

# TMC vs. perturbation

*and other applications*

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- 
- ① *Short introduction to nuclear data uncertainties*
  - ② *Outcomes of the approach (TMC is one of them)*
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  - ⑤ *Fast TMC*
  - ⑥ *Conclusions*



All slides can be found at:

[ftp://ftp.nrg.eu/pub/www/talys/bib\\_rochman/presentation.html](ftp://ftp.nrg.eu/pub/www/talys/bib_rochman/presentation.html).

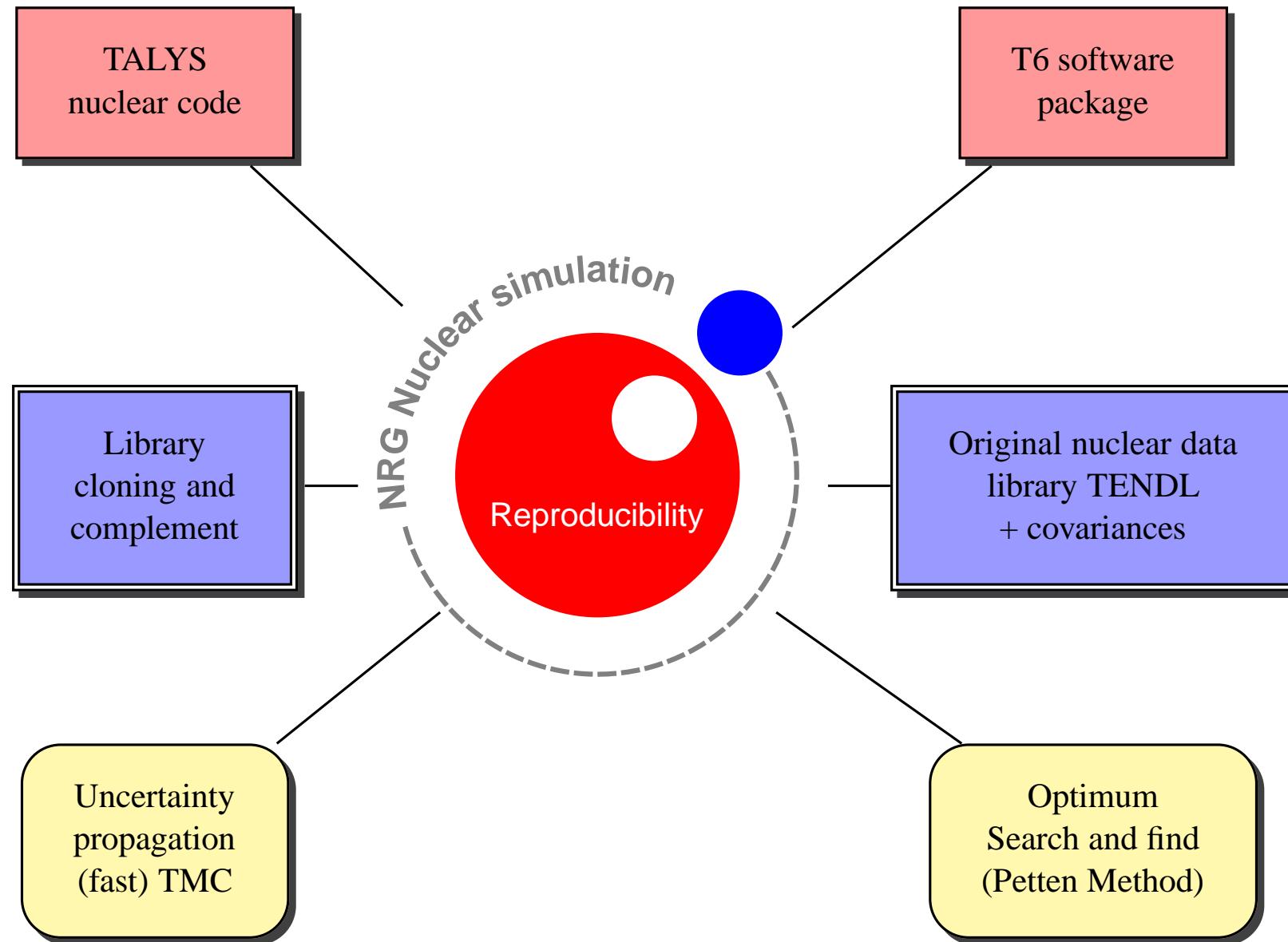
# Introduction to nuclear data uncertainties



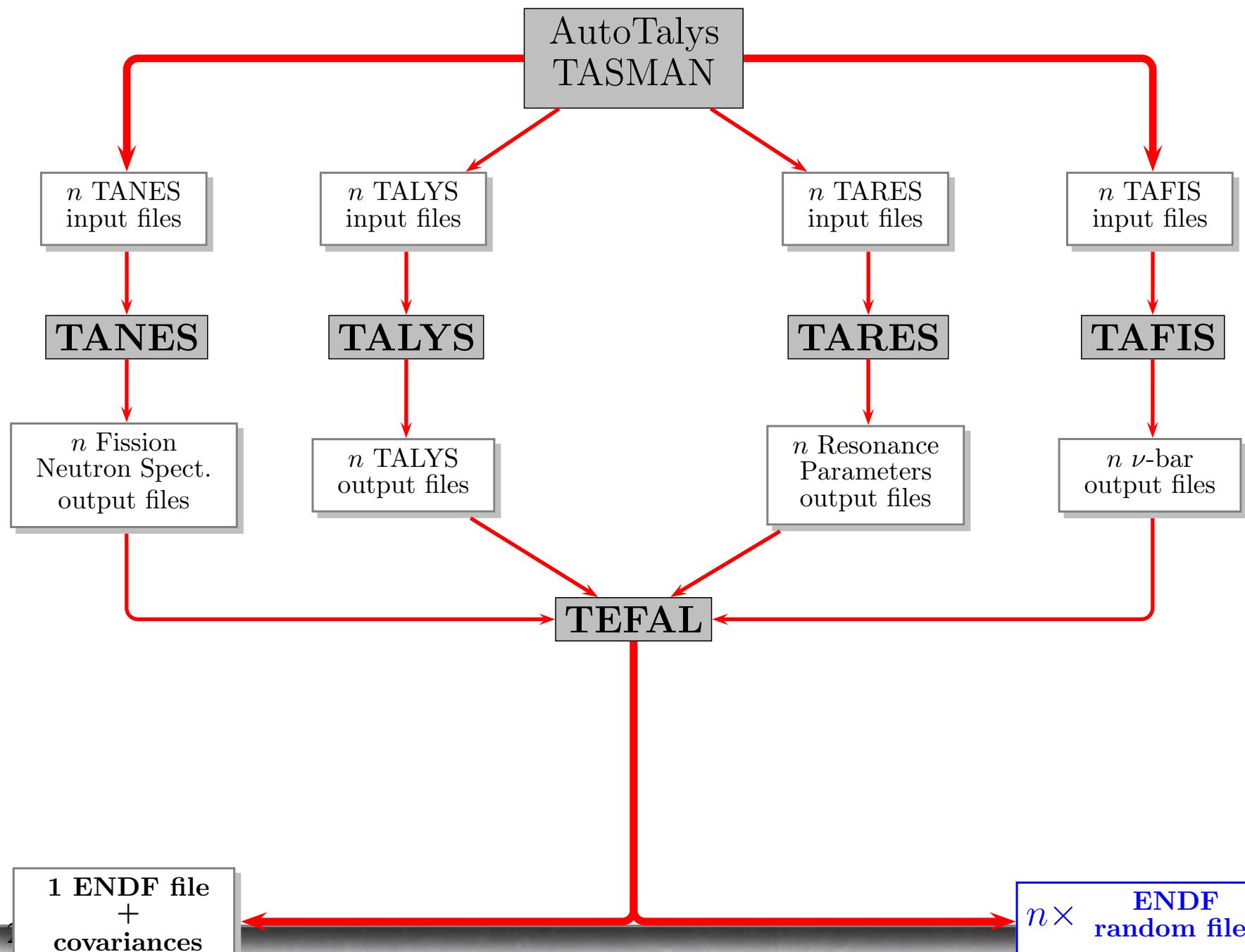
General comments:

- I    uncertainties are not errors (and vice versa),
  - II    uncertainties should now be given with all data (seems obvious ?),
  - III    they are related to risks, quality of work, money, perception, fear, safety...
- 
- ||||                  **Uncertainty  $\Leftarrow$  safety  $\Leftarrow$  professionalism**
  - ||||    True uncertainties do not exist ! They are the reflection of our knowledge and methods.
  - |||| I    All the above for covariances
  - |||| II    The importance of nuclear data uncertainties should be checked. If believed negligible, please prove it !

# Backbone of our methodology: REPRODUCIBILITY



# TMC: procedure for the random file production



# TMC for nuclear data uncertainty propagation, what else ?



- 😊 + No covariance matrices (no 2 Gb files) **but** every possible cross correlation included,
- 😊 + No approximation **but** true probability distribution,
- 😊 + Only essential info for an evaluation is stored,
- 😊 + No perturbation code necessary, **only** “essential” codes,
- 😊 + Feedback to model parameters,
- 😊 + Full reactor core calculation and transient,
- 😊 + Also applicable to fission yields, thermal scattering, pseudo-fission products, all isotopes (...**just everything**),
- 😊 + Other variants: AREVA (NUDUNA), GRS (XSUSA), CIEMAT (ACAB), PSI (NUSS), CNRS Grenoble..., based on covariance files,
- 😊 + Many spin-offs (TENDL covariances, sensitivity, adjustment...)
- 😊 + QA.
  
- 😢 - Needs discipline to reproduce,
- 😢 - Memory and computer time (not human time),
- 😢 - Need mentality change.

# 2008: Total Monte Carlo (TMC)



Control of nuclear data (TALYS system)

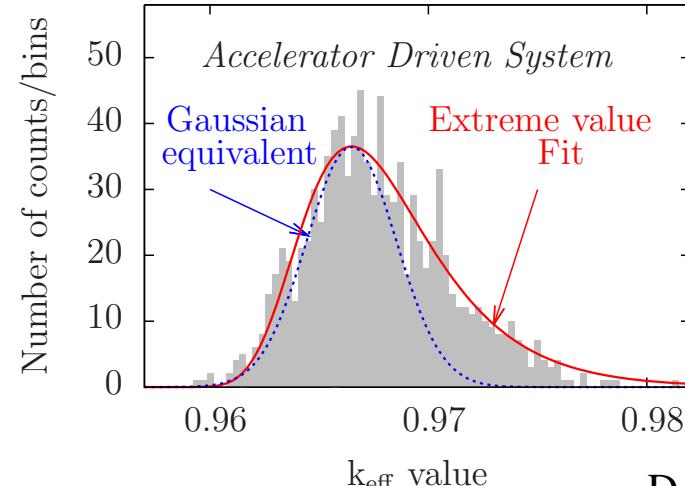
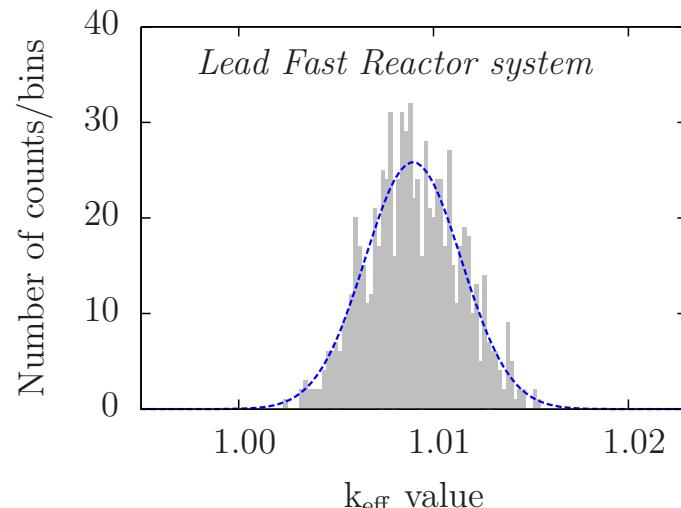
+ processing (NJOY)

+ system simulation (MCNP/ERANOS/CASMO...)

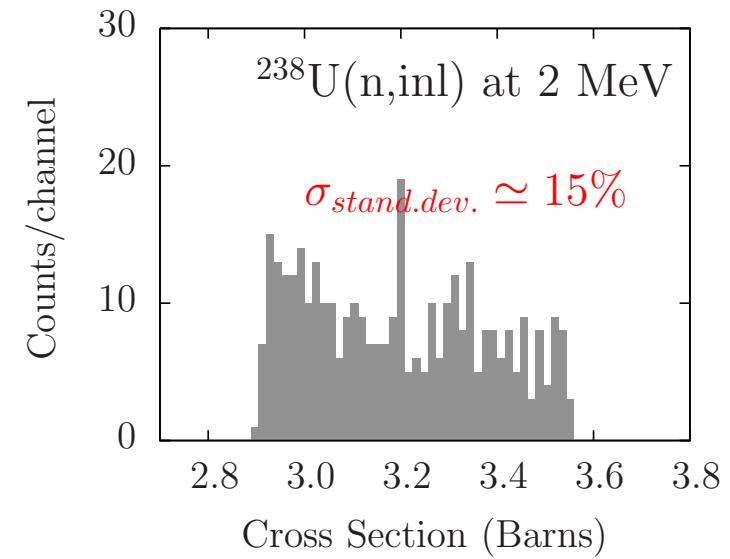
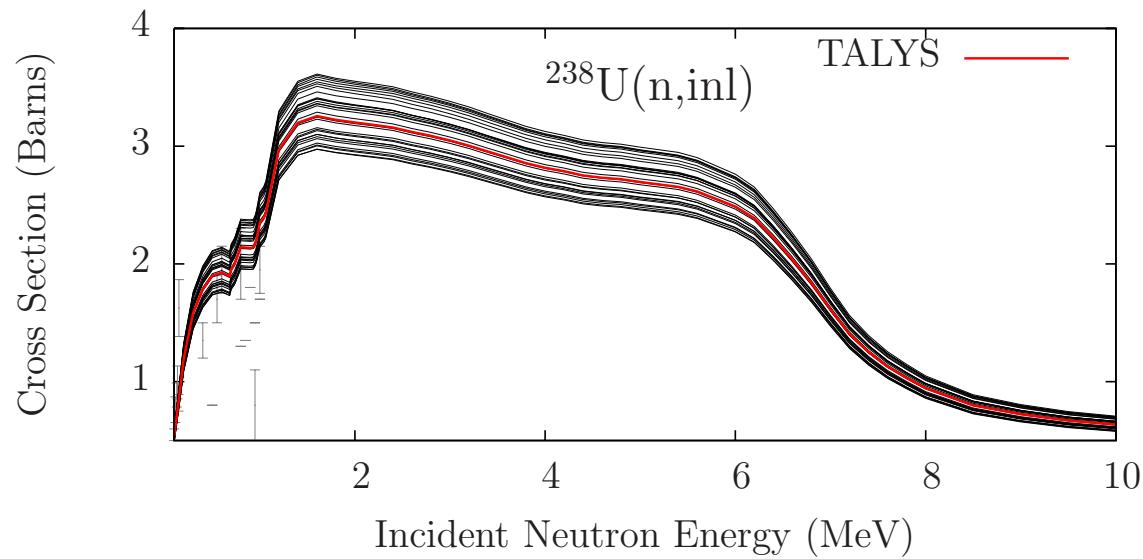
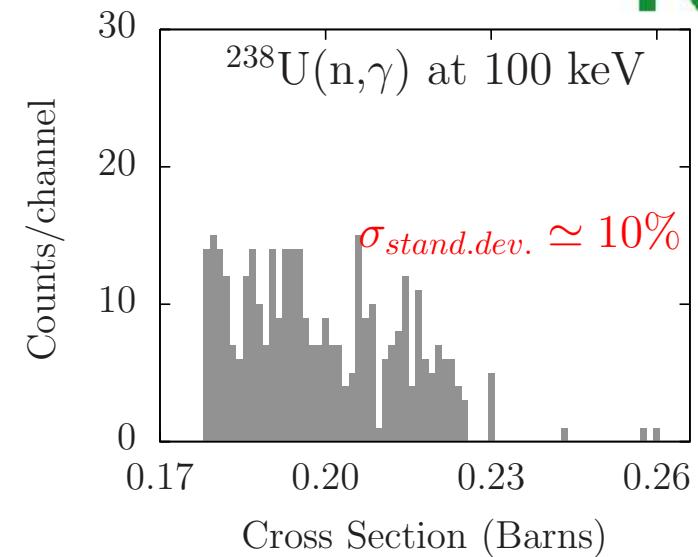
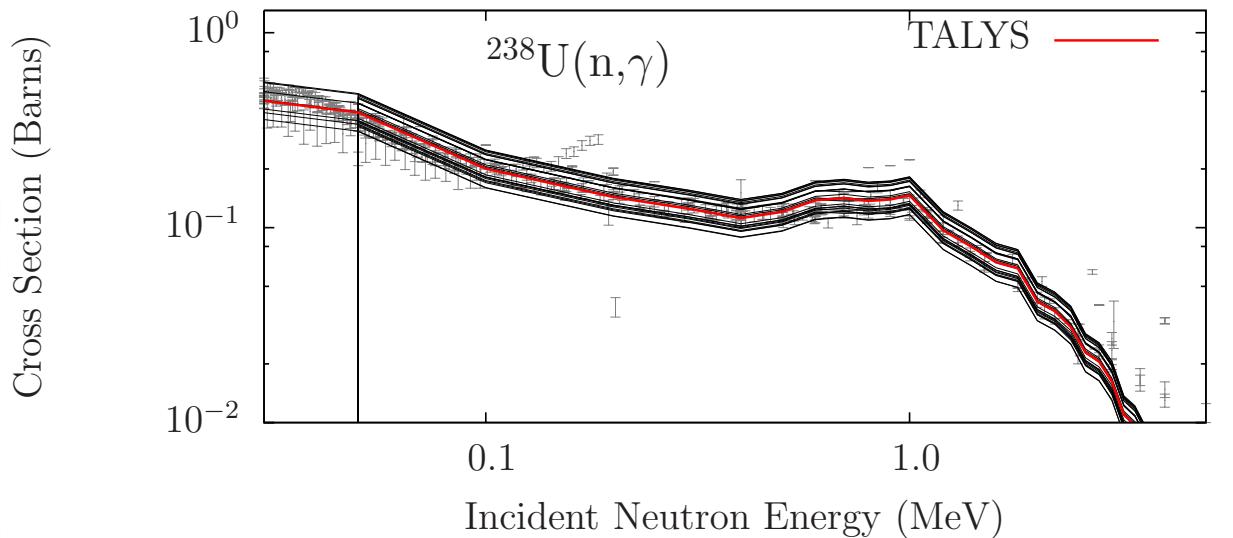
1000  
times

For each random ENDF file, the benchmark calculation is performed with MCNP. At the end of the  $n$  calculations,  $n$  different  $k_{\text{eff}}$  values are obtained.

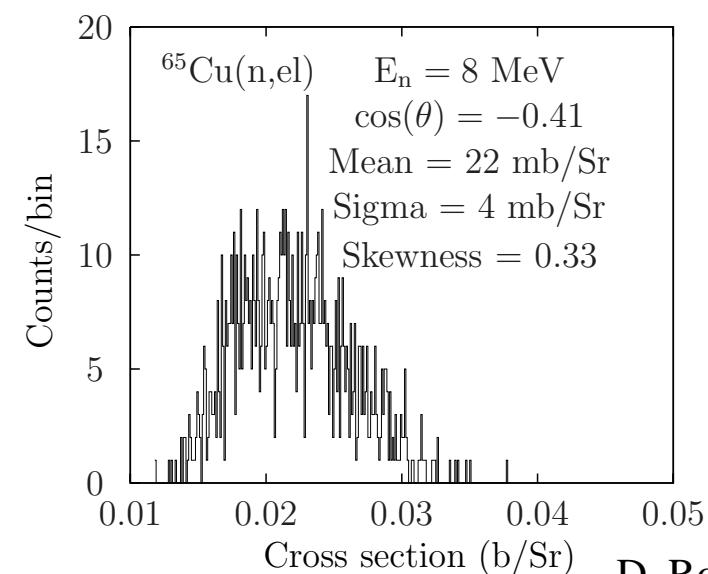
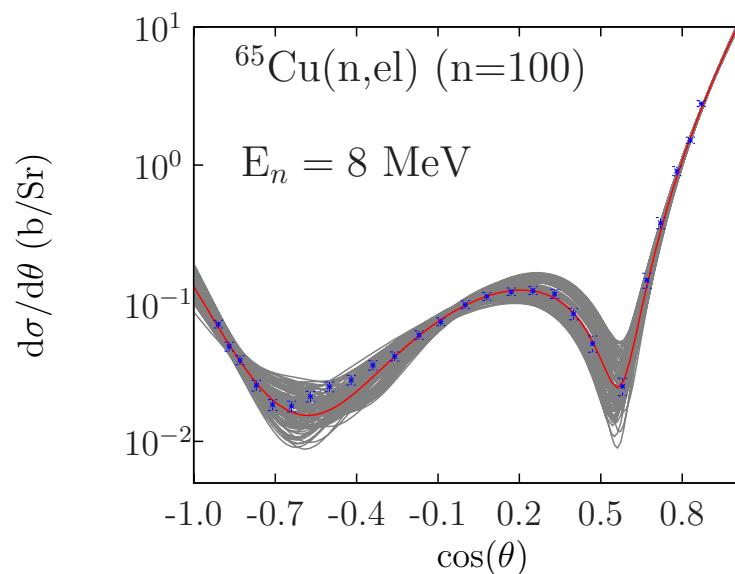
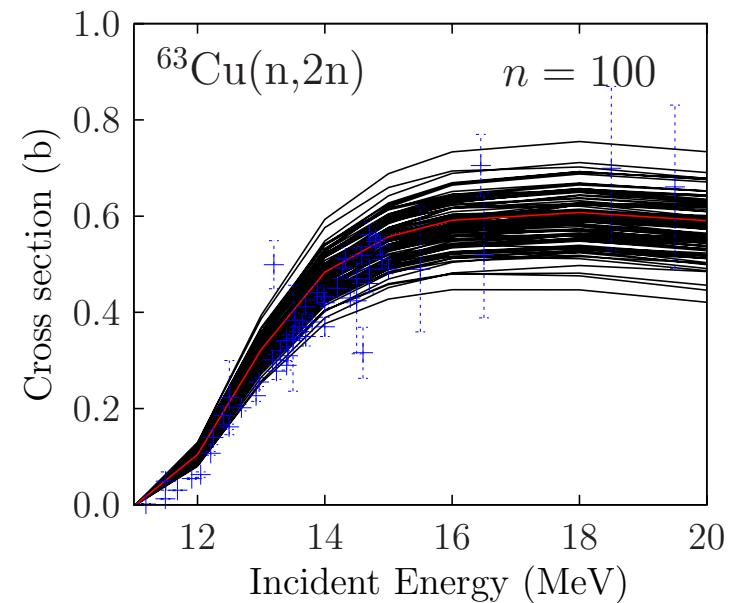
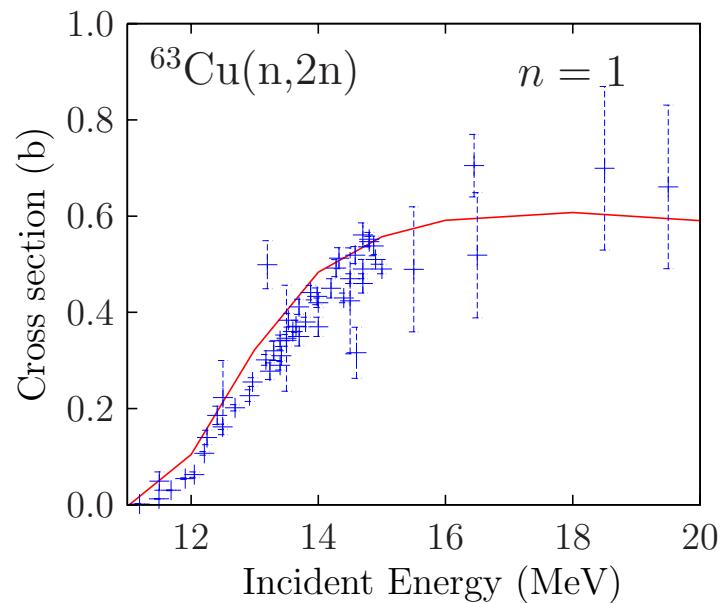
$$\sigma_{\text{total}}^2 = \sigma_{\text{statistics}}^2 + \sigma_{\text{nuclear data}}^2$$



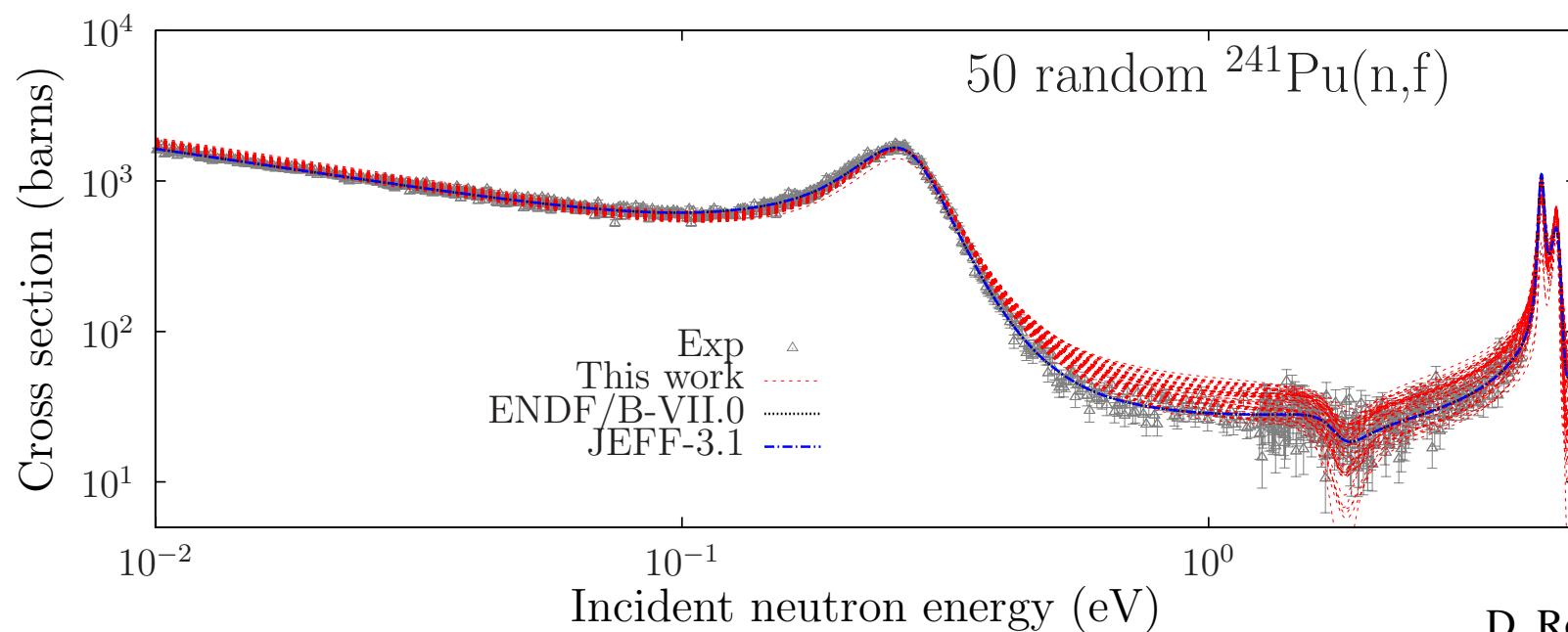
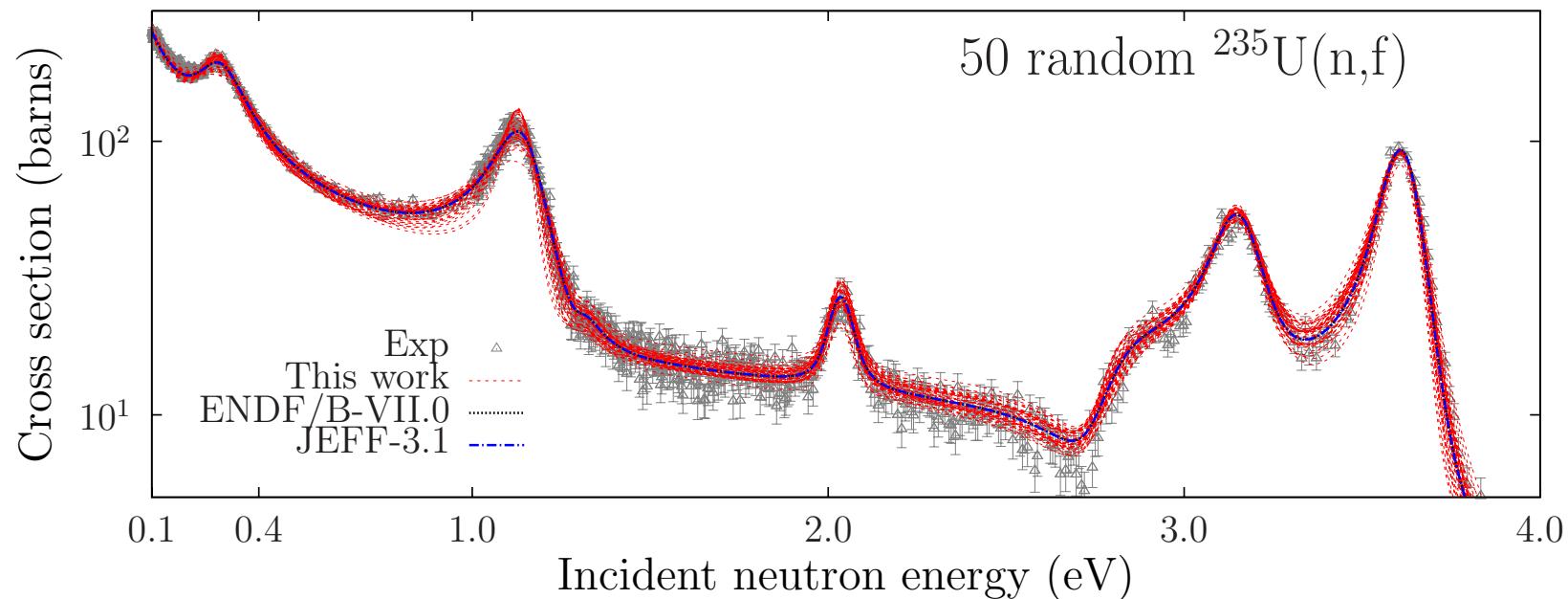
# Example with $^{238}\text{U}$ : Monte Carlo calculations



# Examples with $^{63}\text{Cu}(n,2n)$ and $^{65}\text{Cu}(n,\text{el})$



# Nuclear data: examples in the resonance region

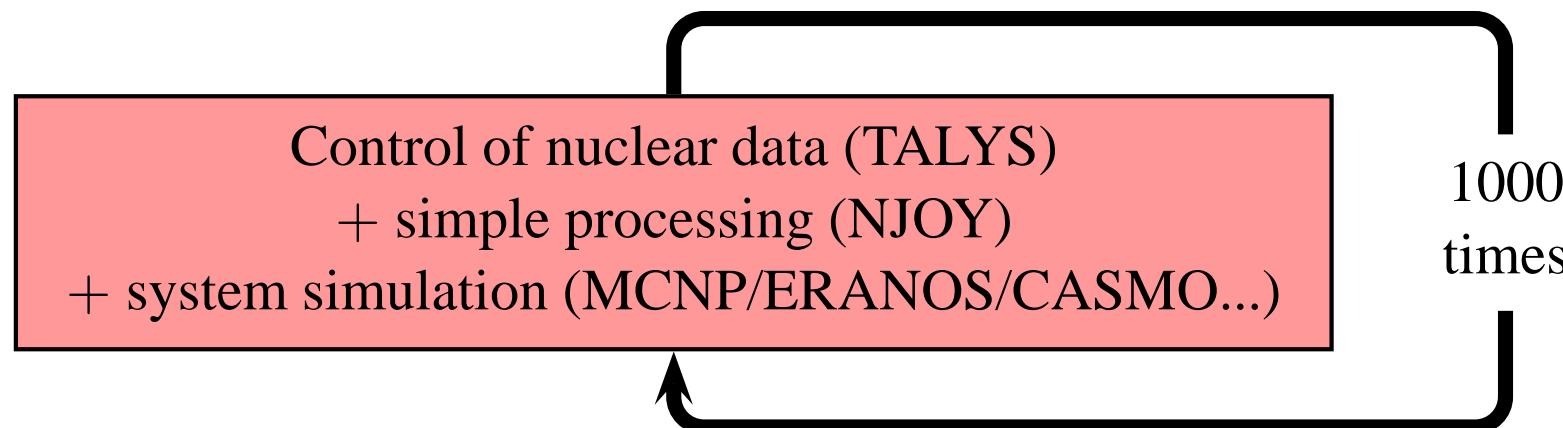


# TMC versus Perturbation method



- ① Obtain uncertainties on large-scale models due to nuclear data uncertainties
- ② Systematic approach, reliable and reproducible

## Solution (1): Total Monte Carlo



## Solution (2): Perturbation method

⇒ MCNP + Perturbation cards + covariance files

# TMC versus Perturbation: Results



Comparison TMC-Perturbation methods for a few  $k_{\text{eff}}$  benchmarks. The ratio in the last column is "TMC over Perturbation".

Benchmark	Isotopes	Total Monte Carlo Uncertainty due to nuclear data (pcm)	Perturbation Uncertainty due to nuclear data (pcm)	Ratio
hst39-6	$^{19}\text{F}$	330	290	1.16
hmf7-34	$^{19}\text{F}$	350	290	1.21
ict3-132	$^{90}\text{Zr}$	190	150	1.29
hmf57-1	$^{208}\text{Pb}$	500	410	1.22
pmf2	$^{239}\text{Pu}$	840	720	1.16
pmf2	$^{240}\text{Pu}$	790	650	1.21

# Results: Details of the TMC-Perturbation methods for $^{239,240}\text{Pu}$ $k_{\text{eff}}$ benchmarks



	pmf2 $^{239}\text{Pu}$			pmf2 $^{240}\text{Pu}$	
	$\Delta k_{\text{eff}}$ (pcm)			$\Delta k_{\text{eff}}$ (pcm)	
	TMC	Perturbation		TMC	Perturbation
Total	840	720		790	650
MF1	400	-		370	-
(n,inl)	170	140		70	50
(n,el)	250	240		30	40
(n, $\gamma$ )	100	100		30	30
(n,f)	720	660		730	640
MF4	20	-		20	-
MF5	50	-		30	-
MF6	50	-		30	-

# Considered data in TMC (or fast TMC)



Several hundreds of random ENDF files for transport + depletion

- 3 Major actinides:  $^{235}\text{U}$ ,  $^{238}\text{U}$ ,  $^{239}\text{Pu}$ ,
- Light elements: lighter than oxygen,
- 2 Thermal scattering data: H in  $\text{H}_2\text{O}$ , D in  $\text{D}_2\text{O}$
- All Fission yields (e.g.  $^{234,235,236,238}\text{U}$ ,  $^{239,240,241}\text{Pu}$ ,  $^{237}\text{Np}$ ,  $^{241,243}\text{Am}$ ,  $^{243,244}\text{Cm}$ ),
- All Minor actinides (e.g.  $^{234,236,237}\text{U}$ ,  $^{237}\text{Np}$ ,  $^{238,240,241,242}\text{Pu}$ , Am, Cm),
- All fission products (e.g. from Ge to Er), and decay data,

(fast) TMC can be applied to **any** input data, propagating uncertainties to **any** outputs

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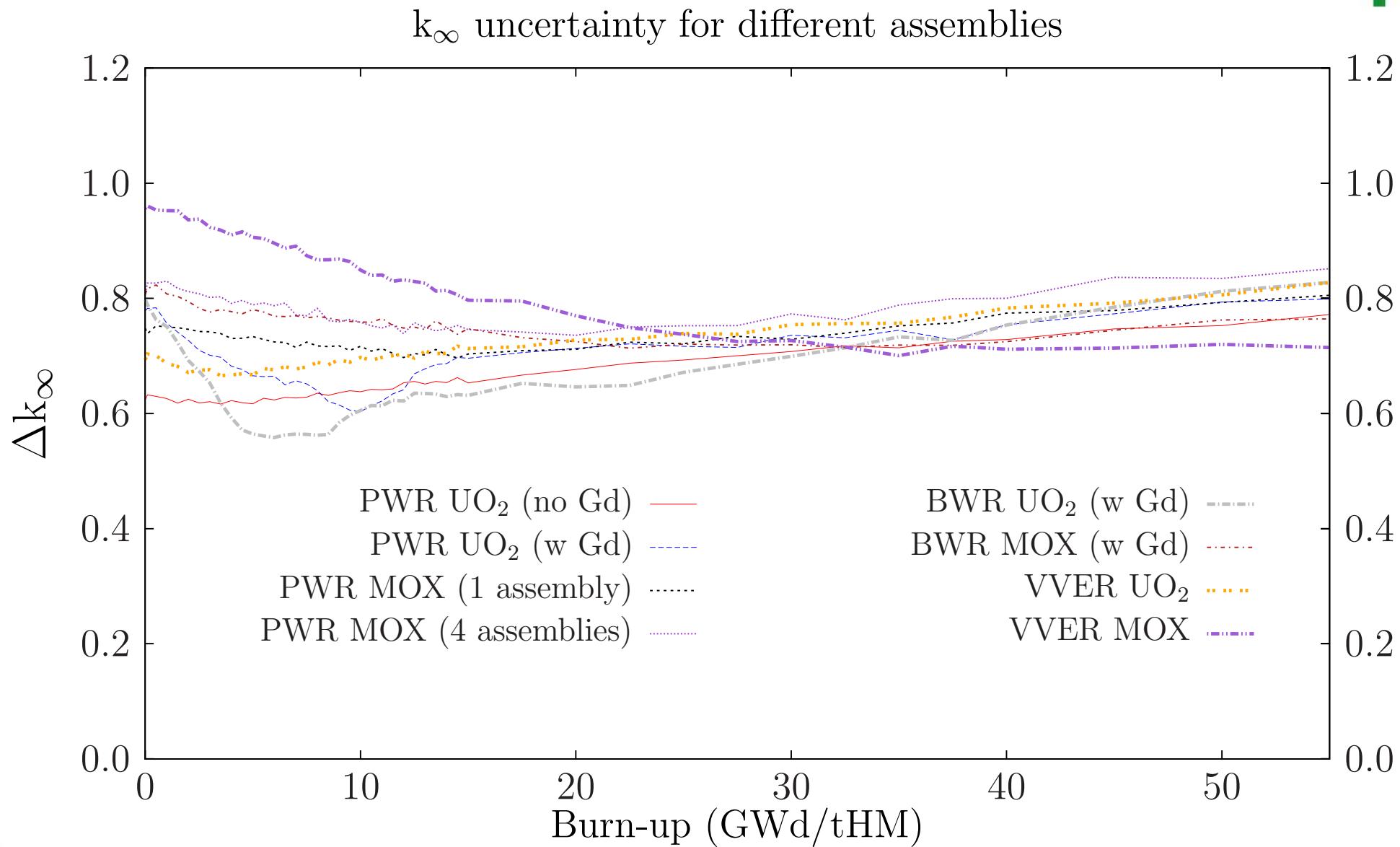
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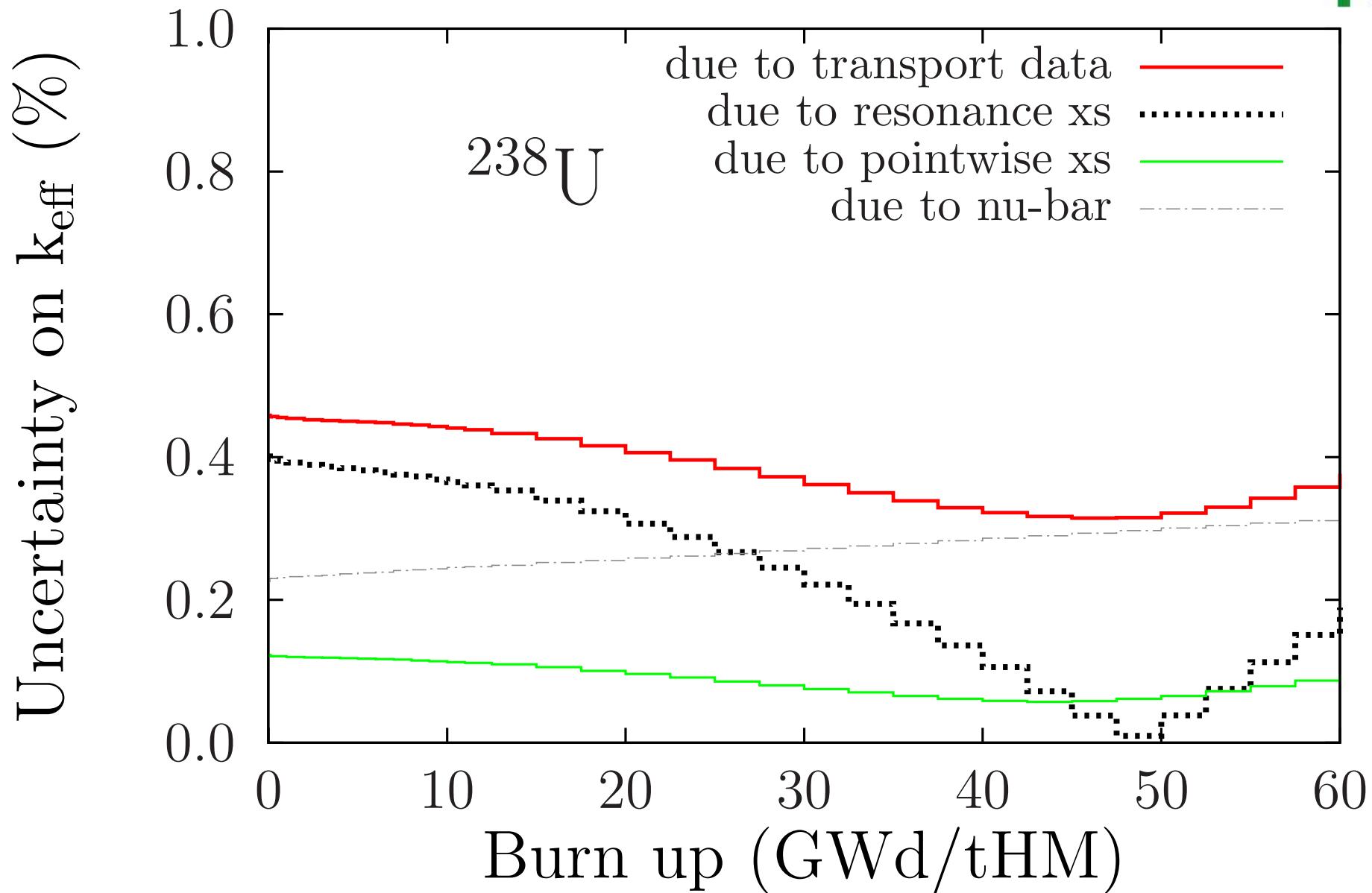
TMC was already applied to

- criticality-safety, shielding, pin-cell/assembly burn-up, activation,
- PWR, BWR, Gen-IV systems,
- $\text{UO}_2$ , MOX fuels,
- MCNP, SERPENT, FISPACT, DRAGON, PANTHER, RELAP-5

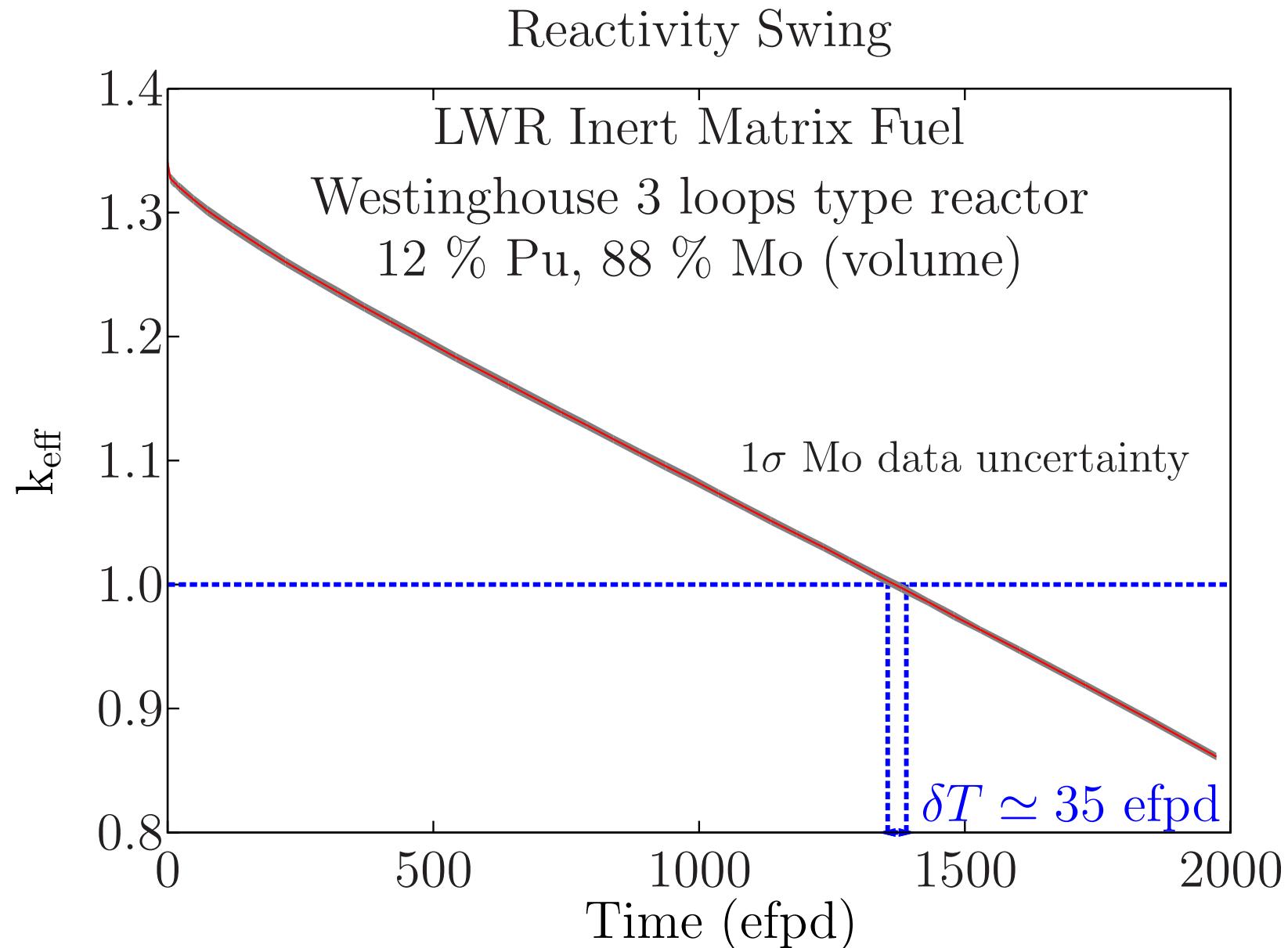
# Comparison of $\Delta k_\infty$ for assemblies and full core (SERPENT)



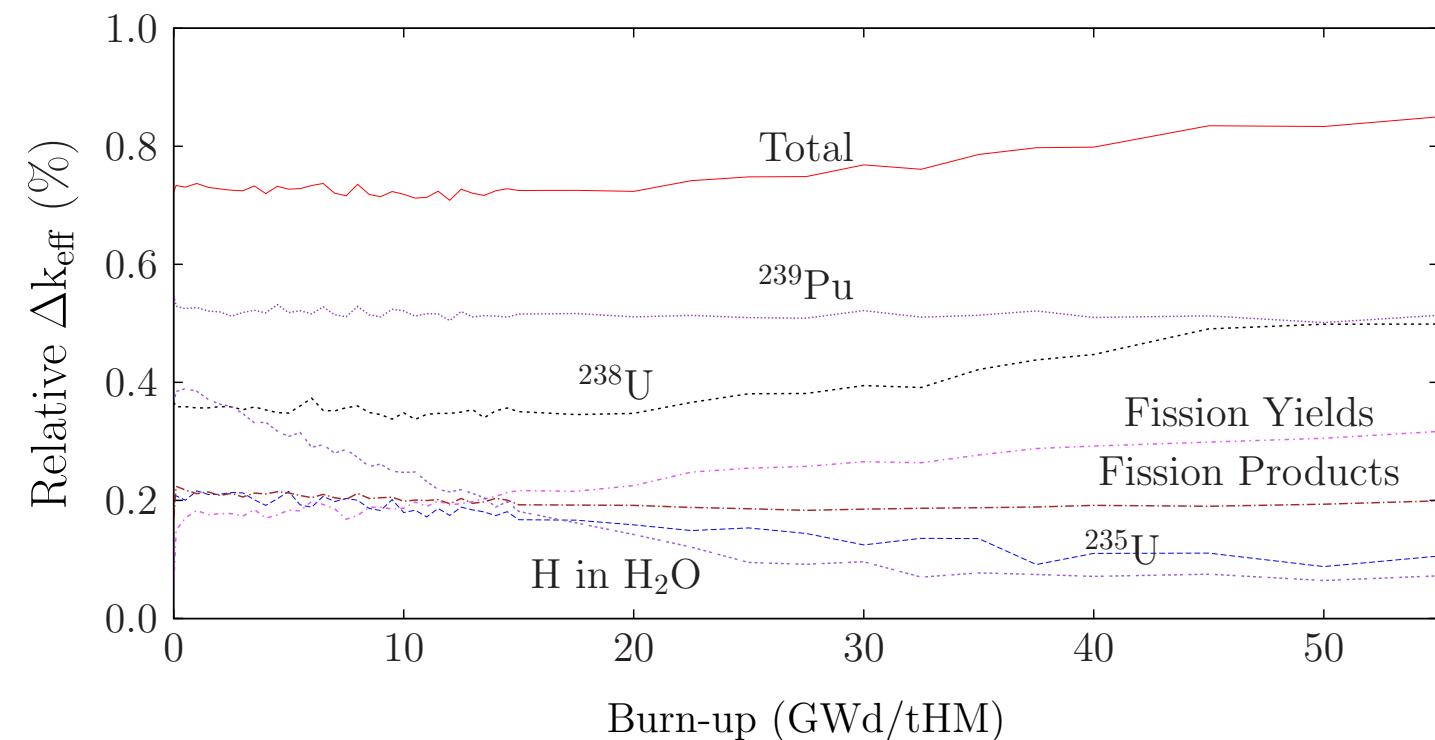
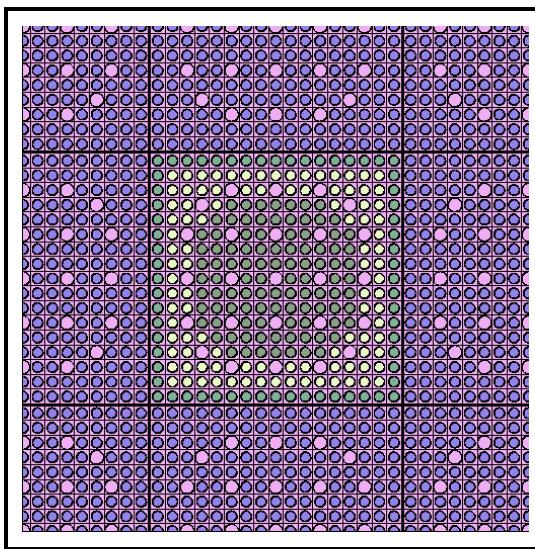
# TMC applied to PWR assembly burn-up calculations with DRAGON



# Example of TMC for the impact of the matrix fuel



# PWR MOX assembly uncertainties



- 1 MOX assembly surrounded by UO<sub>2</sub> assemblies,
- Burn-up calculated with SERPENT,
- All major nuclear data taken into account.

# Effect of H in H<sub>2</sub>O for a full core PWR (courtesy of O. Cabellos, UPM, Spain)



Method: TMC applied to COBAYA (3D multigroup core calculations) + SIMULA (coupled neutronic-thermohydraulics 3D core calculations)

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## III.2 PWR problem description

PWR (WESTINGHOUSE), 3 loops , 157 FA, power 2775. MWth

**1/4 CORE**

	1	2	3	4	5	6	7	8	→
1	1	13	4	21	6	21	16	14	
2	13	11	15	2	16	6	20	7	
3	4	15	3	21	8	22	19		
4	21	2	21	9	18	20	5		
5	6	16	8	18	12	17			
6	21	6	22	20	17				
7	16	20	19	10					
8	14	7							

↓

**AVE. BURNUP PER FUEL ASSEMBLY**

	1	2	3	4	5	6	7	8
1	18.137	11.662	27.397	0.000	30.867	0.000	14.984	11.662
2	11.662	16.188	13.130	28.902	12.155	28.866	0.000	30.191
3	27.397	13.130	27.572	0.000	22.778	0.000	0.000	
4	0.000	28.902	0.000	30.755	15.236	0.000	30.124	
5	30.867	12.155	22.778	15.236	13.123	14.882		
6	0.000	28.866	0.000	0.000	14.882			
7	14.984	0.000	0.000	30.503				
8	11.662	30.191						

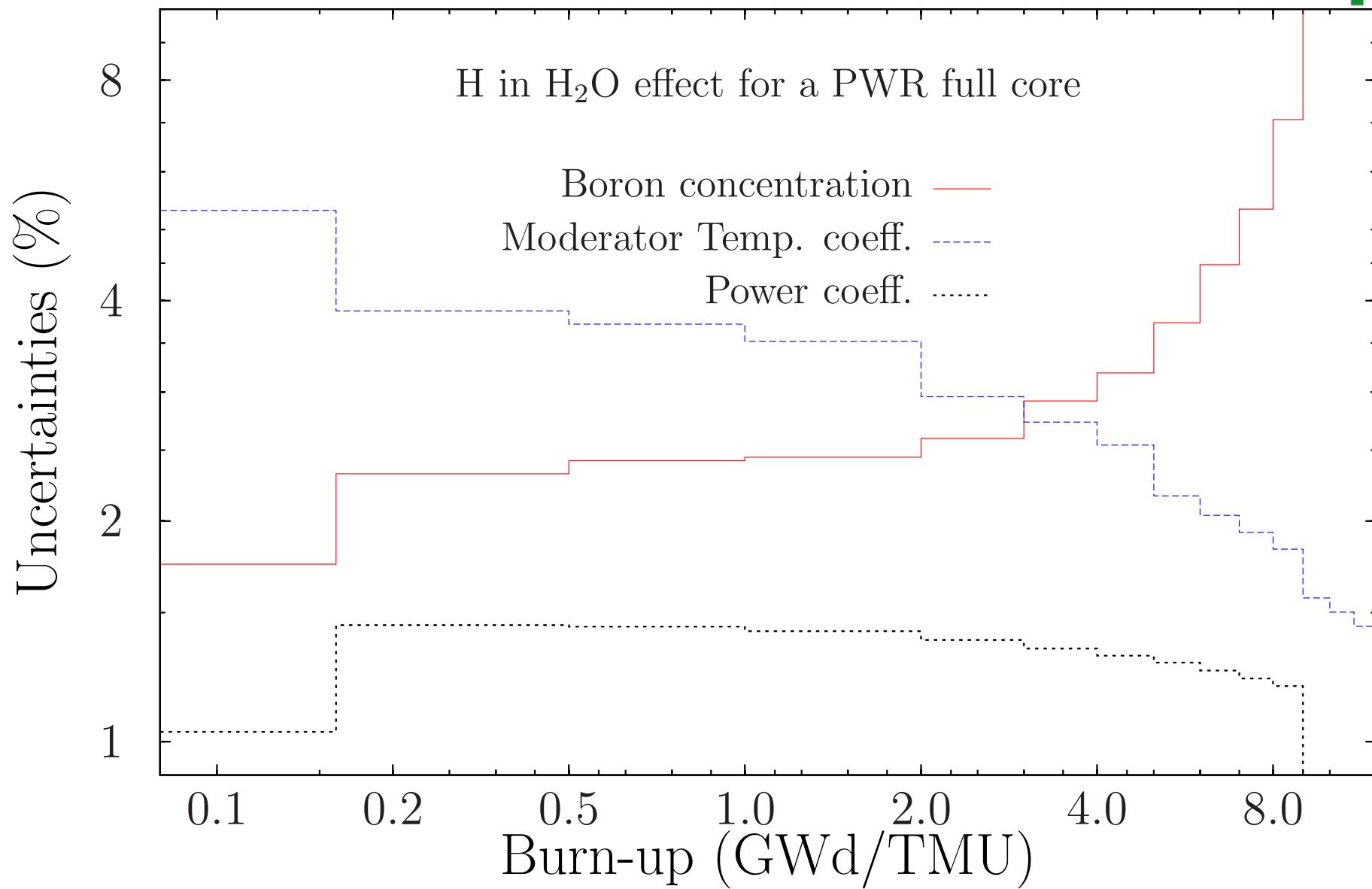
**FUEL TYPE w/o(%) WABAS**

1	OFA	2.10	0
2	OFA	3.10	0
3	OFA	3.24	0
4	OFA	3.24	0
5	OFA	3.24	0
6	OFA	3.24	0
7	OFA	3.24	0
8	OFA	3.24	0
9	OFA	3.24	0
10	OFA	3.24	0
11	OFA	3.24	0
12	AEF	3.60	0
13	AEF	3.60	0
14	AEF	3.60	0
15	AEF	3.60	0
16	AEF	3.60	0
17	AEF	3.60	0
18	AEF	3.60	0
19	AEF	3.60	0
20	AEF	3.60	4
21	AEF	3.60	8
22	AEF	3.60	12

**UAM7 – Paris (France), April 10-12, 2013**

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# Effect of H in $H_2O$ for a full core PWR (courtesy of O. Cabellos, UPM, Spain)



## Drawbacks of the TMC method



In TMC:

*If we can do a calculation **once**, we can also do it a **1000** times, each time with a varying data library.*

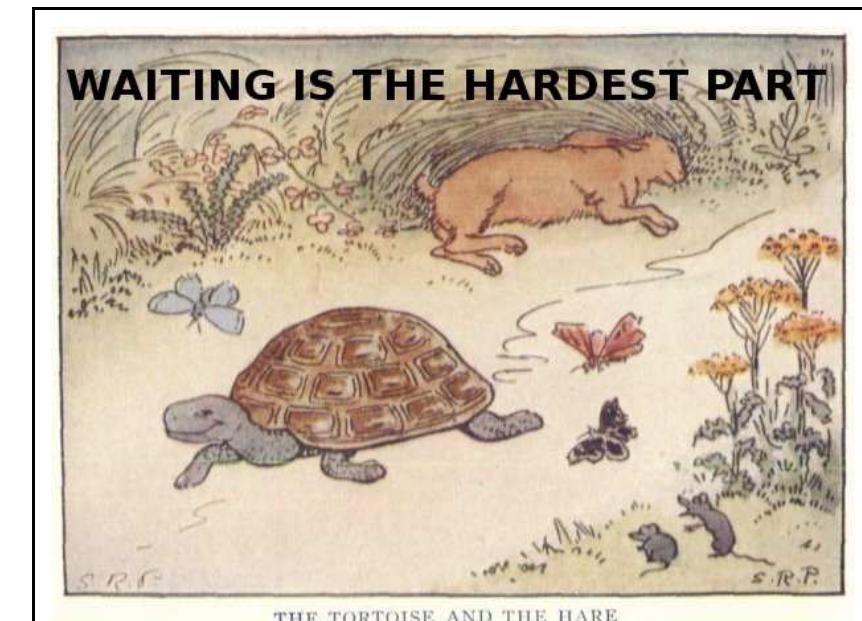
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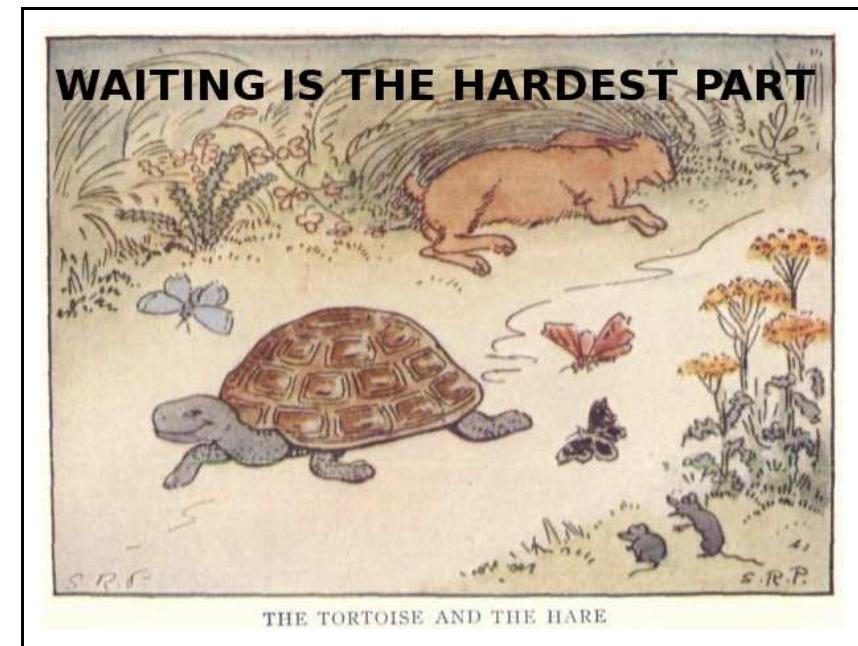
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There is a solution with Monte Carlo codes.



If a single calculation takes  $m$  histories ( $\sigma_{\text{stat}}$  small enough),  
then repeat it  $n$  times with  $m/n$  histories,  
random nuclear data and random seeds.

$$\sigma_{\text{total}}^2 = \sigma_{\text{statistics}}^2 + \sigma_{\text{nuclear data}}^2 \text{ still holds.}$$

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run 0   ENDF/B-VII.1   seed  $s_0$     $m$  histories   T sec.    $k \pm \sigma_{\text{stat}}$

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:	:	:			:
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$$\left\{ \begin{array}{l} \sigma_{\text{total}}^2 = \frac{1}{n-1} \sum_{i=1}^n (k_i - \bar{k})^2 \\ \sigma_{\text{statistics}}^2 = \frac{1}{n} \sum_{i=1}^n \sigma_i^2 \end{array} \right.$$

# The fast TMC method

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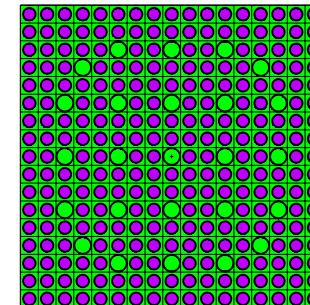
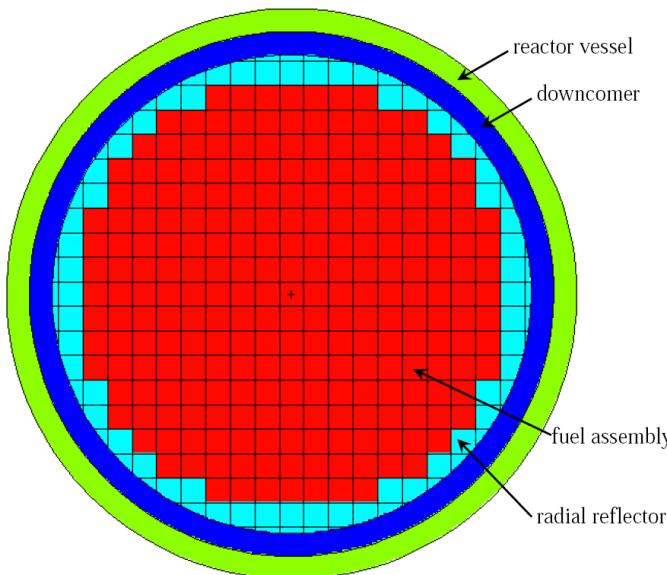


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MCNP model: 241 fuel assemblies, with 264 fuel pins each

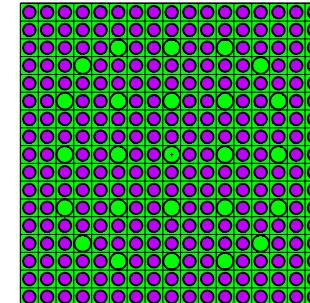
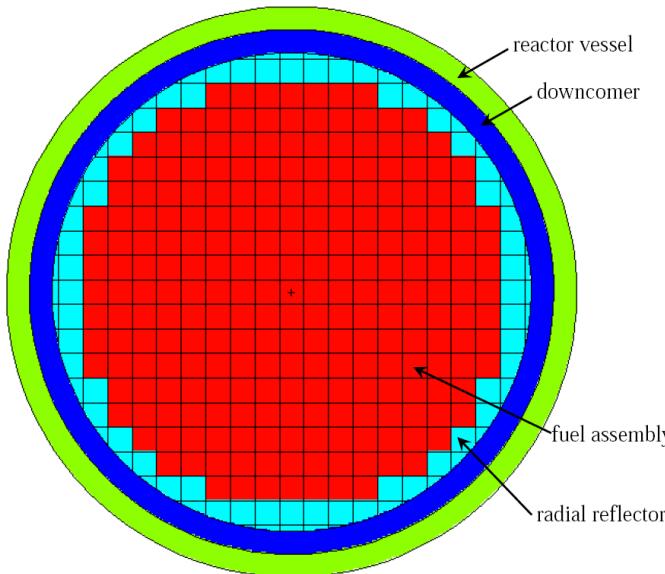


$\Rightarrow 357 \times 357 \times 100$  regions ( $1.26 \times 1.26 \times 3.66 \text{ cm}^3$ ): 12.7 million cells

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Uncertainty on generated local pin power (tally f7) due to  $^{235}\text{U}$ ,  $^{238}\text{U}$ ,  $^{239}\text{Pu}$  and H in  $\text{H}_2\text{O}$  thermal scattering in **each cell** ?

## Fast TMC method

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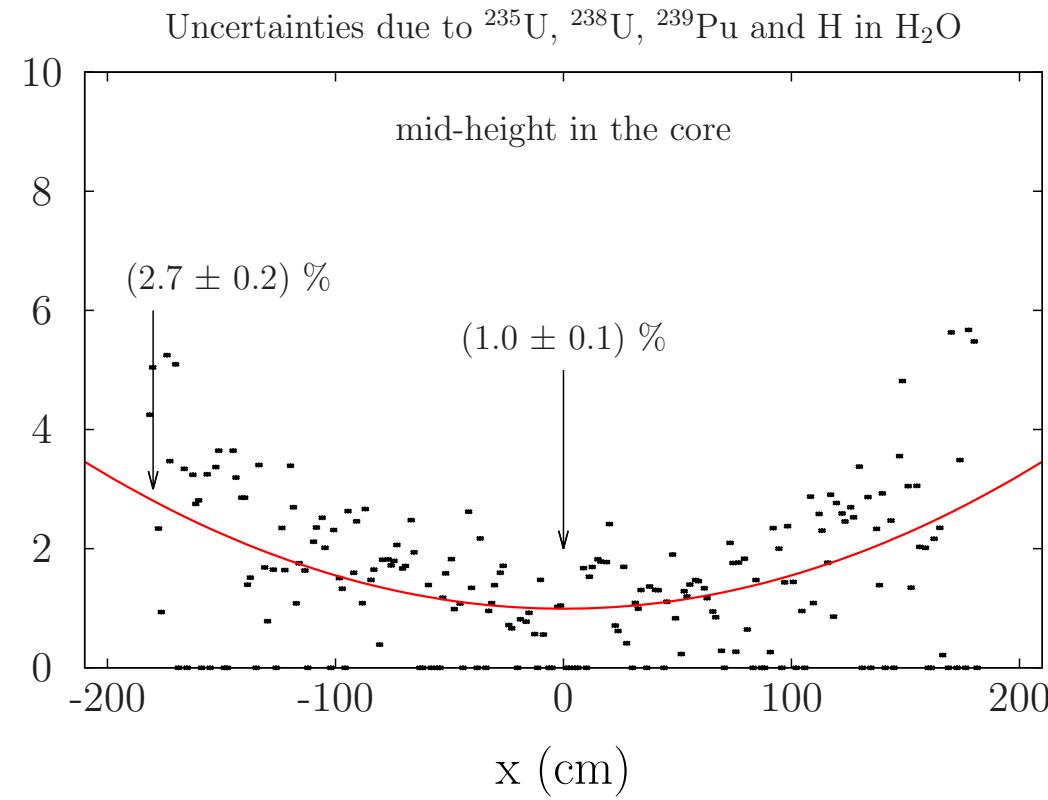
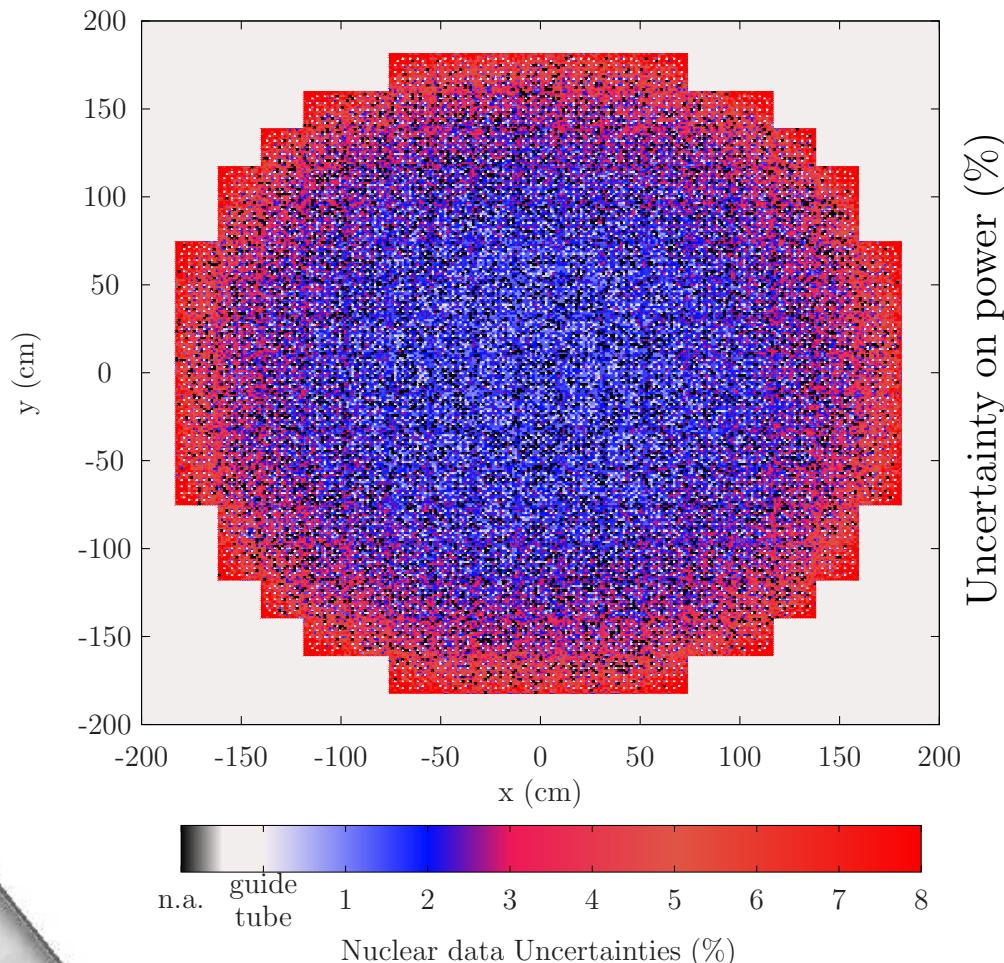
1 normal calculation without nuclear data uncertainty takes  $n = 2 \times 10^{11}$  histories  
( $\sigma_{\text{statistics}} = 0.25\%$  at the center, **500 weeks** on 1 cpu)

⇒ TMC: 500 random runs of  $n = 2 \times 10^{11}$  histories (**500 weeks** for each)

⇒ fast TMC: 500 random runs of  $n/500 = 4 \times 10^8$  histories (**1 week** for each)

# Fast TMC method

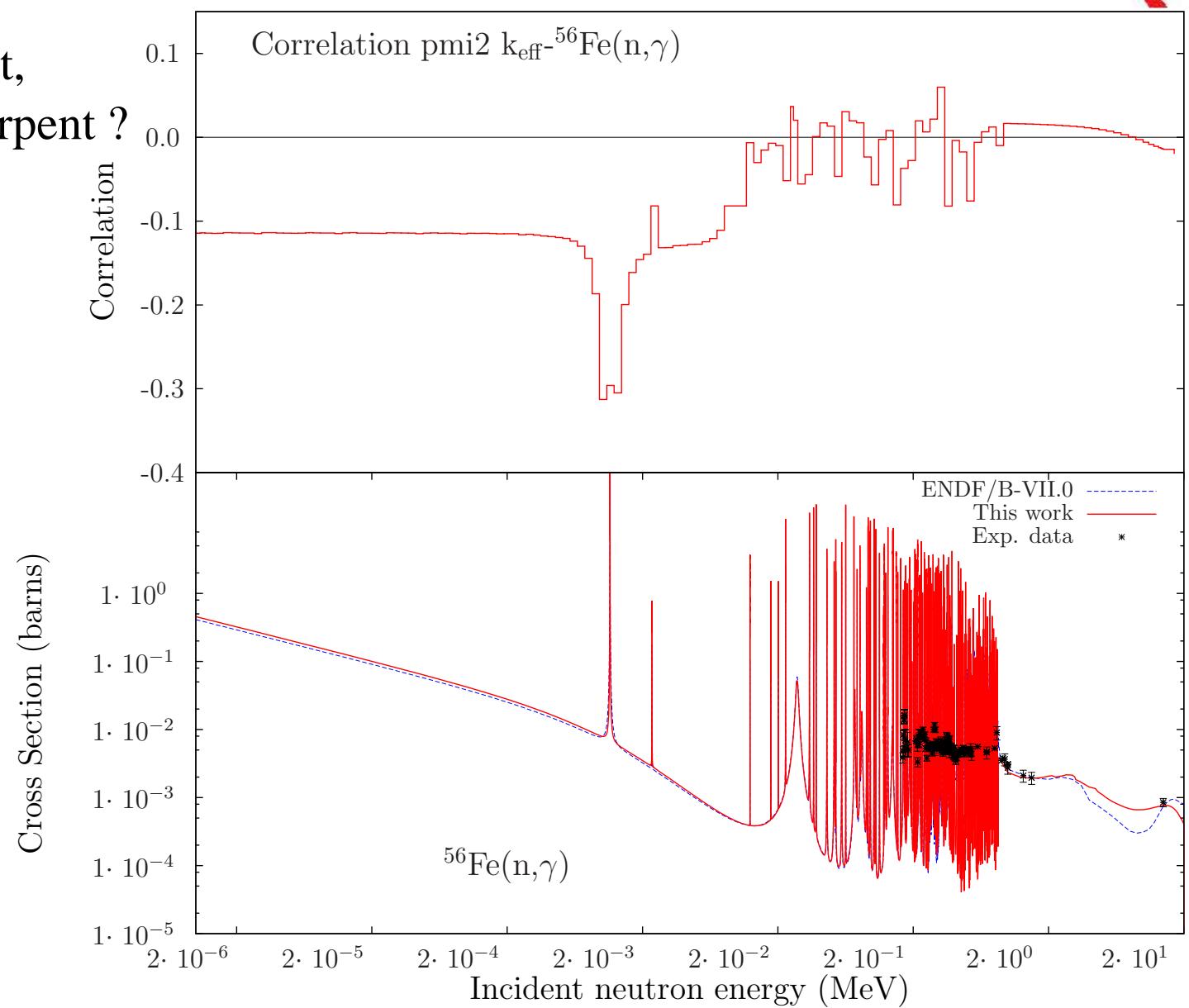
1 normal calculation without nuclear data uncertainty takes  $n = 2 \times 10^{11}$  histories  
( $\sigma_{\text{statistics}} = 0.25\%$  at the center, **500 weeks** on 1 cpu)  
⇒ TMC: 500 random runs of  $n = 2 \times 10^{11}$  histories (**500 weeks** for each)  
⇒ fast TMC: 500 random runs of  $n/500 = 4 \times 10^8$  histories (**1 week** for each)



# Other outcomes of the NRG approach (not detailed here)



- ⌘ Sensitivity,
- ⌘ Nuclear data adjustment,
- ⌘ Include fast TMC in Serpent ?



# Conclusions

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- ⇒ (fast) TMC is a powerful tool for uncertainty propagation,
- ⇒ All types of nuclear data impact can be assessed,
- ⇒ Most direct way to propagate uncertainties,
- ⇒ Better QA, better modern use of computers,
- ⇒ (fast) TMC is part of global approach to improve transparency and safety of nuclear simulation

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*TMC: If we can do a calculation **once**, we can also do it a **1000 times**, each time with a varying data library.*

# Conclusions



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*TMC: If we can do a calculation **once**, we can also do*

*fast TMC:*

*If we can do a calculation **once**, we can also get  
nuclear data uncertainties at the **same** time*