^{238}U	1.00	39	125
lct3-4	^{238}U	1.00	38	137
lct3-5	^{238}U	1.00	38	141
lct3-6	^{238}U	1.00	36	153

Table 3 (Preliminary)

Benchmark	Isotopes	$k_{\text{eff}}/(k_{\text{eff,JEFF-3.1}})$ ratio	Statistical uncertainty (pcm)	Uncertainty from nuclear data (pcm)
hmf7-32	^{19}F	1.00	67	465
hmf7-33	^{19}F	1.00	68	734
hmf7-34	^{19}F	1.00	70	943
hst39-1	^{19}F	1.00	95	1058
hst39-2	^{19}F	1.01	97	1003
hst39-3	^{19}F	1.01	96	961
hst9-2	^{19}F	1.00	24	59
hst9-3	^{19}F	1.00	24	39
lst1	^{19}F	1.00	85	116
imf10-1	$^{28-30}\text{Si}$	0.99	32	25
lct1-1	$^{28-30}\text{Si}$	1.00	69	49
hmf5-2	$^{28-30}\text{Si}$	1.00	72	20
hmf5-3	$^{28-30}\text{Si}$	1.00	76	< 76
hmf5-4	$^{28-30}\text{Si}$	1.00	78	< 78
hmf5-5	$^{28-30}\text{Si}$	1.00	71	18